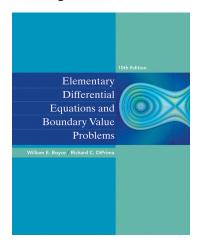
A Solution Manual For

Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima



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1.1 problem 1

Internal problem ID [448]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40

Problem number: 1.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$3y + y' - e^{-2t} - t = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 19

dsolve(3*y(t)+diff(y(t),t) = exp(-2*t)+t,y(t), singsol=all)

$$y(t) = \frac{t}{3} - \frac{1}{9} + e^{-2t} + c_1 e^{-3t}$$

✓ Solution by Mathematica

Time used: 0.084 (sec). Leaf size: 27

DSolve[3*y[t]+y'[t] == Exp[-2*t]+t,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{1}{9}(3t-1) + e^{-3t}(e^t + c_1)$$

1.2 problem 2

Internal problem ID [449]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40

Problem number: 2.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$-2y + y' - e^{2t}t^2 = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 16

 $dsolve(-2*y(t)+diff(y(t),t) = exp(2*t)*t^2,y(t), singsol=all)$

$$y(t) = \left(\frac{t^3}{3} + c_1\right) e^{2t}$$

✓ Solution by Mathematica

Time used: 0.043 (sec). Leaf size: 22

DSolve[-2*y[t]+y'[t]== Exp[2*t]*t^2,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{1}{3}e^{2t}(t^3 + 3c_1)$$

1.3 problem 3

Internal problem ID [450]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40

Problem number: 3.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$y + y' - 1 - t e^{-t} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 18

dsolve(y(t)+diff(y(t),t) = 1+t/exp(t),y(t), singsol=all)

$$y(t) = \left(\frac{t^2}{2} + e^t + c_1\right) e^{-t}$$

✓ Solution by Mathematica

Time used: 0.052 (sec). Leaf size: 23

DSolve[y[t]+y'[t] == 1+t/Exp[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to 1 + e^{-t} \left(\frac{t^2}{2} + c_1 \right)$$

1.4 problem 4

Internal problem ID [451]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40

Problem number: 4.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$\frac{y}{t} + y' - 3\cos(2t) = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 23

dsolve(y(t)/t+diff(y(t),t) = 3*cos(2*t),y(t), singsol=all)

$$y(t) = \frac{\frac{3\cos(2t)}{4} + \frac{3\sin(2t)t}{2} + c_1}{t}$$

✓ Solution by Mathematica

Time used: 0.072 (sec). Leaf size: 30

DSolve[y[t]/t+y'[t] == 3*Cos[2*t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{6t\sin(2t) + 3\cos(2t) + 4c_1}{4t}$$

1.5 problem 5

Internal problem ID [452]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40

Problem number: 5.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$-2y + y' - 3e^t = 0$$

Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

dsolve(-2*y(t)+diff(y(t),t) = 3*exp(t),y(t), singsol=all)

$$y(t) = -3e^t + c_1e^{2t}$$

✓ Solution by Mathematica

Time used: 0.049 (sec). Leaf size: 17

DSolve[-2*y[t]+y'[t] == 3*Exp[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow e^t \left(-3 + c_1 e^t \right)$$

1.6 problem 6

Internal problem ID [453]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40

Problem number: 6.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$2y + ty' - \sin(t) = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

dsolve(2*y(t)+t*diff(y(t),t) = sin(t),y(t), singsol=all)

$$y(t) = \frac{\sin(t) - \cos(t)t + c_1}{t^2}$$

✓ Solution by Mathematica

Time used: 0.043 (sec). Leaf size: 19

DSolve[2*y[t]+t*y'[t]== Sin[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow \frac{\sin(t) - t\cos(t) + c_1}{t^2}$$

1.7 problem 7

Internal problem ID [454]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40

Problem number: 7.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [_linear]

$$2yt + y' - 2t e^{-t^2} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 16

 $dsolve(2*t*y(t)+diff(y(t),t) = 2*t/exp(t^2),y(t), singsol=all)$

$$y(t) = (t^2 + c_1) e^{-t^2}$$

✓ Solution by Mathematica

Time used: 0.053 (sec). Leaf size: 19

DSolve[2*t*y[t]+y'[t] == 2*t/Exp[t^2],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to e^{-t^2} (t^2 + c_1)$$

1.8 problem 8

Internal problem ID [455]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40

Problem number: 8.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$4yt + (t^2 + 1)y' - \frac{1}{(t^2 + 1)^2} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 16

 $dsolve(4*t*y(t)+(t^2+1)*diff(y(t),t) = 1/(t^2+1)^2,y(t), singsol=all)$

$$y(t) = \frac{\arctan(t) + c_1}{(t^2 + 1)^2}$$

✓ Solution by Mathematica

Time used: 0.04 (sec). Leaf size: 18

 $DSolve [4*t*y[t]+(t^2+1)*y'[t] == 1/(t^2+1)^2, y[t], t, Include Singular Solutions \rightarrow True]$

$$y(t) o \frac{\arctan(t) + c_1}{(t^2 + 1)^2}$$

1.9 problem 9

Internal problem ID [456]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40

Problem number: 9.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$y + 2y' - 3t = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

dsolve(y(t)+2*diff(y(t),t) = 3*t,y(t), singsol=all)

$$y(t) = 3t - 6 + e^{-\frac{t}{2}}c_1$$

✓ Solution by Mathematica

Time used: 0.041 (sec). Leaf size: 20

DSolve[y[t]+2*y'[t] == 3*t,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow 3t + c_1 e^{-t/2} - 6$$

1.10 problem 10

Internal problem ID [457]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 10.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$ty' - y - t^2 e^{-t} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 14

 $dsolve(-y(t)+t*diff(y(t),t) = t^2/exp(t),y(t), singsol=all)$

$$y(t) = \left(-\mathrm{e}^{-t} + c_1\right)t$$

✓ Solution by Mathematica

Time used: 0.054 (sec). Leaf size: 16

DSolve[-y[t]+t*y'[t] == t^2/Exp[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow t(\sinh(t) - \cosh(t) + c_1)$$

1.11 problem 11

Internal problem ID [458]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 11.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$y + y' - 5\sin\left(2t\right) = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 21

dsolve(y(t)+diff(y(t),t) = 5*sin(2*t),y(t), singsol=all)

$$y(t) = -2\cos(2t) + \sin(2t) + e^{-t}c_1$$

✓ Solution by Mathematica

Time used: 0.087 (sec). Leaf size: 24

DSolve[y[t]+y'[t] == 5*Sin[2*t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \sin(2t) - 2\cos(2t) + c_1 e^{-t}$$

1.12 problem 12

Internal problem ID [459]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 12.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$y + 2y' - 3t^2 = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 20

 $dsolve(y(t)+2*diff(y(t),t) = 3*t^2,y(t), singsol=all)$

$$y(t) = 3t^2 - 12t + 24 + e^{-\frac{t}{2}}c_1$$

✓ Solution by Mathematica

Time used: 0.047 (sec). Leaf size: 23

DSolve[y[t]+2*y'[t] == 3*t^2,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow 3(t-4)t + c_1e^{-t/2} + 24$$

1.13 problem 13

Internal problem ID [460]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 13.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$-y + y' - 2e^{2t}t = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 16

dsolve([-y(t)+diff(y(t),t) = 2*exp(2*t)*t,y(0) = 1],y(t), singsol=all)

$$y(t) = (2t - 2)e^{2t} + 3e^{t}$$

✓ Solution by Mathematica

Time used: 0.052 (sec). Leaf size: 19

DSolve[{-y[t]+y'[t] == 2*Exp[2*t]*t,y[0]==1},y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow e^t (2e^t(t-1)+3)$$

1.14 problem 14

Internal problem ID [461]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 14.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$2y + y' - t e^{-2t} = 0$$

With initial conditions

$$[y(1) = 0]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

dsolve([2*y(t)+diff(y(t),t) = t/exp(2*t),y(1) = 0],y(t), singsol=all)

$$y(t) = \frac{(t^2 - 1)e^{-2t}}{2}$$

✓ Solution by Mathematica

Time used: 0.052 (sec). Leaf size: 19

 $DSolve[\{2*y[t]+y'[t] == t/Exp[2*t],y[1]==0\},y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \to \frac{1}{2}e^{-2t}(t^2 - 1)$$

1.15 problem 15

Internal problem ID [462]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 15.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$2y + ty' - t^2 + t - 1 = 0$$

With initial conditions

$$\left[y(1) = \frac{1}{2}\right]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 19

 $dsolve([2*y(t)+t*diff(y(t),t) = t^2-t+1,y(1) = 1/2],y(t), singsol=all)$

$$y(t) = \frac{t^2}{4} - \frac{t}{3} + \frac{1}{2} + \frac{1}{12t^2}$$

✓ Solution by Mathematica

Time used: 0.027 (sec). Leaf size: 22

 $DSolve[{2*y[t]+t*y'[t] == t^2-t+1,y[1]==1/2},y[t],t,IncludeSingularSolutions \rightarrow True}]$

$$y(t) \to \frac{1}{12} \left(3t^2 + \frac{1}{t^2} - 4t + 6 \right)$$

1.16 problem 16

Internal problem ID [463]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 16.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$\frac{2y}{t} + y' - \frac{\cos(t)}{t^2} = 0$$

With initial conditions

$$[y(\pi) = 0]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 10

 $dsolve([2*y(t)/t+diff(y(t),t) = cos(t)/t^2,y(Pi) = 0],y(t), singsol=all)$

$$y(t) = \frac{\sin(t)}{t^2}$$

✓ Solution by Mathematica

Time used: 0.04 (sec). Leaf size: 11

DSolve[{2*y[t]/t+y'[t] == Cos[t]/t^2,y[Pi]==0},y[t],t,IncludeSingularSolutions -> True]

$$y(t) o rac{\sin(t)}{t^2}$$

1.17 problem 17

Internal problem ID [464]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 17.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$-2y + y' - e^{2t} = 0$$

With initial conditions

$$[y(0) = 2]$$

✓ Solution by Maple

Time used: 0.328 (sec). Leaf size: 12

dsolve([-2*y(t)+diff(y(t),t) = exp(2*t),y(0) = 2],y(t), singsol=all)

$$y(t) = (2+t)e^{2t}$$

✓ Solution by Mathematica

Time used: 0.04 (sec). Leaf size: 14

DSolve[{-2*y[t]+y'[t] == Exp[2*t],y[0]==2},y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to e^{2t}(t+2)$$

1.18 problem 18

Internal problem ID [465]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 18.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [linear]

$$2y + ty' - \sin(t) = 0$$

With initial conditions

$$\left[y\left(\frac{\pi}{2}\right)=1\right]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 22

dsolve([2*y(t)+t*diff(y(t),t) = sin(t),y(1/2*Pi) = 1],y(t), singsol=all)

$$y(t) = \frac{\sin(t) - \cos(t)t + \frac{\pi^2}{4} - 1}{t^2}$$

✓ Solution by Mathematica

Time used: 0.034 (sec). Leaf size: 26

DSolve[{2*y[t]+t*y'[t] == Sin[t],y[Pi/2]==1},y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{4\sin(t) - 4t\cos(t) + \pi^2 - 4}{4t^2}$$

1.19 problem 19

Internal problem ID [466]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 19.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$4yt^2 + y't^3 - e^{-t} = 0$$

With initial conditions

$$[y(-1) = 0]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 16

 $dsolve([4*t^2*y(t)+t^3*diff(y(t),t) = exp(-t),y(-1) = 0],y(t), singsol=all)$

$$y(t) = -\frac{(t+1)e^{-t}}{t^4}$$

✓ Solution by Mathematica

Time used: 0.064 (sec). Leaf size: 18

DSolve[{4*t^2*y[t]+t^3*y'[t] == Exp[-t],y[-1]==0},y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to -\frac{e^{-t}(t+1)}{t^4}$$

1.20 problem 20

Internal problem ID [467]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 20.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$(t+1)y + ty' - t = 0$$

With initial conditions

$$[y(\ln(2)) = 1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 17

dsolve([(1+t)*y(t)+t*diff(y(t),t) = t,y(ln(2)) = 1],y(t), singsol=all)

$$y(t) = \frac{t - 1 + 2e^{-t}}{t}$$

✓ Solution by Mathematica

Time used: 0.032 (sec). Leaf size: 19

DSolve[{(1+t)*y[t]+t*y'[t]== t,y[Log[2]]==1},y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{t + 2e^{-t} - 1}{t}$$

1.21 problem 21

Internal problem ID [468]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

 ${\bf Section:}\ {\bf Section}\ 2.1.\ {\bf Page}\ 40$

Problem number: 21.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$-\frac{y}{2} + y' - 2\cos(t) = 0$$

With initial conditions

$$[y(0) = a]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 21

dsolve([-1/2*y(t)+diff(y(t),t) = 2*cos(t),y(0) = a],y(t), singsol=all)

$$y(t) = -\frac{4\cos(t)}{5} + \frac{8\sin(t)}{5} + e^{\frac{t}{2}}a + \frac{4e^{\frac{t}{2}}}{5}$$

✓ Solution by Mathematica

Time used: 0.052 (sec). Leaf size: 31

 $DSolve[\{-1/2*y[t]+y'[t] == 2*Cos[t],y[0]==a\},y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \to \frac{1}{5} ((5a+4)e^{t/2} + 8\sin(t) - 4\cos(t))$$

1.22 problem 22

Internal problem ID [469]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 22.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$-y + 2y' - e^{\frac{t}{3}} = 0$$

With initial conditions

$$[y(0) = a]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 18

dsolve([-y(t)+2*diff(y(t),t) = exp(1/3*t),y(0) = a],y(t), singsol=all)

$$y(t) = \left(-3 + (a+3)e^{\frac{t}{6}}\right)e^{\frac{t}{3}}$$

✓ Solution by Mathematica

Time used: 0.052 (sec). Leaf size: 26

 $DSolve[{-y[t]+2*y'[t] == Exp[1/3*t],y[0]==a},y[t],t,IncludeSingularSolutions \rightarrow True]}$

$$y(t) \to e^{t/3} ((a+3)e^{t/6} - 3)$$

1.23 problem 23

Internal problem ID [470]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 23.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$-2y + 3y' - e^{-\frac{\pi t}{2}} = 0$$

With initial conditions

$$[y(0) = a]$$

Solution by Maple

Time used: 0.031 (sec). Leaf size: 35

dsolve([-2*y(t)+3*diff(y(t),t) = exp(-1/2*Pi*t),y(0) = a],y(t), singsol=all)

$$y(t) = \frac{\left(3\pi a - 2e^{t(-\frac{\pi}{2} - \frac{2}{3})} + 4a + 2\right)e^{\frac{2t}{3}}}{3\pi + 4}$$

✓ Solution by Mathematica

Time used: 0.08 (sec). Leaf size: 43

 $DSolve[\{-2*y[t]+3*y'[t] == Exp[-1/2*Pi*t], y[0] == a\}, y[t], t, Include Singular Solutions \rightarrow True]$

$$y(t) \to \frac{e^{2t/3} \left((4+3\pi)a - 2e^{-\frac{1}{6}(4+3\pi)t} + 2 \right)}{4+3\pi}$$

1.24 problem 24

Internal problem ID [471]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 24.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$(t+1)y + ty' - 2te^{-t} = 0$$

With initial conditions

$$[y(1) = a]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 21

dsolve([(1+t)*y(t)+t*diff(y(t),t) = 2*t/exp(t),y(1) = a],y(t), singsol=all)

$$y(t) = \frac{(t^2 + a e - 1) e^{-t}}{t}$$

✓ Solution by Mathematica

Time used: 0.063 (sec). Leaf size: 22

DSolve[{(1+t)*y[t]+t*y'[t] == 2*t/Exp[t],y[1]==a},y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{e^{-t}(ea + t^2 - 1)}{t}$$

1.25 problem 25

Internal problem ID [472]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 25.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$2y + ty' - \frac{\sin(t)}{t} = 0$$

With initial conditions

$$\left[y\left(-\frac{\pi}{2}\right) = a\right]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 19

dsolve([2*y(t)+t*diff(y(t),t) = sin(t)/t,y(-1/2*Pi) = a],y(t), singsol=all)

$$y(t) = \frac{-\cos(t) + \frac{a\pi^2}{4}}{t^2}$$

✓ Solution by Mathematica

Time used: 0.041 (sec). Leaf size: 22

DSolve[{2*y[t]+t*y'[t] == Sin[t]/t,y[-Pi/2]==a},y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{\pi^2 a - 4\cos(t)}{4t^2}$$

1.26 problem 26

Internal problem ID [473]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 26.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$\cos(t) y + \sin(t) y' - e^t = 0$$

With initial conditions

$$[y(1) = a]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 18

$$\label{eq:decomposition} \\ \mbox{dsolve}([\cos(t)*y(t)+\sin(t)*\mbox{diff}(y(t),t) = \exp(t),y(1) = \mbox{a],y(t), singsol=all)} \\$$

$$y(t) = \csc(t) \left(e^t + a \sin(1) - e \right)$$

✓ Solution by Mathematica

Time used: 0.063 (sec). Leaf size: 19

$$y(t) \to \csc(t) \left(a \sin(1) + e^t - e \right)$$

1.27 problem 27

Internal problem ID [474]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 27.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$\frac{y}{2} + y' - 2\cos\left(t\right) = 0$$

With initial conditions

$$[y(0) = -1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 19

dsolve([1/2*y(t)+diff(y(t),t) = 2*cos(t),y(0) = -1],y(t), singsol=all)

$$y(t) = \frac{4\cos(t)}{5} + \frac{8\sin(t)}{5} - \frac{9e^{-\frac{t}{2}}}{5}$$

✓ Solution by Mathematica

Time used: 0.048 (sec). Leaf size: 27

 $DSolve[\{1/2*y[t]+y'[t] == 2*Cos[t],y[0]==-1\},y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \to \frac{1}{5} \left(-9e^{-t/2} + 8\sin(t) + 4\cos(t) \right)$$

1.28 problem 28

Internal problem ID [475]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

 ${\bf Section:}\ {\bf Section}\ 2.1.\ {\bf Page}\ 40$

Problem number: 28.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$\boxed{\frac{2y}{3} + y' - 1 + \frac{t}{2} = 0}$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

dsolve(2/3*y(t)+diff(y(t),t) = 1-1/2*t,y(t), singsol=all)

$$y(t) = -\frac{3t}{4} + \frac{21}{8} + e^{-\frac{2t}{3}}c_1$$

✓ Solution by Mathematica

Time used: 0.06 (sec). Leaf size: 24

DSolve[2/3*y[t]+y'[t] == 1-1/2*t,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow -\frac{3t}{4} + c_1 e^{-2t/3} + \frac{21}{8}$$

1.29 problem 29

Internal problem ID [476]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 29.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[linear, 'class A']]

$$\frac{y}{4} + y' - 3 - 2\cos(2t) = 0$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 24

dsolve([1/4*y(t)+diff(y(t),t) = 3+2*cos(2*t),y(0) = 0],y(t), singsol=all)

$$y(t) = 12 + \frac{8\cos(2t)}{65} + \frac{64\sin(2t)}{65} - \frac{788e^{-\frac{t}{4}}}{65}$$

✓ Solution by Mathematica

Time used: 0.156 (sec). Leaf size: 32

DSolve[{1/4*y[t]+y'[t] == 3+2*Cos[2*t],y[0]==0},y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{4}{65} \left(-197e^{-t/4} + 16\sin(2t) + 2\cos(2t) + 195 \right)$$

1.30 problem 30

Internal problem ID [477]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40 Problem number: 30.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$y + y' - 1 - 3\sin(t) = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 18

dsolve(-y(t)+diff(y(t),t) = 1+3*sin(t),y(t), singsol=all)

$$y(t) = -1 - \frac{3\cos(t)}{2} - \frac{3\sin(t)}{2} + c_1 e^t$$

✓ Solution by Mathematica

Time used: 0.069 (sec). Leaf size: 25

DSolve[-y[t]+y'[t] == 1+3*Sin[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to -\frac{3\sin(t)}{2} - \frac{3\cos(t)}{2} + c_1 e^t - 1$$

1.31 problem 31

Internal problem ID [478]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.1. Page 40

