

1. Consider the system with transfer function

$$G(s) = \frac{Ks + 1}{s^3 + s^2 + (K + k)s + 1}$$

(a) For $K = 1$, find the sensitivity S_k^G of this transfer function with respect to k assuming nominal value $k = 2$. Then plot its magnitude as a function of frequency.

(b) Repeat (a) with $K = 100$ and compare the effect of a large loop gain on the sensitivity.

2. In many instances, steady state errors in control system are due to some non-linearities such as dead zones. A 'Class B' amplifier is a typical example of a device having a dead zone where it takes ~ 1 Volt of input signal to turn on the transistor. Once the device is on, however, it can be assumed to function linearly. The Class B amplifier in Figure 1 can be characterized mathematically (assuming a 1V threshold voltage and $V_{cc} = \infty$) by $N(\cdot)$ which is given by:

$$Y = \begin{cases} 0 & \text{if } -1 \leq U \leq 1, \\ U - 1 & \text{if } U > 1, \\ U + 1 & \text{if } U < -1. \end{cases}$$

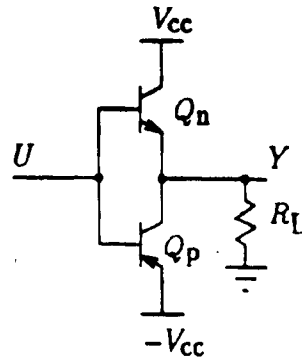


Figure 1: Class B Amplifier Circuit

(a) Develop a plot of Y versus R with $K = 1$ in Figure 2.

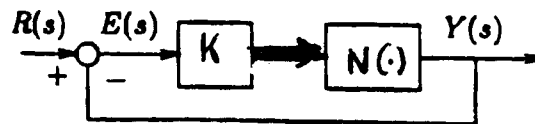


Figure 2: Feedback System

(b) If $r(t) = 5 \sin(t)$, sketch $y(t)$.