Problem number: 31.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$-\frac{3y}{2} + y' - 2e^t - 3t = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 19

dsolve(-3/2*y(t)+diff(y(t),t) = 2*exp(t)+3*t,y(t), singsol=all)

$$y(t) = -2t - \frac{4}{3} - 4e^t + e^{\frac{3t}{2}}c_1$$

✓ Solution by Mathematica

Time used: 0.097 (sec). Leaf size: 27

DSolve[-3/2*y[t]+y'[t] == 2*Exp[t]+3*t,y[t],t,IncludeSingularSolutions -> True]

$$y(t) o -2t - 4e^t + c_1 e^{3t/2} - rac{4}{3}$$

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2.1 problem 1

Internal problem ID [479]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 1.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{x^2}{y} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 33

 $dsolve(diff(y(x),x) = x^2/y(x),y(x), singsol=all)$

$$y(x) = -\frac{\sqrt{6x^3 + 9c_1}}{3}$$

$$y(x) = \frac{\sqrt{6x^3 + 9c_1}}{3}$$

✓ Solution by Mathematica

Time used: 0.08 (sec). Leaf size: 50

 $DSolve[y'[x] == x^2/y[x], y[x], x, IncludeSingularSolutions \rightarrow True]$

$$y(x) \to -\sqrt{\frac{2}{3}}\sqrt{x^3 + 3c_1}$$

$$y(x) \to \sqrt{\frac{2}{3}} \sqrt{x^3 + 3c_1}$$

2.2 problem 2

Internal problem ID [480]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 2.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [separable]

$$y' - \frac{x^2}{(x^3 + 1)y} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 39

 $dsolve(diff(y(x),x) = x^2/(x^3+1)/y(x),y(x), singsol=all)$

$$y(x) = -\frac{\sqrt{6\ln(x^3 + 1) + 9c_1}}{3}$$
$$y(x) = \frac{\sqrt{6\ln(x^3 + 1) + 9c_1}}{3}$$

✓ Solution by Mathematica

Time used: 0.09 (sec). Leaf size: 56

 $DSolve[y'[x] == x^2/(x^3+1)/y[x], y[x], x, IncludeSingularSolutions -> True]$

$$y(x) \to -\sqrt{\frac{2}{3}}\sqrt{\log(x^3+1) + 3c_1}$$

 $y(x) \to \sqrt{\frac{2}{3}}\sqrt{\log(x^3+1) + 3c_1}$

2.3 problem 3

Internal problem ID [481]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 3.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$\sin\left(x\right)y^2 + y' = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 14

 $dsolve(sin(x)*y(x)^2+diff(y(x),x) = 0,y(x), singsol=all)$

$$y(x) = -\frac{1}{\cos(x) - c_1}$$

✓ Solution by Mathematica

Time used: 0.132 (sec). Leaf size: 19

DSolve[Sin[x]*y[x]^2+y'[x]== 0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to -\frac{1}{\cos(x) + c_1}$$

$$y(x) \to 0$$

2.4 problem 4

Internal problem ID [482]

 \mathbf{Book} : Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 4.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [separable]

$$y' - \frac{3x^2 - 1}{3 + 2y} = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 45

 $dsolve(diff(y(x),x) = (3*x^2-1)/(3+2*y(x)),y(x), singsol=all)$

$$y(x) = -\frac{3}{2} - \frac{\sqrt{4x^3 + 4c_1 - 4x + 9}}{2}$$

$$y(x) = -\frac{3}{2} + \frac{\sqrt{4x^3 + 4c_1 - 4x + 9}}{2}$$

✓ Solution by Mathematica

Time used: 0.11 (sec). Leaf size: 59

DSolve[y'[x] == $(3*x^2-1)/(3+2*y[x]),y[x],x,IncludeSingularSolutions -> True$]

$$y(x) \to \frac{1}{2} \left(-3 - \sqrt{4x^3 - 4x + 9 + 4c_1} \right)$$

$$y(x) \to \frac{1}{2} \Big(-3 + \sqrt{4x^3 - 4x + 9 + 4c_1} \Big)$$

2.5 problem 5

Internal problem ID [483]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 5.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \cos(x)^2 \cos(2y)^2 = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 18

 $dsolve(diff(y(x),x) = cos(x)^2*cos(2*y(x))^2,y(x), singsol=all)$

$$y(x) = \frac{\arctan\left(x + 2c_1 + \frac{\sin(2x)}{2}\right)}{2}$$

✓ Solution by Mathematica

Time used: 1.283 (sec). Leaf size: 63

 $DSolve[y'[x] == Cos[x]^2*Cos[2*y[x]]^2,y[x],x,IncludeSingularSolutions -> True]$

$$y(x) \to \frac{1}{2}\arctan\left(x + \sin(x)\cos(x) + \frac{c_1}{4}\right)$$
$$y(x) \to \frac{1}{2}\arctan\left(x + \sin(x)\cos(x) + \frac{c_1}{4}\right)$$
$$y(x) \to -\frac{\pi}{4}$$
$$y(x) \to \frac{\pi}{4}$$

2.6 problem 6

Internal problem ID [484]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 6.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y'x - \sqrt{1 - y^2} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 9

 $dsolve(x*diff(y(x),x) = (1-y(x)^2)^(1/2),y(x), singsol=all)$

$$y(x) = \sin\left(\ln\left(x\right) + c_1\right)$$

✓ Solution by Mathematica

Time used: 0.213 (sec). Leaf size: 29

 $DSolve[x*y'[x] == (1-y[x]^2)^(1/2), y[x], x, IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \cos(\log(x) + c_1)$$

$$y(x) \rightarrow -1$$

$$y(x) \to 1$$

$$y(x) \to \text{Interval}[\{-1,1\}]$$

2.7 problem 7

Internal problem ID [485]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 7.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [' $y=_G(x,y')$ ']

$$y' - \frac{-\mathrm{e}^{-x} + x}{\mathrm{e}^y + x} = 0$$

X Solution by Maple

dsolve(diff(y(x),x) = (-exp(-x)+x)/(exp(y(x))+x),y(x), singsol=all)

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

 $DSolve[y'[x] == (-Exp[-x]+x)/(Exp[y[x]]+x), y[x], x, IncludeSingularSolutions \rightarrow True]$

Not solved

2.8 problem 8

Internal problem ID [486]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 8.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{x^2}{1 + y^2} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 353

$dsolve(diff(y(x),x) = x^2/(1+y(x)^2),y(x), singsol=all)$

$$\begin{split} y(x) &= \frac{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}{2} - \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}} \\ y(x) &= -\frac{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}{4} \\ &+ \frac{1}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &- \frac{i\sqrt{3}\left(\frac{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}{2} + \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}\right)}}{2} \\ y(x) &= -\frac{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}{4}}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{i\sqrt{3}\left(\frac{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}{2} + \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}\right)} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}{\left(4x^3 + 12c_1 + 4\sqrt{x^6 + 6c_1x^3 + 9c_1^2 + 4}\right)^{\frac{1}{3}}}} \\ &+ \frac{2}$$

✓ Solution by Mathematica

Time used: 2.147 (sec). Leaf size: 307

DSolve[y'[x] == $x^2/(1+y[x]^2)$, y[x], x, IncludeSingularSolutions -> True]

$$y(x) \to \frac{-2 + \sqrt[3]{2} \left(x^3 + \sqrt{x^6 + 6c_1x^3 + 4 + 9c_1^2 + 3c_1}\right)^{2/3}}{2^{2/3} \sqrt[3]{x^3 + \sqrt{x^6 + 6c_1x^3 + 4 + 9c_1^2} + 3c_1}}$$

$$y(x) \to \frac{i(\sqrt{3} + i) \sqrt[3]{x^3 + \sqrt{x^6 + 6c_1x^3 + 4 + 9c_1^2} + 3c_1}}{2\sqrt[3]{2}}$$

$$+ \frac{1 + i\sqrt{3}}{2^{2/3} \sqrt[3]{x^3 + \sqrt{x^6 + 6c_1x^3 + 4 + 9c_1^2} + 3c_1}}$$

$$y(x) \to \frac{1 - i\sqrt{3}}{2^{2/3} \sqrt[3]{x^3 + \sqrt{x^6 + 6c_1x^3 + 4 + 9c_1^2} + 3c_1}}$$

$$- \frac{(1 + i\sqrt{3}) \sqrt[3]{x^3 + \sqrt{x^6 + 6c_1x^3 + 4 + 9c_1^2} + 3c_1}}{2\sqrt[3]{2}}$$

2.9 problem 9

Internal problem ID [487]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 9.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - (1 - 2x) y^2 = 0$$

With initial conditions

$$\left[y(0) = -\frac{1}{6}\right]$$

✓ Solution by Maple

Time used: 0.109 (sec). Leaf size: 14

 $dsolve([diff(y(x),x) = (1-2*x)*y(x)^2,y(0) = -1/6],y(x), singsol=all)$

$$y(x) = \frac{1}{x^2 - x - 6}$$

✓ Solution by Mathematica

Time used: 0.137 (sec). Leaf size: 15

 $DSolve[\{y'[x] == (1-2*x)*y[x]^2,y[0] == -1/6\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{1}{x^2 - x - 6}$$

2.10 problem 10

Internal problem ID [488]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 10.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{1 - 2x}{y} = 0$$

With initial conditions

$$[y(1) = -2]$$

✓ Solution by Maple

Time used: 0.359 (sec). Leaf size: 18

dsolve([diff(y(x),x) = (1-2*x)/y(x),y(1) = -2],y(x), singsol=all)

$$y(x) = -\sqrt{-2x^2 + 2x + 4}$$

✓ Solution by Mathematica

Time used: 0.08 (sec). Leaf size: 24

 $DSolve[\{y'[x] == (1-2*x)/y[x],y[1] == -2\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \rightarrow -\sqrt{2}\sqrt{-x^2 + x + 2}$$

2.11 problem 11

Internal problem ID [489]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 11.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$x + e^{-x}y'y = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.125 (sec). Leaf size: 17

dsolve([x+y(x)*diff(y(x),x)/exp(x) = 0,y(0) = 1],y(x), singsol=all)

$$y(x) = \sqrt{-1 - 2x e^x + 2 e^x}$$

✓ Solution by Mathematica

Time used: 1.751 (sec). Leaf size: 19

 $DSolve[\{x+y[x]*y'[x]/Exp[x] == 0,y[0]==1\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \sqrt{-2e^x(x-1)-1}$$

2.12 problem 12

Internal problem ID [490]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 12.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$r' - \frac{r^2}{x} = 0$$

With initial conditions

$$[r(1) = 2]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 14

 $dsolve([diff(r(x),x) = r(x)^2/x,r(1) = 2],r(x), singsol=all)$

$$r(x) = -\frac{2}{2\ln(x) - 1}$$

✓ Solution by Mathematica

Time used: 0.135 (sec). Leaf size: 15

 $DSolve[\{r'[x] == r[x]^2/x, r[1] == 2\}, r[x], x, IncludeSingularSolutions \rightarrow True]$

$$r(x) \to \frac{2}{1 - 2\log(x)}$$

2.13 problem 13

Internal problem ID [491]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 13.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{2x}{y + x^2y} = 0$$

With initial conditions

$$[y(0) = -2]$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 18

 $dsolve([diff(y(x),x) = 2*x/(y(x)+x^2*y(x)),y(0) = -2],y(x), singsol=all)$

$$y(x) = -\sqrt{2\ln(x^2 + 1) + 4}$$

✓ Solution by Mathematica

Time used: 0.091 (sec). Leaf size: 24

 $DSolve[\{y'[x] == 2*x/(y[x]+x^2*y[x]),y[0]==-2\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to -\sqrt{2}\sqrt{\log(x^2+1)+2}$$

2.14 problem 14

Internal problem ID [492]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 14.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{xy^2}{\sqrt{x^2 + 1}} = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 17

 $dsolve([diff(y(x),x) = x*y(x)^2/(x^2+1)^(1/2),y(0) = 1],y(x), singsol=all)$

$$y(x) = -\frac{1}{\sqrt{x^2 + 1} - 2}$$

✓ Solution by Mathematica

Time used: 0.182 (sec). Leaf size: 20

 $DSolve[\{y'[x] == x*y[x]^2/(x^2+1)^(1/2),y[0]==1\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{1}{2 - \sqrt{x^2 + 1}}$$

2.15 problem 15

Internal problem ID [493]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 15.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{2x}{1+2y} = 0$$

With initial conditions

$$[y(2) = 0]$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 17

dsolve([diff(y(x),x) = 2*x/(1+2*y(x)),y(2) = 0],y(x), singsol=all)

$$y(x) = -\frac{1}{2} + \frac{\sqrt{4x^2 - 15}}{2}$$

✓ Solution by Mathematica

Time used: 0.1 (sec). Leaf size: 22

 $DSolve[\{y'[x] == 2*x/(1+2*y[x]),y[2]==0\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{1}{2} \Big(\sqrt{4x^2 - 15} - 1 \Big)$$

2.16 problem 16

Internal problem ID [494]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 16.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{x(x^2 + 1)}{4y^3} = 0$$

With initial conditions

$$\left[y(0) = -\frac{\sqrt{2}}{2}\right]$$

Solution by Maple

Time used: 0.094 (sec). Leaf size: 15

 $dsolve([diff(y(x),x) = \frac{1}{4}xx*(x^2+1)/y(x)^3,y(0) = -\frac{1}{2}x^2(\frac{1}{2})],y(x), singsol=all)$

$$y(x) = -\frac{\sqrt{2x^2 + 2}}{2}$$

✓ Solution by Mathematica

Time used: 0.212 (sec). Leaf size: 23

 $DSolve[\{y'[x] == \frac{1}{4}x*(x^2+1)/y[x]^3, y[0] == -(\frac{1}{Sqrt}[2])\}, y[x], x, IncludeSingularSolutions \rightarrow$

$$y(x) \to -\frac{\sqrt[4]{(x^2+1)^2}}{\sqrt{2}}$$

2.17 problem 17

Internal problem ID [495]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 17.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{-e^x + 3x^2}{-5 + 2y} = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.266 (sec). Leaf size: 21 $\,$

 $dsolve([diff(y(x),x) = (-exp(x)+3*x^2)/(-5+2*y(x)),y(0) = 1],y(x), singsol=all)$

$$y(x) = \frac{5}{2} - \frac{\sqrt{13 + 4x^3 - 4e^x}}{2}$$

✓ Solution by Mathematica

Time used: 0.856 (sec). Leaf size: 29

 $DSolve[\{y'[x] == (-Exp[x]+3*x^2)/(-5+2*y[x]),y[0]==1\},y[x],x,IncludeSingularSolutions \rightarrow True$

$$y(x) \to \frac{1}{2} \Big(5 - \sqrt{4x^3 - 4e^x + 13} \Big)$$

2.18 problem 18

Internal problem ID [496]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 18.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{-e^x + e^{-x}}{3 + 4y} = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.391 (sec). Leaf size: 29

dsolve([diff(y(x),x) = (exp(-x)-exp(x))/(3+4*y(x)),y(0) = 1],y(x), singsol=all)

$$y(x) = -\frac{3}{4} + \frac{\sqrt{e^x (-8 e^{2x} + 65 e^x - 8)} e^{-x}}{4}$$

✓ Solution by Mathematica

Time used: 1.317 (sec). Leaf size: 21

 $DSolve[\{y'[x] == (Exp[-x]-Exp[x])/(3+4*y[x]),y[0]==1\},y[x],x,IncludeSingularSolutions \rightarrow True$

$$y(x) \rightarrow \frac{1}{4} \left(\sqrt{65 - 16 \cosh(x)} - 3 \right)$$

2.19 problem 19

Internal problem ID [497]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 19.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [_separable]

$$\sin(2x) + \cos(3y)y' = 0$$

With initial conditions

$$\left[y\Big(\frac{\pi}{2}\Big)=0\right]$$

✓ Solution by Maple

Time used: 0.125 (sec). Leaf size: 15

dsolve([sin(2*x)+cos(3*y(x))*diff(y(x),x) = 0,y(1/2*Pi) = 0],y(x), singsol=all)

$$y(x) = \frac{\arcsin\left(\frac{3}{2} + \frac{3\cos(2x)}{2}\right)}{3}$$

✓ Solution by Mathematica

Time used: 0.546 (sec). Leaf size: 16

DSolve[{Sin[2*x]+Cos[3*y[x]]*y'[x] == 0,y[Pi/2]==0},y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to \frac{1}{3}\arcsin\left(3\cos^2(x)\right)$$

2.20 problem 20

Internal problem ID [498]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 20.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [_separable]

$$\sqrt{-x^2 + 1} y^2 y' - \arcsin(x) = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.157 (sec). Leaf size: 16

 $dsolve([(-x^2+1)^(1/2)*y(x)^2*diff(y(x),x) = arcsin(x),y(0) = 1],y(x), singsol=all)$

$$y(x) = \frac{\left(8 + 12\arcsin(x)^2\right)^{\frac{1}{3}}}{2}$$

✓ Solution by Mathematica

Time used: 0.485 (sec). Leaf size: 19

 $DSolve[{(-x^2+1)^(1/2)*y[x]^2*y'[x]} == ArcSin[x],y[0]==1},y[x],x,IncludeSingularSolutions \rightarrow$

$$y(x) o \sqrt[3]{\frac{3\arcsin(x)^2}{2} + 1}$$

2.21 problem 21

Internal problem ID [499]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 21.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{3x^2 + 1}{-6y + 3y^2} = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.172 (sec). Leaf size: 109

$$y(x) = \frac{\left(1+i\sqrt{3}\right)\left(4x^3+4x+4\sqrt{x^6+2x^4+x^2-4}\right)^{\frac{2}{3}}-4i\sqrt{3}-4\left(4x^3+4x+4\sqrt{x^6+2x^4+x^2-4}\right)^{\frac{1}{3}}+4x^2+4\sqrt{x^6+2x^4+x^2-4}}{4\left(4x^3+4x+4\sqrt{x^6+2x^4+x^2-4}\right)^{\frac{1}{3}}}$$

✓ Solution by Mathematica

Time used: 3.868 (sec). Leaf size: 110

 $DSolve[\{y'[x] == (3*x^2+1)/(-6*y[x]+3*y[x]^2),y[0]==1\},y[x],x,IncludeSingularSolutions \rightarrow True (3*x^2+1)/(-6*y[x]+3*y[x]^2),y[0]==1\}$

$$y(x) \to \frac{1}{4} \left(-i2^{2/3} \sqrt{3} \sqrt[3]{x^3 + \sqrt{(x^3 + x)^2 - 4} + x} - 2^{2/3} \sqrt[3]{x^3 + \sqrt{(x^3 + x)^2 - 4} + x} + 4 \right)$$
$$+ \frac{4(-1)^{2/3} \sqrt[3]{2}}{\sqrt[3]{x^3 + \sqrt{(x^3 + x)^2 - 4} + x}} + 4 \right)$$

2.22 problem 22

Internal problem ID [500]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 22.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [separable]

$$y' - \frac{3x^2}{-4 + 3y^2} = 0$$

With initial conditions

$$[y(1) = 0]$$

✓ Solution by Maple

Time used: 0.469 (sec). Leaf size: 73

 $dsolve([diff(y(x),x) = 3*x^2/(-4+3*y(x)^2),y(1) = 0],y(x), singsol=all)$

$$y(x) = -\frac{\left(1 + i\sqrt{3}\right)\left(-108 + 108x^3 + 12\sqrt{81x^6 - 162x^3 - 687}\right)^{\frac{2}{3}} - 48i\sqrt{3} + 48i\sqrt{3}}{12\left(-108 + 108x^3 + 12\sqrt{81x^6 - 162x^3 - 687}\right)^{\frac{1}{3}}}$$

✓ Solution by Mathematica

Time used: 9.573 (sec). Leaf size: 137

 $DSolve[\{y'[x]==3*x^2/(-4+3*y[x]^2),y[1]==0\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$\rightarrow \frac{-i\sqrt[3]{2}3^{2/3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - \sqrt[3]{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 8\sqrt{3} - 3\sqrt{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 8\sqrt{3} - 3\sqrt{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 8\sqrt{3} - 3\sqrt{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 8\sqrt{3} - 3\sqrt{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 8\sqrt{3} - 3\sqrt{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 8\sqrt{3} - 3\sqrt{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 8\sqrt{3} - 3\sqrt{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 8\sqrt{3} - 3\sqrt{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 8\sqrt{3} - 3\sqrt{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 8\sqrt{3} - 3\sqrt{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 8\sqrt{3} - 3\sqrt{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 8\sqrt{3} - 3\sqrt{2}\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(9x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 687 - 9\right)^{2/3} - 3\sqrt[6]{3} \left(x^3 + \sqrt{81}x^3 \left(x^3 - 2\right) - 3\sqrt[6]{3} \left(x^3 +$$

2.23 problem 23

Internal problem ID [501]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 23.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - 2y^2 - xy^2 = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.11 (sec). Leaf size: 16

 $dsolve([diff(y(x),x) = 2*y(x)^2+x*y(x)^2,y(0) = 1],y(x), singsol=all)$

$$y(x) = -\frac{2}{x^2 + 4x - 2}$$

✓ Solution by Mathematica

Time used: 0.138 (sec). Leaf size: 16

 $DSolve[\{y'[x] == 2*y[x]^2+x*y[x]^2,y[0]==1\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to -\frac{2}{x(x+4)-2}$$

2.24 problem 24

Internal problem ID [502]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 24.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{-e^x + 2}{3 + 2y} = 0$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 0.25 (sec). Leaf size: 19

dsolve([diff(y(x),x) = (2-exp(x))/(3+2*y(x)),y(0) = 0],y(x), singsol=all)

$$y(x) = -\frac{3}{2} + \frac{\sqrt{13 - 4e^x + 8x}}{2}$$

✓ Solution by Mathematica

Time used: 0.711 (sec). Leaf size: 25

 $DSolve[\{y'[x] == (2-Exp[x])/(3+2*y[x]),y[0]==0\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{1}{2} (\sqrt{8x - 4e^x + 13} - 3)$$

2.25 problem 25

Internal problem ID [503]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 25.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{2\cos(2x)}{3+2y} = 0$$

With initial conditions

$$[y(0) = -1]$$

✓ Solution by Maple

Time used: 0.39 (sec). Leaf size: 18

dsolve([diff(y(x),x) = 2*cos(2*x)/(3+2*y(x)),y(0) = -1],y(x), singsol=all)

$$y(x) = -\frac{3}{2} + \frac{\sqrt{1 + 4\sin(2x)}}{2}$$

✓ Solution by Mathematica

Time used: 0.166 (sec). Leaf size: 23

 $DSolve[\{y'[x] == 2*Cos[2*x]/(3+2*y[x]),y[0]==-1\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{1}{2} \left(\sqrt{4\sin(2x) + 1} - 3 \right)$$

2.26 problem 26

Internal problem ID [504]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 26.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - 2(x+1)(1+y^2) = 0$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 12

 $dsolve([diff(y(x),x) = 2*(1+x)*(1+y(x)^2),y(0) = 0],y(x), singsol=all)$

$$y(x) = \tan\left(x^2 + 2x\right)$$

✓ Solution by Mathematica

Time used: 0.203 (sec). Leaf size: 11

 $DSolve[\{y'[x] == 2*(1+x)*(1+y[x]^2),y[0]==0\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \tan(x(x+2))$$

2.27 problem 27

Internal problem ID [505]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 27.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{t(4-y)y}{3} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 19

dsolve(diff(y(t),t) = 1/3*t*(4-y(t))*y(t),y(t), singsol=all)

$$y(t) = \frac{4}{1 + 4e^{-\frac{2t^2}{3}}c_1}$$

✓ Solution by Mathematica

Time used: 0.248 (sec). Leaf size: 35

DSolve[y'[t] == 1/3*t*(4-y[t])*y[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) o rac{4}{1 + e^{-rac{2t^2}{3} + 4c_1}}$$

$$y(t) \to 0$$

$$y(t) \rightarrow 4$$

2.28 problem 28

Internal problem ID [506]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 28.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{ty(4-y)}{t+1} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 55

dsolve(diff(y(t),t) = t*y(t)*(4-y(t))/(1+t),y(t), singsol=all)

$$y(t) = \frac{4}{1 + 4 e^{-4t} c_1 t^4 + 16 e^{-4t} c_1 t^3 + 24 e^{-4t} c_1 t^2 + 16 e^{-4t} c_1 t + 4 e^{-4t} c_1}$$

✓ Solution by Mathematica

Time used: 2.999 (sec). Leaf size: 37

DSolve[y'[t] == t*y[t]*(4-y[t])/(1+t),y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{4}{1 + (t+1)^4 e^{-4t + 4c_1}}$$

$$y(t) \to 0$$

$$y(t) \rightarrow 4$$

2.29 problem 29

Internal problem ID [507]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 29.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - \frac{b + ay}{d + cy} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 203

dsolve(diff(y(x),x) = (b+a*y(x))/(d+c*y(x)),y(x), singsol=all)

y(x) $= \frac{c_1 a^2 + x a^2 - \left(-\text{LambertW}\left(-\frac{c_1 \frac{c_1 a^2}{ad - bc} + \frac{x a^2}{ad - bc} + \frac{bc}{ad - bc}}{-ad + bc}\right) + \frac{c_1 a^2 + x a^2 + bc}{ad - bc}\right) ad + \left(-\text{LambertW}\left(-\frac{c_1 \frac{c_1 a^2}{ad - bc} + \frac{x}{ad - bc}}{-ad - bc}\right)}{ac}$

✓ Solution by Mathematica

Time used: 15.036 (sec). Leaf size: 83

 $DSolve[y'[x] == (b+a*y[x])/(d+c*y[x]), y[x], x, IncludeSingularSolutions \rightarrow True]$

$$-bc + (ad - bc)W\left(-\frac{c\left(e^{-1 - \frac{a^2(x+c_1)}{bc}}\right)\frac{bc}{bc-ad}}{bc-ad}\right)$$

$$y(x) \to -\frac{b}{ac}$$

$$y(x) \to -\frac{b}{a}$$

2.30 problem 31

Internal problem ID [508]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 31.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, _Riccati]

$$y' - \frac{x^2 + yx + y^2}{x^2} = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 11

 $dsolve(diff(y(x),x) = (x^2+x*y(x)+y(x)^2)/x^2,y(x), singsol=all)$

$$y(x) = \tan\left(\ln\left(x\right) + c_1\right)x$$

✓ Solution by Mathematica

Time used: 0.197 (sec). Leaf size: 13

 $DSolve[y'[x] == (x^2+x*y[x]+y[x]^2)/x^2,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to x \tan(\log(x) + c_1)$$

2.31 problem 32

Internal problem ID [509]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 32.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, _Bernoulli]

$$y' - \frac{x^2 + 3y^2}{2xy} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 26

 $dsolve(diff(y(x),x) = (x^2+3*y(x)^2)/(2*x*y(x)),y(x), singsol=all)$

$$y(x) = \sqrt{c_1 x - 1} x$$

$$y(x) = \sqrt{a_1 x - 1} x$$

$$y(x) = -\sqrt{c_1 x - 1} x$$

Solution by Mathematica

Time used: 0.253 (sec). Leaf size: 34

 $DSolve[y'[x] == (x^2+3*y[x]^2)/(2*x*y[x]), y[x], x, IncludeSingularSolutions \rightarrow True]$

$$y(x) \to -x\sqrt{-1+c_1x}$$

$$y(x) \to x\sqrt{-1+c_1x}$$

2.32 problem 33

Internal problem ID [510]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

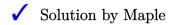
DiPrima

Section: Section 2.2. Page 48 Problem number: 33.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, [_Abel, '2nd type', 'class A']

$$y' - \frac{4y - 3x}{2x - y} = 0$$



Time used: 0.235 (sec). Leaf size: 28

dsolve(diff(y(x),x) = (4*y(x)-3*x)/(2*x-y(x)),y(x), singsol=all)

$$y(x) = \text{RootOf} \left(Z^{20}c_1x^4 - Z^4 + 4 \right)^4 x - 3x$$

✓ Solution by Mathematica

Time used: 3.175 (sec). Leaf size: 336

 $DSolve[y'[x] == (4*y[x]-3*x)/(2*x-y[x]), y[x], x, IncludeSingularSolutions \rightarrow True]$

$$\begin{split} y(x) &\to \operatorname{Root} \left[\# 1^5 + 15 \# 1^4 x + 90 \# 1^3 x^2 + 270 \# 1^2 x^3 + \# 1 \left(405 x^4 - e^{4c_1} \right) + 243 x^5 + e^{4c_1} x \&, 1 \right] \\ y(x) &\to \operatorname{Root} \left[\# 1^5 + 15 \# 1^4 x + 90 \# 1^3 x^2 + 270 \# 1^2 x^3 + \# 1 \left(405 x^4 - e^{4c_1} \right) + 243 x^5 + e^{4c_1} x \&, 2 \right] \\ y(x) &\to \operatorname{Root} \left[\# 1^5 + 15 \# 1^4 x + 90 \# 1^3 x^2 + 270 \# 1^2 x^3 + \# 1 \left(405 x^4 - e^{4c_1} \right) + 243 x^5 + e^{4c_1} x \&, 3 \right] \\ y(x) &\to \operatorname{Root} \left[\# 1^5 + 15 \# 1^4 x + 90 \# 1^3 x^2 + 270 \# 1^2 x^3 + \# 1 \left(405 x^4 - e^{4c_1} \right) + 243 x^5 + e^{4c_1} x \&, 4 \right] \\ y(x) &\to \operatorname{Root} \left[\# 1^5 + 15 \# 1^4 x + 90 \# 1^3 x^2 + 270 \# 1^2 x^3 + \# 1 \left(405 x^4 - e^{4c_1} \right) + 243 x^5 + e^{4c_1} x \&, 5 \right] \end{split}$$

2.33 problem 34

Internal problem ID [511]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 34.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, [_Abel, '2nd type', 'class A']

$$y' + \frac{4x + 3y}{2x + y} = 0$$

✓ Solution by Maple

Time used: 0.203 (sec). Leaf size: 1282

dsolve(diff(y(x),x) = - (4*x+3*y(x))/(2*x+y(x)),y(x), singsol=all)

$$y(x) = \frac{\left(4\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}} - \frac{16x^3c_1}{\left(4c_1x^3 + 4\sqrt{4c_1^2x^9 + c_1^2x^6}\right)^{\frac{1}{3}}}\right)^2 - x^3}{x^2}$$

$$y(x) = \frac{\left(-\frac{1}{2} - \frac{i\sqrt{3}}{2}\right)^6 \left(4\left(4c_1x^3 + 4\sqrt{4c_1^2x^9 + c_1^2x^6}\right)^{\frac{1}{3}} - \frac{16x^3c_1}{\left(4c_1x^3 + 4\sqrt{4c_1^2x^9 + c_1^2x^6}\right)^{\frac{1}{3}}}\right)^2 - x^3}{x^2}$$

$$y(x) = \frac{\left(-\frac{1}{2} + \frac{i\sqrt{3}}{2}\right)^6 \left(4\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}} - \frac{16x^3c_1}{\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}}}\right)^2 - x^3}{y(x)}$$

$$y(x) = \frac{\left(-2\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}} + \frac{8x^3c_1}{\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}} + \frac{2x^3c_1}{\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}}}\right)^2 - x^3}$$

$$y(x) = \frac{\left(-2\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}} + \frac{8x^3c_1}{\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}} + \frac{2x^3c_1}{\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}}}\right)^2} - x^3}$$

$$y(x) = \frac{\left(-2\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}} + \frac{8x^3c_1}{\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}} + \frac{2x^3c_1}{\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}}}\right)^2} - x^3}$$

$$y(x) = \frac{\left(-2\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}} + \frac{8x^3c_1}{\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}} + \frac{2x^3c_1}{\left(4c_1x^3 + 4\sqrt{4c_1^3x^9 + c_1^2x^6}\right)^{\frac{1}{3}}}\right)^2} - x^3$$

$$=\frac{\left(-\frac{1}{2}-\frac{i\sqrt{3}}{2}\right)^{6}\left(-2\left(4c_{1}x^{3}+4\sqrt{4c_{1}^{3}x^{9}+c_{1}^{2}x^{6}}\right)^{\frac{1}{3}}+\frac{8x^{3}c_{1}}{\left(4c_{1}x^{3}+4\sqrt{4c_{1}^{3}x^{9}+c_{1}^{2}x^{6}}\right)^{\frac{1}{3}}}-4i\sqrt{3}\left(\frac{\left(4c_{1}x^{3}+4\sqrt{4c_{1}^{3}x^{9}+c_{1}^{2}x^{6}}\right)^{\frac{1}{3}}}{2}+\frac{2x^{3}c_{1}}{\left(4c_{1}x^{3}+4\sqrt{4c_{1}^{3}x^{9}+c_{1}^{2}x^{6}}\right)^{\frac{1}{3}}}\right)\right)}{64c_{1}}}{x^{2}}$$

$$y(x) = \frac{\left(-\frac{1}{2} - \frac{i\sqrt{3}}{2}\right)^{6} \left(-2\left(4c_{1}x^{3} + 4\sqrt{4c_{1}^{3}x^{9} + c_{1}^{2}x^{6}}\right)^{\frac{1}{3}} + \frac{8x^{3}c_{1}}{\left(4c_{1}x^{3} + 4\sqrt{4c_{1}^{3}x^{9} + c_{1}^{2}x^{6}}\right)^{\frac{1}{3}}} + 4i\sqrt{3}\left(\frac{\left(4c_{1}x^{3} + 4\sqrt{4c_{1}^{3}x^{9} + c_{1}^{2}x^{6}}\right)^{\frac{1}{3}}}{2} + \frac{2x^{3}c_{1}}{\left(4c_{1}x^{3} + 4\sqrt{4c_{1}^{3}x^{9} + c_{1}^{2}x^{6}}\right)^{\frac{1}{3}}}\right)\right)}{x^{2}} = \frac{64c_{1}}{x^{2}}$$

$$y(x) = \frac{\left(-\frac{1}{2} + \frac{i\sqrt{3}}{2}\right)^{6} \left(-2\left(4c_{1}x^{3} + 4\sqrt{4c_{1}^{3}x^{9} + c_{1}^{2}x^{6}}\right)^{\frac{1}{3}} + \frac{8x^{3}c_{1}}{\left(4c_{1}x^{3} + 4\sqrt{4c_{1}^{3}x^{9} + c_{1}^{2}x^{6}}\right)^{\frac{1}{3}}} - 4i\sqrt{3}\left(\frac{\left(4c_{1}x^{3} + 4\sqrt{4c_{1}^{3}x^{9} + c_{1}^{2}x^{6}}\right)^{\frac{1}{3}}}{2} + \frac{2x^{3}c_{1}}{\left(4c_{1}x^{3} + 4\sqrt{4c_{1}^{3}x^{9} + c_{1}^{2}x^{6}}\right)^{\frac{1}{3}}}\right)\right)}{64c_{1}}$$

✓ Solution by Mathematica

Time used: 22.33 (sec). Leaf size: 484

DSolve[y'[x] == - (4*x+3*y[x])/(2*x+y[x]), y[x], x, IncludeSingularSolutions -> True]

$$\begin{split} y(x) &\to \frac{\sqrt[3]{2x^3 + \sqrt{4e^{3c_1}x^3 + e^{6c_1}} + e^{3c_1}}}{\sqrt[3]{2}} + \frac{\sqrt[3]{2}x^2}{\sqrt[3]{2x^3 + \sqrt{4e^{3c_1}x^3 + e^{6c_1}} + e^{3c_1}}} - 3x \\ y(x) &\to \frac{i(\sqrt{3}+i)\sqrt[3]{2x^3 + \sqrt{4e^{3c_1}x^3 + e^{6c_1}} + e^{3c_1}}}{2\sqrt[3]{2}} - \frac{(1+i\sqrt{3})x^2}{2^{2/3}\sqrt[3]{2x^3 + \sqrt{4e^{3c_1}x^3 + e^{6c_1}} + e^{3c_1}}}} - 3x \\ y(x) &\to -\frac{(1+i\sqrt{3})\sqrt[3]{2x^3 + \sqrt{4e^{3c_1}x^3 + e^{6c_1}} + e^{3c_1}}}{2\sqrt[3]{2}} \\ &\quad + \frac{i(\sqrt{3}+i)x^2}{2^{2/3}\sqrt[3]{2x^3 + \sqrt{4e^{3c_1}x^3 + e^{6c_1}} + e^{3c_1}}}} - 3x \\ y(x) &\to \sqrt[3]{x^3 + \frac{(x^3)^{2/3}}{x^3 + \sqrt{4e^{3c_1}x^3 + e^{6c_1}} + e^{3c_1}}}} - 3x \\ y(x) &\to \sqrt[3]{x^3 + \frac{(x^3)^{2/3}}{x^3 + \sqrt{4e^{3c_1}x^3 + e^{6c_1}} + e^{3c_1}}} - 6x \\ \end{pmatrix} \\ y(x) &\to \frac{1}{2} \left(i\left(\sqrt[3]{x} + i\right)\sqrt[3]{x^3} + \frac{i(\sqrt[3]{x} + i)(x^3)^{2/3}}{x} - 6x \right) \\ \end{split}$$

2.34 problem 35

Internal problem ID [512]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 35.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, [_Abel, '2nd type', 'class A'],

$$y' - \frac{x+3y}{x-y} = 0$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 21

dsolve(diff(y(x),x) = (x+3*y(x))/(x-y(x)),y(x), singsol=all)

$$y(x) = -\frac{x(\text{LambertW}(-2c_1x) + 2)}{\text{LambertW}(-2c_1x)}$$

✓ Solution by Mathematica

Time used: 0.12 (sec). Leaf size: 33

 $DSolve[y'[x] == (x+3*y[x])/(x-y[x]),y[x],x,IncludeSingularSolutions \rightarrow True]$

Solve
$$\left[\frac{2}{\frac{y(x)}{x}+1} + \log\left(\frac{y(x)}{x}+1\right) = -\log(x) + c_1, y(x)\right]$$

2.35 problem 36

Internal problem ID [513]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48

Problem number: 36.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, _Riccati]

$$x^2 + 3yx + y^2 - y'x^2 = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 18

 $dsolve((x^2+3*x*y(x)+y(x)^2)-x^2* diff(y(x),x)=0,y(x), singsol=all)$

$$y(x) = -\frac{x(\ln(x) + c_1 + 1)}{\ln(x) + c_1}$$

✓ Solution by Mathematica

Time used: 0.162 (sec). Leaf size: 25

 $DSolve[(x^2+3*x*y[x]+y[x]^2)-x^2* y'[x]==0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to x \left(-1 - \frac{1}{\log(x) + c_1}\right)$$

 $y(x) \to -x$

2.36 problem 37

Internal problem ID [514]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.2. Page 48 Problem number: 37.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, _Bernoulli]

$$y' - \frac{x^2 - 3y^2}{2yx} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 45

 $dsolve(diff(y(x),x) = (x^2-3*y(x)^2)/(2*x*y(x)),y(x), singsol=all)$

$$y(x) = -\frac{\sqrt{5}\sqrt{x(x^5 + 5c_1)}}{5x^2}$$
$$y(x) = \frac{\sqrt{5}\sqrt{x(x^5 + 5c_1)}}{5x^2}$$

✓ Solution by Mathematica

Time used: 0.209 (sec). Leaf size: 50

 $DSolve[y'[x] == (x^2-3*y[x]^2)/(2*x*y[x]), y[x], x, IncludeSingularSolutions \rightarrow True]$

$$y(x) o -rac{\sqrt{rac{x^5}{5}+c_1}}{x^{3/2}}$$

$$y(x)
ightarrow rac{\sqrt{rac{x^5}{5}+c_1}}{x^{3/2}}$$

2.37 problem 38

Internal problem ID [515]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

 ${\bf Section:} \ {\bf Section} \ 2.2. \ {\bf Page} \ 48$

Problem number: 38.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, _Bernoulli]

$$y' - \frac{3y^2 - x^2}{2yx} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 26

 $dsolve(diff(y(x),x) = (3*y(x)^2-x^2)/(2*x*y(x)),y(x), singsol=all)$

$$y(x) = \sqrt{c_1 x + 1} x$$

$$y(x) = -\sqrt{c_1 x + 1} x$$

✓ Solution by Mathematica

Time used: 0.208 (sec). Leaf size: 34

 $DSolve[y'[x] == (3*y[x]^2-x^2)/(2*x*y[x]),y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to -x\sqrt{1+c_1x}$$

$$y(x) \to x\sqrt{1+c_1x}$$

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3.1 problem 1

Internal problem ID [516]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76

Problem number: 1.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [linear]

$$\ln(t) y + (t - 3) y' - 2t = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 56

dsolve(ln(t)*y(t)+(-3+t)*diff(y(t),t) = 2*t,y(t), singsol=all)

$$y(t) = 3^{-\ln(-t+3)} \left(\int -2t(-t+3)^{-1+\ln(3)} e^{-\ln(3)^2} e^{-\operatorname{dilog}\left(\frac{t}{3}\right)} dt + c_1 \right) e^{\ln(3)^2} e^{\operatorname{dilog}\left(\frac{t}{3}\right)}$$

✓ Solution by Mathematica

Time used: 0.186 (sec). Leaf size: 69

 $DSolve[Log[t]*y[t]+(-3+t)*y'[t] == 2*t,y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \to e^{\text{PolyLog}(2,1-\frac{t}{3})-\log(3)\log(t-3)} \left(\int_{1}^{t} \frac{2e^{\log(3)\log(K[1]-3)-\text{PolyLog}\left(2,1-\frac{K[1]}{3}\right)}K[1]}{K[1]-3} dK[1] + c_{1} \right)$$

3.2 problem 2

Internal problem ID [517]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76

Problem number: 2.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y + (t-4)ty' = 0$$

With initial conditions

$$[y(2) = 1]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 19

dsolve([y(t)+(-4+t)*t*diff(y(t),t) = 0,y(2) = 1],y(t), singsol=all)

$$y(t) = rac{\left(rac{1}{2} + rac{i}{2}\right)\sqrt{2} t^{rac{1}{4}}}{\left(-4 + t\right)^{rac{1}{4}}}$$

✓ Solution by Mathematica

Time used: 0.033 (sec). Leaf size: 20

 $DSolve[\{y[t]+(-4+t)*t*y'[t] == 0,y[2]==1\},y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) o rac{\sqrt[4]{t}}{\sqrt[4]{4-t}}$$

3.3 problem 3

Internal problem ID [518]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76

Problem number: 3.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$\tan(t) y + y' - \sin(t) = 0$$

With initial conditions

$$[y(\pi) = 0]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 17

$$dsolve([tan(t)*y(t)+diff(y(t),t) = sin(t),y(Pi) = 0],y(t), singsol=all)$$

$$y(t) = (-\ln(\cos(t)) + i\pi)\cos(t)$$

✓ Solution by Mathematica

Time used: 0.072 (sec). Leaf size: 20

$$y(t) \to i \cos(t) (\pi + i \log(\cos(t)))$$

3.4 problem 4

Internal problem ID [519]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76

Problem number: 4.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [linear]

$$2yt + (-t^2 + 4)y' - 3t^2 = 0$$

With initial conditions

$$[y(-3) = 1]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 42

 $dsolve([2*t*y(t)+(-t^2+4)*diff(y(t),t) = 3*t^2,y(-3) = 1],y(t), singsol=all)$

$$y(t) = \frac{3t}{2} + \frac{3\ln(2+t)t^2}{8} - \frac{3\ln(2+t)}{2} - \frac{3\ln(t-2)t^2}{8} + \frac{3\ln(t-2)}{2} + \frac{11t^2}{10} - \frac{22}{5} + \frac{3\ln(5)t^2}{8} - \frac{3\ln(5)}{2}$$

✓ Solution by Mathematica

Time used: 0.052 (sec). Leaf size: 55

 $DSolve[\{2*t*y[t]+(-t^2+4)*y'[t] == 3*t^2,y[-3]==1\},y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \rightarrow \frac{1}{40} \left(44t^2 - 15i\pi \left(t^2 - 4 \right) - 15\left(t^2 - 4 \right) \log(2 - t) + 15\left(t^2 - 4 \right) \log(5(t + 2)) + 60t - 176 \right)$$

3.5 problem 5

Internal problem ID [520]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76

Problem number: 5.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$2yt + (-t^2 + 4)y' - 3t^2 = 0$$

With initial conditions

$$[y(1) = -3]$$

✓ Solution by Maple

Time used: 0.063 (sec). Leaf size: 46

 $dsolve([2*t*y(t)+(-t^2+4)*diff(y(t),t) = 3*t^2,y(1) = -3],y(t), singsol=all)$

$$y(t) = -6 + \frac{3(t^2 - 4)\ln(2 + t)}{8} + \frac{3i\pi t^2}{8} - \frac{3\ln(3)t^2}{8} - \frac{3\ln(t - 2)t^2}{8} - \frac{3\ln(t - 2)}{8} + \frac{3i\pi}{2} + \frac{3t}{2} + \frac{3\ln(3)}{2} + \frac{3\ln(t - 2)}{2}$$

✓ Solution by Mathematica

Time used: 0.044 (sec). Leaf size: 41

 $DSolve[\{2*t*y[t]+(-t^2+4)*y'[t] == 3*t^2,y[1]==-3\},y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \to \frac{3}{8} (4(t^2 + t - 4) - (t^2 - 4) \log(6 - 3t) + (t^2 - 4) \log(t + 2))$$

3.6 problem 6

Internal problem ID [521]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76

Problem number: 6.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [linear]

$$y + \ln(t) y' - \cot(t) = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 32

dsolve(y(t)+ln(t)*diff(y(t),t) = cot(t),y(t), singsol=all)

$$y(t) = \left(\int \frac{\cot(t) e^{-Ei_1(-\ln(t))}}{\ln(t)} dt + c_1\right) e^{Ei_1(-\ln(t))}$$

Solution by Mathematica

Time used: 0.141 (sec). Leaf size: 36

DSolve[y[t]+Log[t]*y'[t] == Cot[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to e^{-\operatorname{LogIntegral}(t)} \left(\int_1^t \frac{e^{\operatorname{LogIntegral}(K[1])} \cot(K[1])}{\log(K[1])} dK[1] + c_1 \right)$$

3.7 problem 11

Internal problem ID [522]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76 Problem number: 11.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{t^2 + 1}{3y - y^2} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 660

 $dsolve(diff(y(t),t) = (t^2+1)/(3*y(t)-y(t)^2),y(t), singsol=all)$

$$y(t) = \frac{\left(27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}\right)^{\frac{1}{3}}}{2} + \frac{2}{2} + \frac{2}{2} \left(27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}}\right)^{\frac{1}{3}}}{2} + \frac{3}{2}$$

$$y(t) = -\frac{\left(27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}}\right)^{\frac{1}{3}}}{4} - \frac{4}{2}$$

$$-\frac{4}{2} \left(27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}}\right)^{\frac{1}{3}}}{2} - \frac{1}{2} \left(\frac{27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}}{2}\right)^{\frac{1}{3}}}{2} - \frac{1}{2} \left(\frac{27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}}{2}\right)^{\frac{1}{3}}}{4} - \frac{1}{2} \left(\frac{27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}}{2}\right)^{\frac{1}{3}}}{4} + \frac{3}{2}$$

$$\frac{1}{4} \left(27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}}\right)^{\frac{1}{3}}}{4} + \frac{3}{2}$$

$$\frac{1}{4} \left(27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}}{2}\right)^{\frac{1}{3}}}{4} + \frac{3}{2}$$

$$\frac{1}{4} \left(27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}}{2}\right)^{\frac{1}{3}}}{4} + \frac{3}{2}$$

$$\frac{1}{4} \left(27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}}{2}\right)^{\frac{1}{3}}}{4} + \frac{3}{2}$$

$$\frac{1}{4} \left(27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}}\right)^{\frac{1}{3}}}{2} + \frac{3}{2}$$

$$\frac{1}{4} \left(27 - 4t^3 - 12c_1 - 12t + 2\sqrt{4t^6 + 24c_1t^3 + 24t^4 - 54t^3 + 36c_1^2 + 72c_1t + 36t^2 - 162c_1 - 162t}}\right)^{\frac{1}{3}}$$

✓ Solution by Mathematica

Time used: 3.08 (sec). Leaf size: 342

 $DSolve[y'[t] == (t^2+1)/(3*y[t]-y[t]^2), y[t], t, IncludeSingularSolutions -> True]$

$$y(t) \to \frac{1}{2} \left(\sqrt[3]{-4t^3 + \sqrt{-729 + (4t(t^2 + 3) - 3(9 + 4c_1))^2} - 12t + 27 + 12c_1} \right)$$

$$+ \frac{9}{\sqrt[3]{-4t^3 + \sqrt{-729 + (4t(t^2 + 3) - 3(9 + 4c_1))^2} - 12t + 27 + 12c_1}} + 3 \right)$$

$$y(t) \to \frac{1}{4} \left(i \left(\sqrt{3} + i \right) \sqrt[3]{-4t^3 + \sqrt{-729 + (4t(t^2 + 3) - 3(9 + 4c_1))^2} - 12t + 27 + 12c_1} \right)$$

$$+ \frac{-9 - 9i\sqrt{3}}{\sqrt[3]{-4t^3 + \sqrt{-729 + (4t(t^2 + 3) - 3(9 + 4c_1))^2} - 12t + 27 + 12c_1}} + 6 \right)$$

$$y(t) \to \frac{1}{4} \left(-\left(\left(1 + i\sqrt{3} \right) \sqrt[3]{-4t^3 + \sqrt{-729 + (4t(t^2 + 3) - 3(9 + 4c_1))^2} - 12t + 27 + 12c_1} \right)$$

$$+ \frac{9i(\sqrt{3} + i)}{\sqrt[3]{-4t^3 + \sqrt{-729 + (4t(t^2 + 3) - 3(9 + 4c_1))^2} - 12t + 27 + 12c_1}} + 6 \right)$$

3.8 problem 12

Internal problem ID [523]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76 Problem number: 12.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{\cot(t)y}{1+y} = 0$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 9

dsolve(diff(y(t),t) = cot(t)*y(t)/(1+y(t)),y(t), singsol=all)

$$y(t) = \text{LambertW}(c_1 \sin(t))$$

✓ Solution by Mathematica

Time used: 1.599 (sec). Leaf size: 18

DSolve[y'[t] == Cot[t]*y[t]/(1+y[t]),y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to W(e^{c_1}\sin(t))$$

 $y(t) \to 0$

3.9 problem 13

Internal problem ID [524]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76 Problem number: 13.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' + \frac{4t}{y} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 27

dsolve(diff(y(t),t) = -4*t/y(t),y(t), singsol=all)

$$y(t) = \sqrt{-4t^2 + c_1}$$

 $y(t) = -\sqrt{-4t^2 + c_1}$

✓ Solution by Mathematica

Time used: 0.078 (sec). Leaf size: 46

DSolve[y'[t] == -4*t/y[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to -\sqrt{2}\sqrt{-2t^2 + c_1}$$
$$y(t) \to \sqrt{2}\sqrt{-2t^2 + c_1}$$

3.10 problem 14

Internal problem ID [525]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76 Problem number: 14.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - 2ty^2 = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 13

 $dsolve(diff(y(t),t) = 2*t*y(t)^2,y(t), singsol=all)$

$$y(t) = \frac{1}{-t^2 + c_1}$$

✓ Solution by Mathematica

Time used: 0.122 (sec). Leaf size: 20

DSolve[y'[t] == 2*t*y[t]^2,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to -\frac{1}{t^2 + c_1}$$

$$y(t) \to 0$$

3.11 problem 15

Internal problem ID [526]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76 Problem number: 15.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y^3 + y' = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 23

 $dsolve(y(t)^3+diff(y(t),t) = 0,y(t), singsol=all)$

$$y(t) = \frac{1}{\sqrt{2t + c_1}}$$

$$y(t) = -\frac{1}{\sqrt{2t + c_1}}$$

✓ Solution by Mathematica

Time used: 0.122 (sec). Leaf size: 40

 $DSolve[y[t]^3+y'[t] == 0,y[t],t,IncludeSingularSolutions -> True]$

$$y(t) \to -\frac{1}{\sqrt{2t - 2c_1}}$$

$$y(t) o rac{1}{\sqrt{2t - 2c_1}}$$

$$y(t) \to 0$$

3.12 problem 16

Internal problem ID [527]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76 Problem number: 16.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{t^2}{(t^3 + 1)y} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 39

 $dsolve(diff(y(t),t) = t^2/(t^3+1)/y(t),y(t), singsol=all)$

$$y(t) = -\frac{\sqrt{6\ln(t^3 + 1) + 9c_1}}{3}$$
$$y(t) = \frac{\sqrt{6\ln(t^3 + 1) + 9c_1}}{3}$$

✓ Solution by Mathematica

Time used: 0.093 (sec). Leaf size: 56

 $DSolve[y'[t] == t^2/(t^3+1)/y[t], y[t], t, IncludeSingularSolutions -> True]$

$$y(t) \to -\sqrt{\frac{2}{3}}\sqrt{\log(t^3+1)+3c_1}$$

$$y(t) \to \sqrt{\frac{2}{3}} \sqrt{\log(t^3 + 1) + 3c_1}$$

3.13 problem 17

Internal problem ID [528]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76 Problem number: 17.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - t(3-y)y = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 19

dsolve(diff(y(t),t) = t*(3-y(t))*y(t),y(t), singsol=all)

$$y(t) = \frac{3}{1 + 3e^{-\frac{3t^2}{2}}c_1}$$

Solution by Mathematica

Time used: 0.23 (sec). Leaf size: $35\,$

DSolve[y'[t] == t*(3-y[t])*y[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) o rac{3}{1 + e^{-rac{3t^2}{2} + 3c_1}}$$

$$y(t) \to 0$$

$$y(t) \rightarrow 3$$

3.14 problem 18

Internal problem ID [529]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76 Problem number: 18.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_Bernoulli]

$$y' - y(3 - yt) = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 20

dsolve(diff(y(t),t) = y(t)*(3-t*y(t)),y(t), singsol=all)

$$y(t) = \frac{9}{-1 + 9c_1 e^{-3t} + 3t}$$

✓ Solution by Mathematica

Time used: 0.122 (sec). Leaf size: 29

DSolve[y'[t] == y[t]*(3-t*y[t]),y[t],t,IncludeSingularSolutions -> True]

$$y(t) o rac{1}{rac{t}{3} + c_1 e^{-3t} - rac{1}{9}}$$
 $y(t) o 0$

3.15 problem 19

Internal problem ID [530]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76 Problem number: 19.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_Bernoulli]

$$y' + y(3 - yt) = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 20

dsolve(diff(y(t),t) = -y(t)*(3-t*y(t)),y(t), singsol=all)

$$y(t) = \frac{9}{1 + 9c_1 e^{3t} + 3t}$$

✓ Solution by Mathematica

Time used: 0.133 (sec). Leaf size: 28

DSolve[y'[t] == -y[t]*(3-t*y[t]),y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{9}{3t + 9c_1e^{3t} + 1}$$
$$y(t) \to 0$$

3.16 problem 20

Internal problem ID [531]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.4. Page 76 Problem number: 20.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_Riccati]

$$y' - t + 1 + y^2 = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 31

 $dsolve(diff(y(t),t) = t-1-y(t)^2,y(t), singsol=all)$

$$y(t) = \frac{\operatorname{AiryAi}(1, t - 1) c_1 + \operatorname{AiryBi}(1, t - 1)}{\operatorname{AiryAi}(t - 1) c_1 + \operatorname{AiryBi}(t - 1)}$$

✓ Solution by Mathematica

Time used: 0.113 (sec). Leaf size: 47

DSolve[y'[t] == t-1-y[t]^2,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{\text{AiryBiPrime}(t-1) + c_1 \text{AiryAiPrime}(t-1)}{\text{AiryBi}(t-1) + c_1 \text{AiryAi}(t-1)}$$
$$y(t) \to \frac{\text{AiryAiPrime}(t-1)}{\text{AiryAi}(t-1)}$$

4 Section 2.5. Page 88

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4.1 problem 1

Internal problem ID [532]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.5. Page 88

Problem number: 1.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - ay - by^2 = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 20

 $dsolve(diff(y(x),x) = a*y(x)+b*y(x)^2,y(x), singsol=all)$

$$y(x) = \frac{a}{e^{-ax}c_1a - b}$$

✓ Solution by Mathematica

Time used: 0.76 (sec). Leaf size: 38

 $DSolve[y'[x] == a*y[x]+b*y[x]^2,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to -\frac{a}{b - e^{-a(x+c_1)}}$$

$$y(x) \to 0$$

$$y(x) \to -\frac{a}{b}$$

4.2 problem 3

Internal problem ID [533]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.5. Page 88

Problem number: 3.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y(-2 + y)(-1 + y) = 0$$

/

Solution by Maple

Time used: 0.203 (sec). Leaf size: 73

dsolve(diff(y(t),t) = y(t)*(-2+y(t))*(-1+y(t)),y(t), singsol=all)

$$y(t) = -rac{\mathrm{e}^{2t}c_1}{\left(-rac{1}{\sqrt{-c_1\mathrm{e}^{2t}+1}}-1
ight)(c_1\mathrm{e}^{2t}-1)}$$

$$y(t) = -rac{\mathrm{e}^{2t}c_1}{\left(rac{1}{\sqrt{-c_1\mathrm{e}^{2t}+1}}-1
ight)(c_1\mathrm{e}^{2t}-1)}$$

/

Solution by Mathematica

Time used: 10.147 (sec). Leaf size: 58

 $DSolve[y'[t] == y[t]*(-2+y[t])*(-1+y[t]), y[t], t, IncludeSingularSolutions \rightarrow True]$

$$y(t) \to 1 - \frac{1}{\sqrt{1 + e^{2(t+c_1)}}}$$

$$y(t) \to 1 + \frac{1}{\sqrt{1 + e^{2(t+c_1)}}}$$

$$y(t) \to 0$$

$$y(t) \to 1$$

$$y(t) \rightarrow 2$$

4.3 problem 4

Internal problem ID [534]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.5. Page 88

Problem number: 4.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + 1 - e^y = 0$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 15

dsolve(diff(y(t),t) = -1+exp(y(t)),y(t), singsol=all)

$$y(t) = \ln\left(-rac{1}{c_1 \mathrm{e}^t - 1}
ight)$$

✓ Solution by Mathematica

Time used: 0.709 (sec). Leaf size: 21

DSolve[y'[t] == -1+Exp[y[t]],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \log\left(\frac{1}{1 + e^{t + c_1}}\right)$$

 $y(t) \to 0$

4.4 problem 5

Internal problem ID [535]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.5. Page 88

Problem number: 5.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + 1 - e^{-y} = 0$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 18

dsolve(diff(y(t),t) = -1+exp(-y(t)),y(t), singsol=all)

$$y(t) = -t + \ln \left(e^{t+c_1} - 1 \right) - c_1$$

✓ Solution by Mathematica

Time used: 0.825 (sec). Leaf size: 21

 $DSolve[y'[t] == -1 + Exp[-y[t]], y[t], t, IncludeSingularSolutions \rightarrow True]$

$$y(t) \to \log \left(1 + e^{-t + c_1}\right)$$

 $y(t) \to 0$

4.5 problem 6

Internal problem ID [536]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.5. Page 88

Problem number: 6.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + \frac{2\arctan(y)}{1+y^2} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 22

 $dsolve(diff(y(t),t) = -2*arctan(y(t))/(1+y(t)^2),y(t), singsol=all)$

$$t + \int^{y(t)} \frac{a^2 + 1}{2 \arctan(a)} d_a a + c_1 = 0$$

✓ Solution by Mathematica

Time used: 0.89 (sec). Leaf size: 38

DSolve[y'[t] == -2*ArcTan[y[t]]/(1+y[t]^2),y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \text{InverseFunction} \left[\int_1^{\#1} \frac{K[1]^2 + 1}{\arctan(K[1])} dK[1] \& \right] [-2t + c_1]$$

 $y(t) \to 0$

4.6 problem 7

Internal problem ID [537]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.5. Page 88

Problem number: 7.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + k(-1 + y)^2 = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 21

 $dsolve(diff(y(t),t) = -k*(-1+y(t))^2,y(t), singsol=all)$

$$y(t) = \frac{c_1k + tk + 1}{k(t + c_1)}$$

✓ Solution by Mathematica

Time used: 0.149 (sec). Leaf size: 22

DSolve[y'[t] == -k*(-1+y[t])^2,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to 1 + \frac{1}{kt - c_1}$$

 $y(t) \to 1$

4.7 problem 9

Internal problem ID [538]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.5. Page 88

Problem number: 9.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y^2(y^2 - 1) = 0$$

✓ Solution by Maple

Time used: 0.063 (sec). Leaf size: 47

 $dsolve(diff(y(t),t) = y(t)^2*(y(t)^2-1),y(t), singsol=all)$

$$y(t) = \mathrm{e}^{\mathrm{RootOf}\left(-\ln\left(\mathrm{e}^{-Z}-2\right)\mathrm{e}^{-Z}+2c_{1}\mathrm{e}^{-Z}+ _{Z}\mathrm{e}^{-Z}+2t\,\mathrm{e}^{-Z}+\ln\left(\mathrm{e}^{-Z}-2\right)-2c_{1}- _{Z}-2t-2\right)} - 1$$

✓ Solution by Mathematica

Time used: 0.226 (sec). Leaf size: 51

 $DSolve[y'[t] == y[t]^2*(y[t]^2-1),y[t],t,IncludeSingularSolutions -> True]$

$$y(t) \to \text{InverseFunction} \left[\frac{1}{\#1} + \frac{1}{2} \log(1 - \#1) - \frac{1}{2} \log(\#1 + 1) \& \right] [t + c_1]$$

$$y(t) \rightarrow -1$$

$$y(t) \to 0$$

$$y(t) \rightarrow 1$$

4.8 problem 10

Internal problem ID [539]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.5. Page 88 Problem number: 10.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y(1 - y^2) = 0$$

/

Solution by Maple

Time used: 0.015 (sec). Leaf size: 29

 $dsolve(diff(y(t),t) = y(t)*(1-y(t)^2),y(t), singsol=all)$

$$y(t) = \frac{1}{\sqrt{c_1 e^{-2t} + 1}}$$

$$y(t) = -\frac{1}{\sqrt{c_1 e^{-2t} + 1}}$$



Solution by Mathematica

Time used: 0.692 (sec). Leaf size: 100

 $DSolve[y'[t] == y[t]*(1-y[t]^2),y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t)
ightarrow -rac{e^t}{\sqrt{e^{2t}+e^{2c_1}}}$$

$$y(t)
ightarrow rac{e^t}{\sqrt{e^{2t} + e^{2c_1}}}$$

$$y(t) \rightarrow -1$$

$$y(t) \to 0$$

$$y(t) \to 1$$

$$y(t) \to -\frac{e^t}{\sqrt{e^{2t}}}$$

$$y(t) o rac{e^t}{\sqrt{e^{2t}}}$$

4.9 problem 11

Internal problem ID [540]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.5. Page 88 Problem number: 11.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + b\sqrt{y} - ay = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 22

 $dsolve(diff(y(t),t) = -b*y(t)^(1/2)+a*y(t),y(t), singsol=all)$

$$-\frac{b}{a} - e^{\frac{at}{2}}c_1 + \sqrt{y(t)} = 0$$

✓ Solution by Mathematica

Time used: 0.747 (sec). Leaf size: 55

DSolve[y'[t] == -b*y[t]^(1/2)+a*y[t],y[t],t,IncludeSingularSolutions -> True]

$$egin{align} y(t)
ightarrow rac{e^{-ac_1} \left(e^{rac{at}{2}} - be^{rac{ac_1}{2}}
ight){}^2}{a^2} \ y(t)
ightarrow 0 \ y(t)
ightarrow rac{b^2}{a^2} \ \end{array}$$

4.10 problem 12

Internal problem ID [541]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

 ${\bf Section:}\ {\bf Section}\ 2.5.\ {\bf Page}\ 88$

Problem number: 12.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y^2 (4 - y^2) = 0$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 49

 $dsolve(diff(y(t),t) = y(t)^2*(4-y(t)^2),y(t), singsol=all)$

$$y(t) = \mathrm{e}^{\mathrm{RootOf}\left(\ln\left(\mathrm{e}^{-Z} - 4\right)\mathrm{e}^{-Z} + 16c_1\mathrm{e}^{-Z} - \underline{Z}\,\mathrm{e}^{-Z} + 16t\,\mathrm{e}^{-Z} - 2\ln\left(\mathrm{e}^{-Z} - 4\right) - 32c_1 + 2\underline{Z} - 32t + 4\right)} - 2$$

✓ Solution by Mathematica

Time used: 0.236 (sec). Leaf size: 57

 $DSolve[y'[t] == y[t]^2*(4-y[t]^2),y[t],t,IncludeSingularSolutions -> True]$

$$y(t) \to \text{InverseFunction}\left[\frac{1}{4\#1} + \frac{1}{16}\log(2 - \#1) - \frac{1}{16}\log(\#1 + 2)\&\right][-t + c_1]$$

$$y(t) \rightarrow -2$$

$$y(t) \to 0$$

$$y(t) \rightarrow 2$$

4.11 problem 13

Internal problem ID [542]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.5. Page 88 Problem number: 13.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - (1 - y)^2 y^2 = 0$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 66

 $dsolve(diff(y(t),t) = (1-y(t))^2*y(t)^2,y(t), singsol=all)$

$$y(t) = \mathrm{e}^{\mathrm{RootOf}\left(-2\ln(\mathrm{e}^{-Z}+1)\mathrm{e}^{2-Z}+c_1\mathrm{e}^{2-Z}+2_-Z\mathrm{e}^{2-Z}+t\,\mathrm{e}^{2-Z}-2\ln(\mathrm{e}^{-Z}+1)\mathrm{e}^{-Z}+c_1\mathrm{e}^{-Z}+2_-Z\mathrm{e}^{-Z}+t\,\mathrm{e}^{-Z}+2_-Z\mathrm{e}^{-Z}+1\right)} + 1$$

✓ Solution by Mathematica

Time used: 0.358 (sec). Leaf size: 50

 $DSolve[y'[t] == (1-y[t])^2*y[t]^2,y[t],t,IncludeSingularSolutions -> True]$

$$y(t) \to \text{InverseFunction}\left[-\frac{1}{\#1-1} - \frac{1}{\#1} - 2\log(1-\#1) + 2\log(\#1)\&\right][t+c_1]$$

$$y(t) \to 0$$

$$y(t) \to 1$$

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5.1 problem 1

Internal problem ID [543]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 1.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$3 + 2x + (-2 + 2y)y' = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 43

dsolve(3+2*x+(-2+2*y(x))*diff(y(x),x) = 0,y(x), singsol=all)

$$y(x) = 1 - \sqrt{-x^2 - c_1 - 3x + 1}$$
$$y(x) = 1 + \sqrt{-x^2 - c_1 - 3x + 1}$$

✓ Solution by Mathematica

Time used: 0.114 (sec). Leaf size: 47

 $DSolve[3+2*x+(-2+2*y[x])*y'[x] == 0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to 1 - \sqrt{-x(x+3) + 1 + 2c_1}$$

 $y(x) \to 1 + \sqrt{-x(x+3) + 1 + 2c_1}$

5.2 problem 2

Internal problem ID [544]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 2.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, [_Abel, '2nd type', 'class A'],

$$2x + 4y + (2x - 2y)y' = 0$$

✓ Solution by Maple

Time used: 0.203 (sec). Leaf size: 56

dsolve(2*x+4*y(x)+(2*x-2*y(x))*diff(y(x),x) = 0,y(x), singsol=all)

$$-\frac{\ln\left(-\frac{x^{2}+3xy(x)-y(x)^{2}}{x^{2}}\right)}{2} - \frac{\sqrt{13} \operatorname{arctanh}\left(\frac{(-2y(x)+3x)\sqrt{13}}{13x}\right)}{13} - \ln(x) - c_{1} = 0$$

✓ Solution by Mathematica

Time used: 0.067 (sec). Leaf size: 63

 $DSolve[2*x+4*y[x]+(2*x-2*y[x])*y'[x] == 0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$\begin{aligned} &\operatorname{Solve}\left[\frac{1}{26}\left(\left(13+\sqrt{13}\right)\log\left(-\frac{2y(x)}{x}+\sqrt{13}+3\right)\right.\right.\\ &\left.-\left(\sqrt{13}-13\right)\log\left(\frac{2y(x)}{x}+\sqrt{13}-3\right)\right)=-\log(x)+c_1,y(x)\right] \end{aligned}$$

5.3 problem 3

Internal problem ID [545]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 3.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_exact, _rational]

$$2 + 3x^{2} - 2yx + (3 - x^{2} + 6y^{2})y' = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 582

 $dsolve(2+3*x^2-2*x*y(x)+(3-x^2+6*y(x)^2)*diff(y(x),x) = 0,y(x), singsol=all)$

$$y(x) = \frac{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}}{6\left(-\frac{x^2}{6} + \frac{1}{2}\right)} - \frac{6}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{12}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{12}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{-x^2 + 3}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{-x^2 + 3}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{12}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{1}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{-x^2 + 3}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{-x^2 + 3}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{-x^2 + 3}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{-x^2 + 3}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{-x^2 + 3}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{-x^2 + 3}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{-x^2 + 3}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{-x^2 + 3}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75}x^6 + 162c_1x^3 + 378x^4 + 81c_1^2 + 324c_1x + 162x^2 + 162\right)^{\frac{1}{3}}} + \frac{-x^2 + 3}{\left(-54x^3 - 54c_1 - 108x + 6\sqrt{75$$

✓ Solution by Mathematica

Time used: 9.366 (sec). Leaf size: 421

 $DSolve[2+3*x^2-2*x*y[x]+(3-x^2+6*y[x]^2)*y'[x] == 0, y[x], x, Include Singular Solutions \rightarrow True]$

$$y(x) \to -\frac{x^2 - 3}{\sqrt[3]{6}\sqrt[3]{9x^3 + \sqrt{3}\sqrt{-2(x^2 - 3)^3 + 27(x^3 + 2x + c_1)^2 + 18x + 9c_1}}}{-\frac{\sqrt[3]{9x^3 + \sqrt{3}\sqrt{-2(x^2 - 3)^3 + 27(x^3 + 2x + c_1)^2 + 18x + 9c_1}}{6^{2/3}}}$$

$$\begin{array}{l} y(x) \\ \to \frac{\sqrt[3]{6} \left(1+i \sqrt{3}\right) \left(x^2-3\right)+\left(1-i \sqrt{3}\right) \left(9 x^3+\sqrt{3} \sqrt{-2 \left(x^2-3\right)^3+27 \left(x^3+2 x+c_1\right){}^2}+18 x+9 c_1\right){}^{2/3}}{2 \; 6^{2/3} \sqrt[3]{9 x^3+\sqrt{3} \sqrt{-2 \left(x^2-3\right)^3+27 \left(x^3+2 x+c_1\right){}^2}+18 x+9 c_1}} \end{array}$$

$$\begin{array}{l} y(x) \\ \to \frac{\sqrt[3]{6} \left(1-i \sqrt{3}\right) \left(x^2-3\right)+\left(1+i \sqrt{3}\right) \left(9 x^3+\sqrt{3} \sqrt{-2 \left(x^2-3\right)^3+27 \left(x^3+2 x+c_1\right){}^2}+18 x+9 c_1\right){}^{2/3}}{2 \ 6^{2/3} \sqrt[3]{9 x^3+\sqrt{3} \sqrt{-2 \left(x^2-3\right)^3+27 \left(x^3+2 x+c_1\right){}^2}+18 x+9 c_1} \end{array}$$

5.4 problem 4

Internal problem ID [546]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 4.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$2y + 2xy^{2} + (2x + 2x^{2}y)y' = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 31

 $dsolve(2*y(x)+2*x*y(x)^2+(2*x+2*x^2*y(x))*diff(y(x),x) = 0,y(x), singsol=all)$

$$y(x) = -\frac{1}{x}$$
$$y(x) = \frac{-1 - c_1}{x}$$
$$y(x) = \frac{c_1 - 1}{x}$$

✓ Solution by Mathematica

Time used: 0.023 (sec). Leaf size: 29

 $DSolve[2*y[x]+2*x*y[x]^2+(2*x+2*x^2*y[x])*y'[x] == 0,y[x],x,IncludeSingularSolutions -> True]$

$$y(x) \to -\frac{1}{x}$$

$$y(x) \to \frac{c_1}{x}$$

$$y(x) \to -\frac{1}{x}$$

5.5 problem 5

Internal problem ID [547]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 5.

ODE order: 1. ODE degree: 1.

 ${\rm CAS\ Maple\ gives\ this\ as\ type\ [[_homogeneous,\ `class\ A'],\ _rational,\ [_Abel,\ `2nd\ type',\ `class A'],\ _rational,\ [_Abel,\ `2nd\ type',\ `class A'],\ _rational,\ [_Abel,\ `2nd\ type',\ `2nd\ type$

$$y' - \frac{-ax - yb}{bx + cy} = 0$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 83

dsolve(diff(y(x),x) = (-a*x-b*y(x))/(b*x+c*y(x)),y(x), singsol=all)

$$y(x) = -\frac{bxc_1 - \sqrt{-ac\,c_1^2x^2 + b^2c_1^2x^2 + c}}{cc_1}$$
$$y(x) = -\frac{bxc_1 + \sqrt{-ac\,c_1^2x^2 + b^2c_1^2x^2 + c}}{cc_1}$$

✓ Solution by Mathematica

Time used: 17.767 (sec). Leaf size: 135

 $DSolve[y'[x] == (-a*x-b*y[x])/(b*x+c*y[x]), y[x], x, IncludeSingularSolutions \rightarrow True]$

$$y(x) \rightarrow -\frac{bx + \sqrt{x^2 (b^2 - ac) + ce^{2c_1}}}{c}$$

$$y(x) \rightarrow \frac{-bx + \sqrt{x^2 (b^2 - ac) + ce^{2c_1}}}{c}$$

$$y(x) \rightarrow -\frac{\sqrt{x^2 (b^2 - ac)} + bx}{c}$$

$$y(x) \rightarrow \frac{\sqrt{x^2 (b^2 - ac)} - bx}{c}$$

5.6 problem 6

Internal problem ID [548]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 6.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, [_Abel, '2nd type', 'class A'],

$$y' - \frac{-ax + yb}{bx - cy} = 0$$

✓ Solution by Maple

Time used: 0.609 (sec). Leaf size: 52

dsolve(diff(y(x),x) = (-a*x+b*y(x))/(b*x-c*y(x)),y(x), singsol=all)

$$y(x) = \operatorname{RootOf}\left(c_Z^2 - a - e^{\operatorname{RootOf}\left(\tanh\left(\frac{\sqrt{ac}\left(2c_1 + _Z + 2\ln(x)\right)}{2b}\right)^2 a - a - e^{-Z}\right)}\right) x$$

✓ Solution by Mathematica

Time used: 0.073 (sec). Leaf size: 58

DSolve[y'[x] == (-a*x+b*y[x])/(b*x-c*y[x]),y[x],x,IncludeSingularSolutions -> True]

Solve
$$-\frac{b \operatorname{arctanh}\left(\frac{\sqrt{c}y(x)}{\sqrt{a}x}\right)}{\sqrt{a}\sqrt{c}} - \frac{1}{2}\log\left(\frac{cy(x)^2}{x^2} - a\right) = \log(x) + c_1, y(x)$$

5.7 problem 7

Internal problem ID [549]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 7.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_exact]

$$e^{x} \sin(y) - 2 \sin(x) y + (2 \cos(x) + e^{x} \cos(y)) y' = 0$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 17

dsolve(exp(x)*sin(y(x))-2*sin(x)*y(x)+(2*cos(x)+exp(x)*cos(y(x)))*diff(y(x),x) = 0,y(x), sing(x)

$$e^{x} \sin(y(x)) + 2\cos(x)y(x) + c_{1} = 0$$

✓ Solution by Mathematica

Time used: 0.299 (sec). Leaf size: 20

$$Solve[e^x \sin(y(x)) + 2y(x)\cos(x) = c_1, y(x)]$$

5.8 problem 8

Internal problem ID [550]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 8.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type ['x=G(y,y')']

$$e^{x} \sin(y) + 3y - (3x - e^{x} \sin(y)) y' = 0$$

X Solution by Maple

dsolve(exp(x)*sin(y(x))+3*y(x)-(3*x-exp(x)*sin(y(x)))*diff(y(x),x) = 0,y(x), singsol=all)

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

Not solved

5.9 problem 9

Internal problem ID [551]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 9.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_exact]

$$2x - 2e^{yx}\sin(2x) + e^{yx}\cos(2x)y + (-3 + e^{yx}x\cos(2x))y' = 0$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 40

$$y(x) = -\frac{-x^3 - c_1 x + 3 \operatorname{LambertW}\left(-\frac{x \cos(2x) e^{\frac{x^3}{3}} e^{\frac{c_1 x}{3}}}{3}\right)}{3x}$$

✓ Solution by Mathematica

Time used: 4.092 (sec). Leaf size: 48

DSolve[2*x-2*Exp[x*y[x]]*Sin[2*x]+Exp[x*y[x]]*Cos[2*x]*y[x]+(-3+Exp[x*y[x]]*x*Cos[2*x])*y'[x]

$$y(x) o rac{-3W\left(-\frac{1}{3}xe^{\frac{1}{3}x(x^2-c_1)}\cos(2x)\right) + x^3 - c_1x}{3x}$$

5.10 problem 10

Internal problem ID [552]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 10.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$\frac{y}{x} + 6x + (\ln(x) - 2)y' = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 18

dsolve((y(x)/x+6*x)+(ln(x)-2)*diff(y(x),x) = 0,y(x), singsol=all)

$$y(x) = \frac{-3x^2 + c_1}{\ln(x) - 2}$$

✓ Solution by Mathematica

Time used: 0.073 (sec). Leaf size: 20

DSolve[(y[x]/x+6*x)+(Log[x]-2)*y'[x] == 0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to \frac{-3x^2 + c_1}{\log(x) - 2}$$

5.11 problem 11

Internal problem ID [553]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 11.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_Abel, '2nd type', 'class B']]

$$x \ln(x) + yx + (\ln(x)y + yx)y' = 0$$

X Solution by Maple

```
dsolve((x*ln(x)+x*y(x))+(y(x)*ln(x)+x*y(x))*diff(y(x),x) = 0,y(x), singsol=all)
```

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

```
 DSolve[(x*Log[x]+x*y[x])+(y[x]*Log[x]+x*y[x])*y'[x] == 0, y[x], x, IncludeSingularSolutions \rightarrow T + x + y[x] + x + y[x]
```

Not solved

5.12 problem 12

Internal problem ID [554]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 12.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$\frac{x}{(x^2+y^2)^{\frac{3}{2}}} + \frac{yy'}{(x^2+y^2)^{\frac{3}{2}}} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 27

 $dsolve(x/(x^2+y(x)^2)^3(3/2)+y(x)*diff(y(x),x)/(x^2+y(x)^2)^3(3/2) = 0,y(x), singsol=all)$

$$y(x) = \sqrt{-x^2 + c_1}$$

$$y(x) = -\sqrt{-x^2 + c_1}$$

✓ Solution by Mathematica

Time used: 0.076 (sec). Leaf size: 39

 $DSolve[x/(x^2+y[x]^2)^(3/2)+y[x]*y'[x]/(x^2+y[x]^2)^(3/2) == 0, y[x], x, IncludeSingularSolution$

$$y(x) \to -\sqrt{-x^2 + 2c_1}$$

$$y(x) \to \sqrt{-x^2 + 2c_1}$$

5.13 problem 13

Internal problem ID [555]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 13.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _exact, _rational, [_Abel, '2nd type

$$2x - y + (-x + 2y)y' = 0$$

With initial conditions

$$[y(1) = 3]$$

✓ Solution by Maple

Time used: 0.141 (sec). Leaf size: 19

dsolve([2*x-y(x)+(-x+2*y(x))*diff(y(x),x) = 0,y(1) = 3],y(x), singsol=all)

$$y(x) = \frac{x}{2} + \frac{\sqrt{-3x^2 + 28}}{2}$$

✓ Solution by Mathematica

Time used: 0.429 (sec). Leaf size: 22

 $DSolve[\{2*x-y[x]+(-x+2*y[x])*y'[x] == 0,y[1]==3\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{1}{2} \Big(\sqrt{28 - 3x^2} + x \Big)$$

5.14 problem 14

Internal problem ID [556]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 14.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [_exact, _rational, [_1st_order, '_with_symmetry_[F(x),G(x)]'],

$$-1 + 9x^{2} + y + (x - 4y)y' = 0$$

With initial conditions

$$[y(1) = 0]$$

✓ Solution by Maple

Time used: 0.063 (sec). Leaf size: 25

 $dsolve([-1+9*x^2+y(x)+(x-4*y(x))*diff(y(x),x) = 0,y(1) = 0],y(x), singsol=all)$

$$y(x) = \frac{x}{4} - \frac{\sqrt{24x^3 + x^2 - 8x - 16}}{4}$$

✓ Solution by Mathematica

Time used: 0.131 (sec). Leaf size: 32

 $DSolve[\{-1+9*x^2+y[x]+(x-4*y[x])*y'[x] == 0,y[1]==0\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{1}{4} \Big(x + i\sqrt{16 - x(24x^2 + x - 8)} \Big)$$

5.15 problem 19

Internal problem ID [557]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 19.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [_separable]

$$x^{2}y^{3} + x(1+y^{2})y' = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 25

 $dsolve(x^2*y(x)^3+x*(1+y(x)^2)*diff(y(x),x) = 0,y(x), singsol=all)$

$$y(x) = \mathrm{e}^{rac{\mathrm{LambertW}\left(\mathrm{e}^{x^2+2c_1}
ight)}{2} - rac{x^2}{2} - c_1}$$

✓ Solution by Mathematica

Time used: 3.823 (sec). Leaf size: 46

 $DSolve[x^2*y[x]^3+x*(1+y[x]^2)*y'[x] == 0,y[x],x,IncludeSingularSolutions -> True]$

$$y(x) \rightarrow -\frac{1}{\sqrt{W\left(e^{x^2-2c_1}\right)}}$$

$$y(x) o rac{1}{\sqrt{W(e^{x^2 - 2c_1})}}$$

$$y(x) \to 0$$

5.16 problem 21

Internal problem ID [558]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 21.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_1st_order, '_with_symmetry_[F(x)*G(y),0]']]

$$y + (2x - e^y y) y' = 0$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 27

dsolve(y(x)+(2*x-exp(y(x))*y(x))*diff(y(x),x) = 0,y(x), singsol=all)

$$x - \frac{(y(x)^{2} - 2y(x) + 2) e^{y(x)} + c_{1}}{y(x)^{2}} = 0$$

✓ Solution by Mathematica

Time used: 0.225 (sec). Leaf size: 32

DSolve[y[x]+(2*x-Exp[y[x]]*y[x])*y'[x] == 0,y[x],x,IncludeSingularSolutions -> True]

Solve
$$\left[x = \frac{e^{y(x)}(y(x)^2 - 2y(x) + 2)}{y(x)^2} + \frac{c_1}{y(x)^2}, y(x)\right]$$

5.17 problem 22

Internal problem ID [559]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 22.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$(2+x)\sin(y) + x\cos(y)y' = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 16

dsolve((2+x)*sin(y(x))+x*cos(y(x))*diff(y(x),x) = 0,y(x), singsol=all)

$$y(x) = \arcsin\left(\frac{\mathrm{e}^{-x}}{c_1 x^2}\right)$$

✓ Solution by Mathematica

Time used: 50.001 (sec). Leaf size: 23

DSolve[(2+x)*Sin[y[x]]+x*Cos[y[x]]*y'[x] == 0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to \csc^{-1} \left(x^2 e^{x - c_1} \right)$$

 $y(x) \to 0$

5.18 problem 25

Internal problem ID [560]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 25.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class D'], _rational]

$$2yx + 3x^{2}y + y^{3} + (x^{2} + y^{2})y' = 0$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 420

$$dsolve(2*x*y(x)+3*x^2*y(x)+y(x)^3+(x^2+y(x)^2)*diff(y(x),x) = 0,y(x), singsol=all)$$

$$\begin{split} y(x) &= \frac{\mathrm{e}^{-3x} \Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}}{2c_1} - \frac{2x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}}}{2c_1} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}}}{2c_1} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}}}{2c_1} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}}}{2c_1} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}}}{2c_1} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}}}{2c_1} + \frac{x^2 \mathrm{e}^{3x} c_1}{\Big(\Big(4 + 4\sqrt{4x^6} \mathrm{e}^{6x} c_1^2 + 1 \Big) \, \mathrm{e}^{6x} c_1^2 \Big)^{\frac{1}{3}}}}$$

✓ Solution by Mathematica

Time used: 60.294 (sec). Leaf size: 352

 $DSolve [2*x*y[x]+3*x^2*y[x]+y[x]^3+(x^2+y[x]^2)*y'[x] == 0, y[x], x, Include Singular Solutions \rightarrow 0, y[x], y[x$

$$y(x) \rightarrow \frac{e^{-3x} \left(-2e^{6x}x^2 + \sqrt[3]{2} \left(\sqrt{4e^{18x}x^6 + e^{6(2x+c_1)}} + e^{6x+3c_1}\right)^{2/3}\right)}{2^{2/3} \sqrt[3]{\sqrt{4e^{18x}x^6 + e^{6(2x+c_1)}} + e^{6x+3c_1}}}$$

$$y(x) \rightarrow \frac{4\sqrt[3]{-2}e^{3x}x^2 + 2(-2)^{2/3}e^{-3x} \left(\sqrt{4e^{18x}x^6 + e^{6(2x+c_1)}} + e^{6x+3c_1}\right)^{2/3}}{4\sqrt[3]{\sqrt{4e^{18x}x^6 + e^{6(2x+c_1)}} + e^{6x+3c_1}}}$$

$$y(x) \rightarrow \frac{e^{-3x} \left(\left(1 - i\sqrt{3}\right)e^{6x}x^2 - \sqrt[3]{-2}\left(\sqrt{4e^{18x}x^6 + e^{6(2x+c_1)}} + e^{6x+3c_1}\right)^{2/3}\right)}{2^{2/3} \sqrt[3]{\sqrt{4e^{18x}x^6 + e^{6(2x+c_1)}} + e^{6x+3c_1}}}$$

5.19 problem 26

Internal problem ID [561]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 26.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$y' + 1 - e^{2x} - y = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 14

dsolve(diff(y(x),x) = -1+exp(2*x)+y(x),y(x), singsol=all)

$$y(x) = e^{2x} + 1 + e^x c_1$$

✓ Solution by Mathematica

Time used: 0.046 (sec). Leaf size: 17

 $DSolve[y'[x] == -1 + Exp[2*x] + y[x], y[x], x, IncludeSingularSolutions \rightarrow True]$

$$y(x) \to 1 + e^x(e^x + c_1)$$

5.20 problem 27

Internal problem ID [562]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 27.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_1st_order, '_with_symmetry_[F(x)*G(y),0]']]

$$1 + \left(-\sin\left(y\right) + \frac{x}{y}\right)y' = 0$$

✓ Solution by Maple

Time used: 0.141 (sec). Leaf size: 23

dsolve(1+(-sin(y(x))+x/y(x))*diff(y(x),x) = 0,y(x), singsol=all)

$$x - \frac{-y(x)\cos(y(x)) + \sin(y(x)) + c_1}{y(x)} = 0$$

✓ Solution by Mathematica

Time used: 0.149 (sec). Leaf size: 29

 $DSolve[1+(-Sin[y[x]]+x/y[x])*y'[x] == 0,y[x],x,IncludeSingularSolutions \rightarrow True]$

Solve
$$\left[x = \frac{\sin(y(x)) - y(x)\cos(y(x))}{y(x)} + \frac{c_1}{y(x)}, y(x)\right]$$

5.21 problem 28

Internal problem ID [563]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 28.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_1st_order, _with_exponential_symmetries]]

$$y + (-e^{-2y} + 2yx) y' = 0$$

✓ Solution by Maple

Time used: 0.063 (sec). Leaf size: 24

dsolve(y(x)+(-exp(-2*y(x))+2*x*y(x))*diff(y(x),x) = 0,y(x), singsol=all)

$$y(x) = e^{\text{RootOf}(c_1 e^{-2 e^{-Z}} + Ze^{-2 e^{-Z}} - x)}$$

✓ Solution by Mathematica

Time used: 0.245 (sec). Leaf size: 25

 $DSolve[y[x]+(-Exp[-2*y[x]]+2*x*y[x])*y'[x] == 0,y[x],x,IncludeSingularSolutions \rightarrow True]$

Solve
$$[x = e^{-2y(x)} \log(y(x)) + c_1 e^{-2y(x)}, y(x)]$$

5.22 problem 29

Internal problem ID [564]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 29.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_1st_order, '_with_symmetry_[F(x)*G(y),0]']]

$$e^{x} + (e^{x} \cot(y) + 2 \csc(y) y) y' = 0$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 15

dsolve(exp(x)+(exp(x)*cot(y(x))+2*csc(y(x))*y(x))*diff(y(x),x) = 0,y(x), singsol=all)

$$e^x \sin(y(x)) + y(x)^2 + c_1 = 0$$

✓ Solution by Mathematica

Time used: 0.304 (sec). Leaf size: 18

DSolve [Exp[x] + (Exp[x] * Cot[y[x]] + 2*Csc[y[x]] * y[x]) * y'[x] == 0, y[x], x, Include Singular Solutions)

Solve
$$[y(x)^2 + e^x \sin(y(x)) = c_1, y(x)]$$

5.23 problem 30

Internal problem ID [565]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 30.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_rational]

$$\frac{4x^3}{y^2} + \frac{3}{y} + \left(\frac{3x}{y^2} + 4y\right)y' = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 17

 $dsolve(4*x^3/y(x)^2+3/y(x)+(3*x/y(x)^2+4*y(x))*diff(y(x),x) = 0,y(x), singsol=all)$

$$x^4 + y(x)^4 + 3xy(x) + c_1 = 0$$

✓ Solution by Mathematica

Time used: 60.149 (sec). Leaf size: 1181

$$y(x) \rightarrow -\frac{1}{2} \sqrt{\frac{4\sqrt{2}(x^4 - c_1)}{\sqrt[3]{243x^2 + \sqrt{59049x^4 - 6912(x^4 - c_1)^3}}} + \frac{3\sqrt{243x^2 + \sqrt{59049x^4 - 6912(x^4 - c_1)^3}}}{\sqrt[3]{243x^2 + \sqrt{59049x^4 - 6912(x^4 - c_1)^3}}} - \frac{1}{\sqrt[3]{243x^2 + \sqrt{59049x^4 - 6912(x^4 - c_1)^3}}}} - \frac{1}{\sqrt[3]{243x^2 + \sqrt{59049x^4 - 6912(x^4 - c_1)^3}}}} - \frac{1}{\sqrt[3]{243x^2 + \sqrt{59049x^4 - 6912(x^4 - c_1)^3}}} - \frac{1}{\sqrt[3]{243x^2 + \sqrt{59049x^4 - 6912(x^4 - c_1)^3}}} - \frac{1}{\sqrt[3]{243x^2 + \sqrt{59049x^4 - 6912(x^4 - c_1)^3}}}} - \frac{1}{\sqrt[3]{243x^2 +$$

5.24 problem 30

Internal problem ID [566]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 30.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_rational]

$$3x + \frac{6}{y} + \left(\frac{x^2}{y} + \frac{3y}{x}\right)y' = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 430

 $dsolve(3*x+6/y(x)+(x^2/y(x)+3*y(x)/x)*diff(y(x),x) = 0,y(x), singsol=all)$

$$y(x) = \frac{\left(-324x^2 - 108c_1 + 12\sqrt{12x^9 + 729x^4 + 486c_1x^2 + 81c_1^2}\right)^{\frac{1}{3}}}{6} - \frac{2x^3}{\left(-324x^2 - 108c_1 + 12\sqrt{12x^9 + 729x^4 + 486c_1x^2 + 81c_1^2}\right)^{\frac{1}{3}}}}{12}$$

$$y(x) = -\frac{\left(-324x^2 - 108c_1 + 12\sqrt{12x^9 + 729x^4 + 486c_1x^2 + 81c_1^2}\right)^{\frac{1}{3}}}{12} + \frac{x^3}{\left(-324x^2 - 108c_1 + 12\sqrt{12x^9 + 729x^4 + 486c_1x^2 + 81c_1^2}\right)^{\frac{1}{3}}}}$$

$$-\frac{i\sqrt{3}\left(\frac{\left(-324x^2 - 108c_1 + 12\sqrt{12x^9 + 729x^4 + 486c_1x^2 + 81c_1^2}\right)^{\frac{1}{3}}}{6} + \frac{2x^3}{\left(-324x^2 - 108c_1 + 12\sqrt{12x^9 + 729x^4 + 486c_1x^2 + 81c_1^2}\right)^{\frac{1}{3}}}}\right)}}{2}$$

$$y(x) = -\frac{\left(-324x^2 - 108c_1 + 12\sqrt{12x^9 + 729x^4 + 486c_1x^2 + 81c_1^2}\right)^{\frac{1}{3}}}{12} + \frac{x^3}{\left(-324x^2 - 108c_1 + 12\sqrt{12x^9 + 729x^4 + 486c_1x^2 + 81c_1^2}\right)^{\frac{1}{3}}}}$$

$$i\sqrt{3}\left(\frac{\left(-324x^2 - 108c_1 + 12\sqrt{12x^9 + 729x^4 + 486c_1x^2 + 81c_1^2}\right)^{\frac{1}{3}}}{6} + \frac{2x^3}{\left(-324x^2 - 108c_1 + 12\sqrt{12x^9 + 729x^4 + 486c_1x^2 + 81c_1^2}\right)^{\frac{1}{3}}}}$$

$$+ \frac{1\sqrt{3}\left(\frac{\left(-324x^2 - 108c_1 + 12\sqrt{12x^9 + 729x^4 + 486c_1x^2 + 81c_1^2}\right)^{\frac{1}{3}}}{6} + \frac{2x^3}{\left(-324x^2 - 108c_1 + 12\sqrt{12x^9 + 729x^4 + 486c_1x^2 + 81c_1^2}\right)^{\frac{1}{3}}}}$$

✓ Solution by Mathematica

Time used: 4.467 (sec). Leaf size: 331

 $DSolve[3*x+6/y[x]+(x^2/y[x]+3*y[x]/x)*y'[x] == 0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \rightarrow \frac{\sqrt[3]{-81x^2 + \sqrt{108x^9 + 729(-3x^2 + c_1)^2} + 27c_1}}{3\sqrt[3]{2}x^3} - \frac{\sqrt[3]{2}x^3}{\sqrt[3]{-81x^2 + \sqrt{108x^9 + 729(-3x^2 + c_1)^2} + 27c_1}}$$

$$y(x) \rightarrow \frac{(-1 + i\sqrt{3})\sqrt[3]{-81x^2 + \sqrt{108x^9 + 729(-3x^2 + c_1)^2} + 27c_1}}{6\sqrt[3]{2}} + \frac{(1 + i\sqrt{3})x^3}{2^{2/3}\sqrt[3]{-81x^2 + \sqrt{108x^9 + 729(-3x^2 + c_1)^2} + 27c_1}}}{(1 - i\sqrt{3})x^3}$$

$$y(x) \rightarrow \frac{(1 - i\sqrt{3})x^3}{2^{2/3}\sqrt[3]{-81x^2 + \sqrt{108x^9 + 729(-3x^2 + c_1)^2} + 27c_1}} - \frac{(1 + i\sqrt{3})\sqrt[3]{-81x^2 + \sqrt{108x^9 + 729(-3x^2 + c_1)^2} + 27c_1}}{6\sqrt[3]{2}}$$

5.25 problem 32

Internal problem ID [567]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Section 2.6. Page 100

Problem number: 32.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, [_Abel, '2nd type', 'class A'],

$$3yx + y^{2} + (x^{2} + yx)y' = 0$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 59

 $dsolve(3*x*y(x)+y(x)^2+(x^2+x*y(x))*diff(y(x),x) = 0,y(x), singsol=all)$

$$y(x) = \frac{-c_1 x^2 - \sqrt{c_1^2 x^4 + 1}}{c_1 x}$$

$$y(x) = \frac{-c_1 x^2 + \sqrt{c_1^2 x^4 + 1}}{c_1 x}$$

✓ Solution by Mathematica

Time used: 0.613 (sec). Leaf size: 93

 $DSolve [3*x*y[x]+y[x]^2+(x^2+x*y[x])*y'[x] == 0, y[x], x, Include Singular Solutions \rightarrow True]$

$$y(x) \to -\frac{x^2 + \sqrt{x^4 + e^{2c_1}}}{x}$$

$$y(x) \to -x + \frac{\sqrt{x^4 + e^{2c_1}}}{x}$$

$$y(x) \rightarrow -\frac{\sqrt{x^4} + x^2}{x}$$

$$y(x) o rac{\sqrt{x^4}}{x} - x$$

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6.1 problem 1

Internal problem ID [568]

 $\mathbf{Book} \text{: } \mathbf{Elementary \ differential \ equations \ and \ boundary \ value \ problems, \ 10th \ ed., \ Boyce \ and }$

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 1.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$y' - \frac{x^3 - 2y}{x} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

 $dsolve(diff(y(x),x) = (x^3-2*y(x))/x,y(x), singsol=all)$

$$y(x) = \frac{\frac{x^5}{5} + c_1}{x^2}$$

✓ Solution by Mathematica

Time used: 0.024 (sec). Leaf size: 19

 $DSolve[y'[x] == (x^3-2*y[x])/x, y[x], x, IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{x^3}{5} + \frac{c_1}{x^2}$$

6.2 problem 2

Internal problem ID [569]

 \mathbf{Book} : Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 2.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [separable]

$$y' - \frac{\cos(x) + 1}{2 - \sin(y)} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

dsolve(diff(y(x),x) = (1+cos(x))/(2-sin(y(x))),y(x), singsol=all)

$$x + \sin(x) - 2y(x) - \cos(y(x)) + c_1 = 0$$

✓ Solution by Mathematica

Time used: 0.346 (sec). Leaf size: 27

 $DSolve[y'[x] == (1+Cos[x])/(2-Sin[y[x]]), y[x], x, IncludeSingularSolutions \rightarrow True]$

$$y(x) \rightarrow \text{InverseFunction}[-2\#1 - \cos(\#1)\&][-x - \sin(x) + c_1]$$

6.3 problem 3

Internal problem ID [570]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 3.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [rational]

$$y' - \frac{2x + y}{3 - x + 3y^2} = 0$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 0.109 (sec). Leaf size: 75

$$y(x) = \frac{\left(108x^2 + 12\sqrt{81x^4 - 12x^3 + 108x^2 - 324x + 324}\right)^{\frac{2}{3}} + 12x - 36}{6\left(108x^2 + 12\sqrt{81x^4 - 12x^3 + 108x^2 - 324x + 324}\right)^{\frac{1}{3}}}$$

✓ Solution by Mathematica

Time used: 5.275 (sec). Leaf size: 98

 $DSolve[\{y'[x] == (2*x+y[x])/(3-x+3*y[x]^2),y[0]==0\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{-\sqrt[3]{2} \left(\sqrt{3x(x(x(27x-4)+36)-108)+324}-9x^2\right)^{2/3}-2\sqrt[3]{3}x+6\sqrt[3]{3}}{6^{2/3}\sqrt[3]{\sqrt{3x(x(x(27x-4)+36)-108)+324}-9x^2}}$$

6.4 problem 4

Internal problem ID [571]

 $\mathbf{Book} \text{: } \mathbf{Elementary \ differential \ equations \ and \ boundary \ value \ problems, \ 10th \ ed., \ Boyce \ and }$

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 4.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - 3 + 6x - y + 2yx = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

dsolve(diff(y(x),x) = 3-6*x+y(x)-2*x*y(x),y(x), singsol=all)

$$y(x) = -3 + e^{-x(x-1)}c_1$$

✓ Solution by Mathematica

Time used: 0.046 (sec). Leaf size: 24

DSolve[y'[x] == 3-6*x+y[x]-2*x*y[x],y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to -3 + c_1 e^{x - x^2}$$
$$y(x) \to -3$$

6.5 problem 5

Internal problem ID [572]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 5.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_rational, [_Abel, '2nd type', 'class B']]

$$y' - \frac{-1 - 2yx - y^2}{x^2 + 2yx} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 57

 $dsolve(diff(y(x),x) = (-1-2*x*y(x)-y(x)^2)/(x^2+2*x*y(x)),y(x), singsol=all)$

$$y(x) = \frac{-x^2 + \sqrt{x^4 - 4c_1x - 4x^2}}{2x}$$

$$y(x) = -\frac{x^2 + \sqrt{x^4 - 4c_1x - 4x^2}}{2x}$$

✓ Solution by Mathematica

Time used: 0.437 (sec). Leaf size: 67

 $DSolve[y'[x] == (-1-2*x*y[x]-y[x]^2)/(x^2+2*x*y[x]), y[x], x, IncludeSingularSolutions -> True]$

$$y(x) \to -\frac{x^2 + \sqrt{x(x^3 - 4x + 4c_1)}}{2x}$$

$$y(x) \to \frac{-x^2 + \sqrt{x(x^3 - 4x + 4c_1)}}{2x}$$

6.6 problem 6

Internal problem ID [573]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 6.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [linear]

$$yx + y'x - 1 + y = 0$$

With initial conditions

$$[y(1) = 0]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 18

dsolve([x*y(x)+x*diff(y(x),x) = 1-y(x),y(1) = 0],y(x), singsol=all)

$$y(x) = \frac{1 - e^{1-x}}{x}$$

✓ Solution by Mathematica

Time used: 0.028 (sec). Leaf size: 20

 $DSolve[\{x*y[x]+x*y'[x] == 1-y[x],y[1]==0\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{e \sinh(x) - e \cosh(x) + 1}{x}$$

6.7 problem 7

Internal problem ID [574]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 7.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{4x^3 + 1}{y(2+3y)} = 0$$

✓ Solution by Maple

y(x)

Time used: 0.0 (sec). Leaf size: 660

 $dsolve(diff(y(x),x) = (4*x^3+1)/(y(x)*(2+3*y(x))),y(x), singsol=all)$

$$= \frac{\left(-8+108x^4+108c_1+108x+12\sqrt{81x^8+162x^4c_1+162x^5}-12x^4+81c_1^2+162c_1x+81x^2-12c_1-18x^4+108x^4+108c_1+108x+12\sqrt{81x^8+162x^4c_1+162x^5}-12x^4+81c_1^2+162c_1x+81x^2-12c_1-18x^4+108c_1+108x+12\sqrt{81x^8+162x^4c_1+162x^5}-12x^4+81c_1^2+162c_1x+81x^2-12c_1-18x^4+108c_1+108x+12\sqrt{81x^8+162x^4c_1+162x^5}-12x^4+81c_1^2+162c_1x+81x^2-12c_1-18x^4+108c_1+108x+12\sqrt{81x^8+162x^4c_1+162x^5}-12x^4+81c_1^2+162c_1x+81x^2-12c_1-18x^4+108c_1+108x+12\sqrt{81x^8+162x^4c_1+162x^5}-12x^4+81c_1^2+162c_1x+81x^2-12c_1-18x^4+108c_1+108x^4+108c_1+108x+12\sqrt{81x^8+162x^4c_1+162x^5}-12x^4+81c_1^2+162c_1x+81x^2-12c_1-12x^4+108c_1+108x^4+108c_1+108x+12\sqrt{81x^8+162x^4c_1+162x^5}-12x^4+81c_1^2+162c_1x+81x^2-12c_1-12c_1-12x^4+162c_1x+81x^2-12c_1-12c_1-12x^4+162x^5}-12x^4+108c_1+108x^4+108c_1+108x+12\sqrt{81x^8+162x^4c_1+162x^5}-12x^4+81c_1^2+162c_1x+81x^2-12c_1-1$$

✓ Solution by Mathematica

Time used: 4.325 (sec). Leaf size: 333

DSolve[y'[x] == $(4*x^3+1)/(y[x]*(2+3*y[x]))$, y[x], x, IncludeSingularSolutions -> True]

$$y(x) \to \frac{1}{6} \left(2^{2/3} \sqrt[3]{27x^4 + \sqrt{-4 + (27(x^4 + x) - 2 + 27c_1)^2 + 27x - 2 + 27c_1}} \right. \\ + \frac{2\sqrt[3]{2}}{\sqrt[3]{27x^4 + \sqrt{-4 + (27(x^4 + x) - 2 + 27c_1)^2 + 27x - 2 + 27c_1}}} - 2 \right)$$

$$y(x) \to \frac{1}{12} \left(i2^{2/3} \left(\sqrt{3} + i \right) \sqrt[3]{27x^4 + \sqrt{-4 + (27(x^4 + x) - 2 + 27c_1)^2 + 27x - 2 + 27c_1}} \right. \\ - \frac{4\sqrt[3]{-2}}{\sqrt[3]{27x^4 + \sqrt{-4 + (27(x^4 + x) - 2 + 27c_1)^2 + 27x - 2 + 27c_1}}} - 4 \right)$$

$$y(x) \to \frac{1}{12} \left(-2^{2/3} \left(1 + i\sqrt{3} \right) \sqrt[3]{27x^4 + \sqrt{-4 + (27(x^4 + x) - 2 + 27c_1)^2 + 27x - 2 + 27c_1}} \right. \\ + \frac{4(-1)^{2/3} \sqrt[3]{2}}{\sqrt[3]{27x^4 + \sqrt{-4 + (27(x^4 + x) - 2 + 27c_1)^2 + 27x - 2 + 27c_1}}} - 4 \right)$$

6.8 problem 8

Internal problem ID [575]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 8.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [linear]

$$2y + y'x - \frac{\sin(x)}{x} = 0$$

With initial conditions

$$[y(2) = 1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 16

dsolve([2*y(x)+x*diff(y(x),x) = sin(x)/x,y(2) = 1],y(x), singsol=all)

$$y(x) = \frac{-\cos(x) + 4 + \cos(2)}{x^2}$$

✓ Solution by Mathematica

Time used: 0.037 (sec). Leaf size: 17

 $DSolve[\{2*y[x]+x*y'[x] == Sin[x]/x,y[2]==1\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{-\cos(x) + 4 + \cos(2)}{x^2}$$

6.9 problem 9

Internal problem ID [576]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 9.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [_rational, [_1st_order, '_with_symmetry_[F(x),G(x)]'], [_Abel,

$$y' - \frac{-1 - 2yx}{x^2 + 2y} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 47

 $dsolve(diff(y(x),x) = (-1-2*x*y(x))/(x^2+2*y(x)),y(x), singsol=all)$

$$y(x) = -\frac{x^2}{2} - \frac{\sqrt{x^4 - 4c_1 - 4x}}{2}$$

$$y(x) = -\frac{x^2}{2} + \frac{\sqrt{x^4 - 4c_1 - 4x}}{2}$$

✓ Solution by Mathematica

Time used: 0.125 (sec). Leaf size: 61

 $DSolve[y'[x] == (-1-2*x*y[x])/(x^2+2*y[x]), y[x], x, IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{1}{2} \Big(-x^2 - \sqrt{x^4 - 4x + 4c_1} \Big)$$

$$y(x) \to \frac{1}{2} \left(-x^2 + \sqrt{x^4 - 4x + 4c_1} \right)$$

6.10 problem 10

Internal problem ID [577]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 10.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$\frac{-x^2 + x + 1}{x^2} + \frac{yy'}{y - 2} = 0$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 26

 $dsolve((-x^2+x+1)/x^2+y(x)*diff(y(x),x)/(-2+y(x)) = 0,y(x), singsol=all)$

$$y(x) = 2 \operatorname{LambertW}\left(rac{c_1 \mathrm{e}^{rac{x}{2}-1+rac{1}{2x}}}{2\sqrt{x}}
ight) + 2$$

✓ Solution by Mathematica

Time used: 54.455 (sec). Leaf size: 68

 $DSolve[(-x^2+x+1)/x^2+y[x]*y'[x]/(-2+y[x]) == 0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to 2\left(1 + W\left(-\frac{1}{2}\sqrt{\frac{e^{x + \frac{1}{x} - 2 + c_1}}{x}}\right)\right)$$
$$y(x) \to 2\left(1 + W\left(\frac{1}{2}\sqrt{\frac{e^{x + \frac{1}{x} - 2 + c_1}}{x}}\right)\right)$$
$$y(x) \to 2$$

6.11 problem 11

Internal problem ID [578]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 11.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_exact]

$$x^{2} + y + (e^{y} + x)y' = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 38

 $dsolve(x^2+y(x)+(exp(y(x))+x)*diff(y(x),x) = 0,y(x), singsol=all)$

$$y(x) = -\operatorname{LambertW}\left(rac{\mathrm{e}^{-rac{x^2}{3}}\mathrm{e}^{-rac{c_1}{x}}}{x}
ight) - rac{x^3 + 3c_1}{3x}$$

✓ Solution by Mathematica

Time used: 3.308 (sec). Leaf size: 42

 $DSolve[x^2+y[x]+(Exp[y[x]]+x)*y'[x] == 0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) o -W \left(rac{e^{-rac{x^2}{3} + rac{c_1}{x}}}{x}
ight) - rac{x^2}{3} + rac{c_1}{x}$$

6.12 problem 12

Internal problem ID [579]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

 $\operatorname{DiPrima}$

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 12.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [_linear]

$$y' + y - \frac{1}{e^x + 1} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 16

dsolve(y(x)+diff(y(x),x) = 1/(1+exp(x)),y(x), singsol=all)

$$y(x) = (\ln (1 + e^x) + c_1) e^{-x}$$

✓ Solution by Mathematica

Time used: 0.068 (sec). Leaf size: 20

DSolve[y[x]+y'[x] == 1/(1+Exp[x]),y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-x}(\log(e^x + 1) + c_1)$$

6.13 problem 13

Internal problem ID [580]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 13.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - 1 - 2x - y^2 - 2xy^2 = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 11

 $dsolve(diff(y(x),x) = 1+2*x+y(x)^2+2*x*y(x)^2,y(x), singsol=all)$

$$y(x) = \tan\left(x^2 + c_1 + x\right)$$

✓ Solution by Mathematica

Time used: 0.176 (sec). Leaf size: 13

 $DSolve[y'[x] == 1 + 2 * x + y[x]^2 + 2 * x * y[x]^2, y[x], x, IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \tan\left(x^2 + x + c_1\right)$$

6.14 problem 14

Internal problem ID [581]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 14.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _exact, _rational, [_Abel, '2nd type

$$x + y + (x + 2y)y' = 0$$

With initial conditions

$$[y(2) = 3]$$

✓ Solution by Maple

Time used: 0.141 (sec). Leaf size: 19

dsolve([x+y(x)+(x+2*y(x))*diff(y(x),x) = 0,y(2) = 3],y(x), singsol=all)

$$y(x) = -\frac{x}{2} + \frac{\sqrt{-x^2 + 68}}{2}$$

✓ Solution by Mathematica

Time used: 0.438 (sec). Leaf size: 24

 $DSolve[\{x+y[x]+(x+2*y[x])*y'[x] == 0,y[2]==3\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{1}{2} \left(\sqrt{68 - x^2} - x \right)$$

6.15 problem 15

Internal problem ID [582]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 15.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [_separable]

$$(e^x + 1) y' - y + e^x y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 14

dsolve((1+exp(x))*diff(y(x),x) = y(x)-exp(x)*y(x),y(x), singsol=all)

$$y(x) = \frac{c_1 \mathrm{e}^x}{\left(1 + \mathrm{e}^x\right)^2}$$

✓ Solution by Mathematica

Time used: 0.075 (sec). Leaf size: 23

DSolve[(1+Exp[x])*y'[x] == y[x]-Exp[x]*y[x],y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to \frac{c_1 e^x}{\left(e^x + 1\right)^2}$$

$$y(x) \to 0$$

6.16 problem 16

Internal problem ID [583]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 16.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [NONE]

$$y' - \frac{-e^{2y}\cos(x) + \cos(y)e^{-x}}{2e^{2y}\sin(x) - \sin(y)e^{-x}} = 0$$

✓ Solution by Maple

Time used: 0.063 (sec). Leaf size: 21

dsolve(diff(y(x),x) = (-exp(2*y(x))*cos(x)+cos(y(x))/exp(x))/(2*exp(2*y(x))*sin(x)-sin(y(x))/exp(x))/(2*exp(2*y(x))*sin(x)-sin(y(x))/exp(x))/(2*exp(2*y(x))*sin(x)-sin(y(x))/exp(x))/(2*exp(2*y(x))*sin(x)-sin(y(x))/exp(x))/(2*exp(2*y(x))*sin(x)-sin(y(x))/exp(x))/(2*exp(2*y(x))*sin(x)-sin(y(x))/exp(x))/(2*exp(2*y(x))*sin(x)-sin(y(x))/exp(x)/exp

$$e^{2y(x)}\sin(x) + \cos(y(x))e^{-x} + c_1 = 0$$

✓ Solution by Mathematica

Time used: 0.485 (sec). Leaf size: 25

DSolve[y'[x] == (-Exp[2*y[x]]*Cos[x]+Cos[y[x]]/Exp[x])/(2*Exp[2*y[x]]*Sin[x]-Sin[y[x]]/Exp[x])

Solve
$$[e^{2y(x)}\sin(x) + e^{-x}\cos(y(x)) = c_1, y(x)]$$

6.17 problem 17

Internal problem ID [584]

 \mathbf{Book} : Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 17.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$y' - e^{2x} - 3y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

dsolve(diff(y(x),x) = exp(2*x)+3*y(x),y(x), singsol=all)

$$y(x) = \left(-\mathrm{e}^{-x} + c_1\right) \mathrm{e}^{3x}$$

✓ Solution by Mathematica

Time used: 0.041 (sec). Leaf size: 19

DSolve[y'[x] == Exp[2*x]+3*y[x],y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{2x}(-1 + c_1 e^x)$$

6.18 problem 18

Internal problem ID [585]

 \mathbf{Book} : Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 18.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_linear, 'class A']]

$$2y + y' - e^{-x^2 - 2x} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 18

 $dsolve(2*y(x)+diff(y(x),x) = exp(-x^2-2*x),y(x), singsol=all)$

$$y(x) = \left(\frac{\sqrt{\pi} \operatorname{erf}(x)}{2} + c_1\right) e^{-2x}$$

✓ Solution by Mathematica

Time used: 0.088 (sec). Leaf size: 27

DSolve $[2*y[x]+y'[x] == Exp[-x^2-2*x], y[x], x, IncludeSingularSolutions -> True]$

$$y(x) \rightarrow \frac{1}{2}e^{-2x} \left(\sqrt{\pi}\operatorname{erf}(x) + 2c_1\right)$$

6.19 problem 19

Internal problem ID [586]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 19.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_rational]

$$y' - \frac{3x^2 - 2y - y^3}{2x + 3xy^2} = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 507

 $dsolve(diff(y(x),x) = (3*x^2-2*y(x)-y(x)^3)/(2*x+3*x*y(x)^2),y(x), singsol=all)$

$$y(x) = \frac{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}{6x} \\ - \frac{4x}{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}}{(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1)x^2)^{\frac{1}{3}}}} \\ y(x) = -\frac{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}{12x}}{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}} \\ -\frac{i\sqrt{3}\left(\frac{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}{6x}}{2} + \frac{4x}{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}} \\ + \frac{12x}{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}} \\ + \frac{i\sqrt{3}\left(\frac{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}{6x}} + \frac{4x}{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}} \\ + \frac{i\sqrt{3}\left(\frac{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}{6x}} + \frac{4x}{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}} \\ + \frac{2x}{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}} + \frac{4x}{\left(\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}} \\ + \frac{12x}{\left(108x^3 + 12\sqrt{3}\sqrt{27x^6 - 54c_1x^3 + 27c_1^2 + 32x^2} - 108c_1\right)x^2\right)^{\frac{1}{3}}}}$$

✓ Solution by Mathematica

Time used: 32.11 (sec). Leaf size: 358

$$y(x) \rightarrow \frac{\sqrt[3]{27x^5 + 27c_1x^2 + \sqrt{864x^6 + 729x^4 (x^3 + c_1)^2}}}{3\sqrt[3]{2}x} - \frac{2\sqrt[3]{2}x}{\sqrt[3]{27x^5 + 27c_1x^2 + \sqrt{864x^6 + 729x^4 (x^3 + c_1)^2}}}$$

$$y(x) \rightarrow \frac{\sqrt[3]{2(1 + i\sqrt{3}) x}}{\sqrt[3]{27x^5 + 27c_1x^2 + \sqrt{864x^6 + 729x^4 (x^3 + c_1)^2}}} - \frac{(1 - i\sqrt{3})\sqrt[3]{27x^5 + 27c_1x^2 + \sqrt{864x^6 + 729x^4 (x^3 + c_1)^2}}}{6\sqrt[3]{2}x}$$

$$y(x) \rightarrow \frac{\sqrt[3]{2(1 - i\sqrt{3}) x}}{\sqrt[3]{27x^5 + 27c_1x^2 + \sqrt{864x^6 + 729x^4 (x^3 + c_1)^2}}} - \frac{(1 + i\sqrt{3})\sqrt[3]{27x^5 + 27c_1x^2 + \sqrt{864x^6 + 729x^4 (x^3 + c_1)^2}}}{6\sqrt[3]{2}x}$$

6.20 problem 20

Internal problem ID [587]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 20.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - e^{x+y} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 13

dsolve(diff(y(x),x) = exp(x+y(x)),y(x), singsol=all)

$$y(x) = \ln\left(-\frac{1}{e^x + c_1}\right)$$

✓ Solution by Mathematica

Time used: 0.751 (sec). Leaf size: 18

DSolve[y'[x] == Exp[x+y[x]],y[x],x,IncludeSingularSolutions -> True]

$$y(x) \rightarrow -\log\left(-e^x - c_1\right)$$

6.21 problem 21

Internal problem ID [588]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 21.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_rational]

$$\frac{-4 + 6yx + 2y^2}{3x^2 + 4yx + 3y^2} + y' = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 561

 $dsolve((-4+6*x*y(x)+2*y(x)^2)/(3*x^2+4*x*y(x)+3*y(x)^2)+diff(y(x),x)=0,y(x), singsol=all)$

$$y(x) = \frac{\left(152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}{6} - \frac{6}{10x^2} - \frac{6}{3\left(152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}{2} - \frac{2x}{3}$$

$$y(x) = -\frac{\left(152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}{12} - \frac{12}{3\left(152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}{2} - \frac{2x}{3}$$

$$-\frac{2x}{3}$$

$$i\sqrt{3}\left(\frac{\left(152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}{6} + \frac{10x^2}{3\left(152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2}$$

$$y(x) = -\frac{\left(152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}{12} + \frac{12}{3\left(152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}{12} - \frac{2x}{3} - \frac{2x}{3} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}{12} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x + 1296x^2}\right)^{\frac{1}{3}}}}{2} + \frac{10x^2}{3\left(\frac{152x^3 - 108c_1 + 432x + 12\sqrt{216x^6 - 228c_1x^3 + 912x^4 + 81c_1^2 - 648c_1x +$$

✓ Solution by Mathematica

Time used: 4.605 (sec). Leaf size: 383

 $DSolve[(-4+6*x*y[x]+2*y[x]^2)/(3*x^2+4*x*y[x]+3*y[x]^2)+y'[x]==0,y[x],x,IncludeSingularSoluti]$

$$y(x) \to \frac{1}{6} \left(2^{2/3} \sqrt[3]{38x^3 + \sqrt{500x^6 + (38x^3 + 108x + 27c_1)^2 + 108x + 27c_1}} - \frac{10\sqrt[3]{2}x^2}{\sqrt[3]{38x^3 + \sqrt{500x^6 + (38x^3 + 108x + 27c_1)^2 + 108x + 27c_1}}} - 4x \right)$$

$$y(x) \to \frac{1}{12} \left(i2^{2/3} \left(\sqrt{3} + i \right) \sqrt[3]{38x^3 + \sqrt{500x^6 + (38x^3 + 108x + 27c_1)^2 + 108x + 27c_1}} + \frac{10\sqrt[3]{2} (1 + i\sqrt{3}) x^2}{\sqrt[3]{38x^3 + \sqrt{500x^6 + (38x^3 + 108x + 27c_1)^2 + 108x + 27c_1}}} - 8x \right)$$

$$y(x) \to \frac{1}{12} \left(-2^{2/3} \left(1 + i\sqrt{3} \right) \sqrt[3]{38x^3 + \sqrt{500x^6 + (38x^3 + 108x + 27c_1)^2 + 108x + 27c_1}} - 8x \right)$$

$$+ \frac{10\sqrt[3]{2} (1 - i\sqrt{3}) x^2}{\sqrt[3]{38x^3 + \sqrt{500x^6 + (38x^3 + 108x + 27c_1)^2 + 108x + 27c_1}}} - 8x \right)$$

6.22 problem 22

Internal problem ID [589]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 22.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [separable]

$$y' - \frac{x^2 - 1}{1 + y^2} = 0$$

With initial conditions

$$[y(-1) = 1]$$

✓ Solution by Maple

Time used: 0.172 (sec). Leaf size: 87

 $dsolve([diff(y(x),x) = (x^2-1)/(1+y(x)^2),y(-1) = 1],y(x), singsol=all)$

$$y(x) = \frac{\left(8 + 4x^3 - 12x + 4\sqrt{x^6 - 6x^4 + 4x^3 + 9x^2 - 12x + 8}\right)^{\frac{2}{3}} - 4}{2\left(8 + 4x^3 - 12x + 4\sqrt{x^6 - 6x^4 + 4x^3 + 9x^2 - 12x + 8}\right)^{\frac{1}{3}}}$$

✓ Solution by Mathematica

Time used: 2.826 (sec). Leaf size: 85

 $DSolve[\{y'[x]==(x^2-1)/(1+y[x]^2),y[-1]==1\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{\sqrt[3]{2} \left(x^3 + \sqrt{x(x^2 - 3)(x^3 - 3x + 4) + 8} - 3x + 2\right)^{2/3} - 2}{2^{2/3} \sqrt[3]{x^3 + \sqrt{x(x^2 - 3)(x^3 - 3x + 4) + 8} - 3x + 2}}$$

6.23 problem 23

Internal problem ID [590]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 23.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$(t+1)y + ty' - e^{2t} = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 20

dsolve((1+t)*y(t)+t*diff(y(t),t) = exp(2*t),y(t), singsol=all)

$$y(t) = rac{\left(rac{\mathrm{e}^{3t}}{3} + c_1
ight)\mathrm{e}^{-t}}{t}$$

✓ Solution by Mathematica

Time used: 0.057 (sec). Leaf size: 27

DSolve[(1+t)*y[t]+t*y'[t] == Exp[2*t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) o rac{e^{2t} + 3c_1e^{-t}}{3t}$$

6.24 problem 24

Internal problem ID [591]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 24.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_separable]

$$2\cos(x)\sin(x)\sin(y) + \cos(y)\sin(x)^{2}y' = 0$$

✓ Solution by Maple

Time used: 0.109 (sec). Leaf size: 18

 $dsolve(2*cos(x)*sin(x)*sin(y(x))+cos(y(x))*sin(x)^2*diff(y(x),x) = 0,y(x), singsol=all)$

$$y(x) = -\arcsin\left(\frac{2c_1}{-1 + \cos(2x)}\right)$$

✓ Solution by Mathematica

Time used: 5.1 (sec). Leaf size: 21

$$y(x) \to \arcsin\left(\frac{1}{2}c_1\csc^2(x)\right)$$

 $y(x) \to 0$

6.25 problem 25

Internal problem ID [592]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 25.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_exact, _rational]

$$\frac{2x}{y} - \frac{y}{x^2 + y^2} + \left(-\frac{x^2}{y^2} + \frac{x}{x^2 + y^2}\right)y' = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 19

 $dsolve(2*x/y(x)-y(x)/(x^2+y(x)^2)+(-x^2/y(x)^2+x/(x^2+y(x)^2))*diff(y(x),x) = 0,y(x), singsolve(x) + (x^2+y(x)^2) + (x^2+y(x$

$$y(x) = \frac{x}{\tan \left(\text{RootOf} \left(-\underline{Z} + x \tan \left(\underline{Z} \right) + c_1 \right) \right)}$$

✓ Solution by Mathematica

Time used: 0.256 (sec). Leaf size: 23

 $DSolve[2*x/y[x]-y[x]/(x^2+y[x]^2)+(-x^2/y[x]^2+x/(x^2+y[x]^2))*y'[x] == 0,y[x],x,IncludeSingularing various and various and$

Solve
$$\left[\arctan\left(\frac{x}{y(x)}\right) - \frac{x^2}{y(x)} = c_1, y(x)\right]$$

6.26 problem 26

Internal problem ID [593]

 \mathbf{Book} : Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 26.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _dAlembert]

$$y'x - e^{\frac{y}{x}}x - y = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 15

dsolve(x*diff(y(x),x) = exp(y(x)/x)*x+y(x),y(x), singsol=all)

$$y(x) = \ln\left(-\frac{1}{\ln(x) + c_1}\right)x$$

✓ Solution by Mathematica

Time used: 0.301 (sec). Leaf size: 18

DSolve[x*y'[x] == Exp[y[x]/x]*x+y[x],y[x],x,IncludeSingularSolutions -> True]

$$y(x) \rightarrow -x \log(-\log(x) - c_1)$$

6.27 problem 27

Internal problem ID [594]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 27.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_rational, [_1st_order, '_with_symmetry_[F(x)*G(y),0]']]

$$y' - \frac{x}{x^2 + y + y^3} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 40

 $dsolve(diff(y(x),x) = x/(x^2+y(x)+y(x)^3),y(x), singsol=all)$

$$c_1 - e^{-2y(x)}x^2 - \frac{(4y(x)^3 + 6y(x)^2 + 10y(x) + 5)e^{-2y(x)}}{4} = 0$$

✓ Solution by Mathematica

Time used: 0.171 (sec). Leaf size: 48

DSolve[y'[x] == $x/(x^2+y[x]+y[x]^3)$,y[x],x,IncludeSingularSolutions -> True]

Solve
$$\left[-\frac{1}{2}x^2e^{-2y(x)} - \frac{1}{8}e^{-2y(x)} \left(4y(x)^3 + 6y(x)^2 + 10y(x) + 5 \right) = c_1, y(x) \right]$$

6.28 problem 28

Internal problem ID [595]

 $\mathbf{Book} \text{: } \textbf{Elementary differential equations and boundary value problems, } 10 \textbf{th ed.}, \ \textbf{Boyce and}$

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 28.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [_linear]

$$3t + 2y + ty' = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 13

dsolve(3*t+2*y(t) = -t*diff(y(t),t),y(t), singsol=all)

$$y(t) = -t + \frac{c_1}{t^2}$$

✓ Solution by Mathematica

Time used: 0.025 (sec). Leaf size: 15

DSolve[3*t+2*y[t] == -t*y'[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow -t + \frac{c_1}{t^2}$$

6.29 problem 29

Internal problem ID [596]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 29.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, [_Abel, '2nd type', 'class A'],

$$y' - \frac{x+y}{x-y} = 0$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 24

dsolve(diff(y(x),x) = (x+y(x))/(x-y(x)),y(x), singsol=all)

$$y(x) = \tan\left(\operatorname{RootOf}\left(-2_Z + \ln\left(\frac{1}{\cos\left(_Z\right)^2}\right) + 2\ln(x) + 2c_1\right)\right)x$$

✓ Solution by Mathematica

Time used: 0.033 (sec). Leaf size: 36

 $DSolve[y'[x] == (x+y[x])/(x-y[x]), y[x], x, IncludeSingularSolutions \rightarrow True]$

Solve
$$\left[\frac{1}{2}\log\left(\frac{y(x)^2}{x^2}+1\right) - \arctan\left(\frac{y(x)}{x}\right) = -\log(x) + c_1, y(x)\right]$$

6.30 problem 30

Internal problem ID [597]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 30.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class A'], _rational, [_Abel, '2nd type', 'class A'],

$$2yx + 3y^2 - (x^2 + 2yx)y' = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 35

 $dsolve(2*x*y(x)+3*y(x)^2-(x^2+2*x*y(x))*diff(y(x),x) = 0,y(x), singsol=all)$

$$y(x) = \left(-\frac{1}{2} - \frac{\sqrt{4c_1x + 1}}{2}\right)x$$

$$y(x) = \left(-\frac{1}{2} + \frac{\sqrt{4c_1x + 1}}{2}\right)x$$

✓ Solution by Mathematica

Time used: 0.373 (sec). Leaf size: 61

 $DSolve[2*x*y[x]+3*y[x]^2-(x^2+2*x*y[x])*y'[x] == 0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to -\frac{1}{2}x \Big(1 + \sqrt{1 + 4e^{c_1}x}\Big)$$

$$y(x) \to \frac{1}{2}x \Big(-1 + \sqrt{1 + 4e^{c_1}x}\Big)$$

$$y(x) \to 0$$

$$y(x) \to -x$$

6.31 problem 31

Internal problem ID [598]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Miscellaneous problems, end of chapter 2. Page 133

Problem number: 31.

ODE order: 1. ODE degree: 1.

CAS Maple gives this as type [[_homogeneous, 'class G'], _rational, [_Abel, '2nd type', 'class G'],

$$y' - \frac{-3x^2y - y^2}{2x^3 + 3yx} = 0$$

With initial conditions

$$[y(1) = -2]$$

✓ Solution by Maple

Time used: 1.281 (sec). Leaf size: 111

 $dsolve([diff(y(x),x) = (-3*x^2*y(x)-y(x)^2)/(2*x^3+3*x*y(x)),y(1) = -2],y(x), singsol=all)$

$$=\frac{\left(i\sqrt{3}-1\right) \left(-\left(x^{7}-6\sqrt{3}\sqrt{x^{7}+27}+54\right) x^{2}\right)^{\frac{2}{3}}-x^{3} \left(ix^{3}\sqrt{3}+x^{3}+2 \left(-\left(x^{7}-6\sqrt{3}\sqrt{x^{7}+27}+54\right) x^{2}\right)^{\frac{1}{3}}\right)}{6 \left(-\left(x^{7}-6\sqrt{3}\sqrt{x^{7}+27}+54\right) x^{2}\right)^{\frac{1}{3}} x}$$

✓ Solution by Mathematica

Time used: 42.543 (sec). Leaf size: 116

$$y(x) = i \left(2ix^{3} + (\sqrt{3} + i) \sqrt[3]{6\sqrt{3}\sqrt{x^{4}(x^{7} + 27)} - x^{2}(x^{7} + 54)} - \frac{(\sqrt{3} - i)x^{6}}{\sqrt[3]{6\sqrt{3}\sqrt{x^{4}(x^{7} + 27)} - x^{2}(x^{7} + 54)}} \right) = \frac{i}{6x}$$

7 Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

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7.1 problem 1

Internal problem ID [599]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

Problem number: 1.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 2y' - 3y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

dsolve(diff(y(x),x\$2) +2*diff(y(x),x)-3*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 \mathrm{e}^{-3x} + \mathrm{e}^x c_2$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 20

DSolve[y''[x]+2*y'[x]-3*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to c_1 e^{-3x} + c_2 e^x$$

7.2 problem 2

Internal problem ID [600]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

Problem number: 2.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 3y' + 2y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

dsolve(diff(y(x),x\$2) +3*diff(y(x),x)+2*y(x) = 0,y(x), singsol=all)

$$y(x) = e^{-x}c_1 + c_2e^{-2x}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 20

DSolve[y''[x]+3*y'[x]+2*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-2x}(c_2 e^x + c_1)$$

7.3 problem 3

Internal problem ID [601]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

Problem number: 3.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$6y'' - y' - y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

dsolve(6*diff(y(x),x\$2) -diff(y(x),x)-y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-\frac{x}{3}} + c_2 e^{\frac{x}{2}}$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 26

DSolve[6*y''[x]-y'[x]-y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-x/3} (c_2 e^{5x/6} + c_1)$$

7.4 problem 4

Internal problem ID [602]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section:}\ {\bf Chapter}\ {\bf 3},\ {\bf Second}\ {\bf order}\ {\bf linear}\ {\bf equations},\ {\bf 3.1}\ {\bf Homogeneous}\ {\bf Equations}\ {\bf with}\ {\bf Constant}$

Coefficients, page 144 **Problem number**: 4.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$2y'' - 3y' + y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

dsolve(2*diff(y(x),x\$2) -3*diff(y(x),x)+y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{\frac{x}{2}} + e^x c_2$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 35

DSolve[y''[x]-3*y'[x]+y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \rightarrow e^{-\frac{1}{2}\left(\sqrt{5}-3\right)x}\left(c_2e^{\sqrt{5}x}+c_1\right)$$

7.5 problem 5

Internal problem ID [603]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

Problem number: 5.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 5y' = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 12

dsolve(diff(y(x),x\$2) +5*diff(y(x),x) = 0,y(x), singsol=all)

$$y(x) = c_1 + c_2 e^{-5x}$$

✓ Solution by Mathematica

Time used: 0.009 (sec). Leaf size: 19

DSolve[y''[x]+5*y'[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to c_2 - \frac{1}{5}c_1e^{-5x}$$

7.6 problem 6

Internal problem ID [604]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

Problem number: 6.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$4y'' - 9y = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 17

dsolve(4*diff(y(x),x\$2) -9*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-\frac{3x}{2}} + c_2 e^{\frac{3x}{2}}$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 24

DSolve[4*y''[x]-9*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-3x/2} (c_1 e^{3x} + c_2)$$

7.7 problem 7

Internal problem ID [605]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

Problem number: 7.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - 9y' + 9y = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 27

dsolve(diff(y(x),x\$2) -9*diff(y(x),x)+9*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{\frac{3(3+\sqrt{5})x}{2}} + c_2 e^{-\frac{3(\sqrt{5}-3)x}{2}}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 36

DSolve[y''[x]-9*y'[x]+9*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-\frac{3}{2}(\sqrt{5}-3)x} \left(c_2 e^{3\sqrt{5}x} + c_1\right)$$

7.8 problem 8

Internal problem ID [606]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

Problem number: 8.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - 2y' - 2y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 26

dsolve(diff(y(x),x\$2) -2*diff(y(x),x)-2*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{(1+\sqrt{3})x} + c_2 e^{-(\sqrt{3}-1)x}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 34

DSolve[y''[x]-2*y'[x]-2*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \rightarrow e^{x-\sqrt{3}x} \left(c_2 e^{2\sqrt{3}x} + c_1\right)$$

7.9 problem 9

Internal problem ID [607]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} \hbox{: } {\bf Chapter \ 3, \ Second \ order \ linear \ equations, \ 3.1 \ Homogeneous \ Equations \ with \ Constant}$

Coefficients, page 144 **Problem number:** 9.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + y' - 2y = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 16

dsolve([diff(y(x),x\$2) + diff(y(x),x)-2*y(x) = 0,y(0) = 0, D(y)(0) = 1],y(x), singsol=all)

$$y(x) = \frac{(e^{3x} - 1)e^{-2x}}{3}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 21

 $DSolve[\{y''[x]+y'[x]-2*y[x]==0,\{y[0]==0,y'[0]==1\}\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{1}{3}e^{-2x}(e^{3x} - 1)$$

7.10 problem 10

Internal problem ID [608]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant

Coefficients, page 144 **Problem number**: 10.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 4y' + 3y = 0$$

With initial conditions

$$[y(0) = 2, y'(0) = -1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 17

dsolve([diff(y(x),x\$2) +4*diff(y(x),x)+3*y(x) = 0,y(0) = 2, D(y)(0) = -1],y(x), singsol=all)

$$y(x) = \frac{5e^{-x}}{2} - \frac{e^{-3x}}{2}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 23

DSolve[$\{y''[x]+4*y'[x]+3*y[x]==0,\{y[0]==2,y'[0]==-1\}\},y[x],x,IncludeSingularSolutions -> True$

$$y(x) \to \frac{1}{2}e^{-3x}(5e^{2x} - 1)$$

7.11 problem 11

Internal problem ID [609]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant

Coefficients, page 144

Problem number: 11.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$6y'' - 5y' + y = 0$$

With initial conditions

$$[y(0) = 4, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 17

dsolve([6*diff(y(x),x\$2) -5*diff(y(x),x)+y(x) = 0,y(0) = 4, D(y)(0) = 0],y(x), singsol=all)

$$y(x) = -8e^{\frac{x}{2}} + 12e^{\frac{x}{3}}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 48

$$y(x) o rac{4}{23}e^{5x/12} \Biggl(23\cos\left(rac{\sqrt{23}x}{12}
ight) - 5\sqrt{23}\sin\left(rac{\sqrt{23}x}{12}
ight) \Biggr)$$

7.12 problem 12

Internal problem ID [610]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section:}\ {\bf Chapter}\ 3,\ {\bf Second}\ {\bf order}\ {\bf linear}\ {\bf equations},\ 3.1\ {\bf Homogeneous}\ {\bf Equations}\ {\bf with}\ {\bf Constant}$

Coefficients, page 144

Problem number: 12.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 3y' = 0$$

With initial conditions

$$[y(0) = -2, y'(0) = 3]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 12

dsolve([diff(y(x),x\$2) +3*diff(y(x),x) = 0,y(0) = -2, D(y)(0) = 3],y(x), singsol=all)

$$y(x) = -1 - e^{-3x}$$

✓ Solution by Mathematica

Time used: 0.014 (sec). Leaf size: 14

$$y(x) \to -e^{-3x} - 1$$

7.13 problem 13

Internal problem ID [611]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

Problem number: 13.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 5y' + 3y = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.422 (sec). Leaf size: 39

dsolve([diff(y(x),x\$2) +5*diff(y(x),x)+3*y(x) = 0,y(0) = 1, D(y)(0) = 0],y(x), singsol=all)

$$y(x) = \frac{\left(5\sqrt{13} + 13\right)e^{\frac{\left(-5+\sqrt{13}\right)x}{2}}}{26} + \frac{\left(-5\sqrt{13} + 13\right)e^{-\frac{\left(5+\sqrt{13}\right)x}{2}}}{26}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 51

DSolve[{y''[x]+5*y'[x]+3*y[x]==0,{y[0]==1,y'[0]==0}},y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to \frac{1}{26} e^{-\frac{1}{2}(5+\sqrt{13})x} \left(\left(13+5\sqrt{13}\right) e^{\sqrt{13}x} + 13 - 5\sqrt{13} \right)$$

7.14 problem 14

Internal problem ID [612]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section:}\ {\bf Chapter}\ 3,\ {\bf Second}\ {\bf order}\ {\bf linear}\ {\bf equations},\ 3.1\ {\bf Homogeneous}\ {\bf Equations}\ {\bf with}\ {\bf Constant}$

Coefficients, page 144 **Problem number**: 14.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$2y'' + y' - 4y = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

✓ Solution by Maple

Time used: 0.062 (sec). Leaf size: 30

dsolve([2*diff(y(x),x\$2) + diff(y(x),x)-4*y(x) = 0,y(0) = 0, D(y)(0) = 1],y(x), singsol=all)

$$y(x) = -\frac{2\left(-e^{\frac{\left(-1+\sqrt{33}\right)x}{4}} + e^{-\frac{\left(1+\sqrt{33}\right)x}{4}}\right)\sqrt{33}}{33}$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 30

DSolve[{2*y''[x]+y'[x]-4*y[x]==0,{y[0]==0,y'[0]==1}},y[x],x,IncludeSingularSolutions -> True]

$$y(x) o rac{4e^{-x/4}\sinh\left(rac{\sqrt{33}x}{4}
ight)}{\sqrt{33}}$$

7.15 problem 15

Internal problem ID [613]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section:}\ {\bf Chapter}\ 3,\ {\bf Second}\ {\bf order}\ {\bf linear}\ {\bf equations},\ 3.1\ {\bf Homogeneous}\ {\bf Equations}\ {\bf with}\ {\bf Constant}$

Coefficients, page 144 **Problem number**: 15.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 8y' - 9y = 0$$

With initial conditions

$$[y(1) = 1, y'(1) = 0]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 19

dsolve([diff(y(x),x\$2) +8*diff(y(x),x)-9*y(x) = 0,y(1) = 1, D(y)(1) = 0],y(x), singsol=all)

$$y(x) = \frac{e^{9-9x}}{10} + \frac{9e^{x-1}}{10}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 26

DSolve[{y''[x]+8*y'[x]-9*y[x]==0,{y[1]==1,y'[1]==0}},y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to \frac{1}{10}e^{9-9x} + \frac{9e^{x-1}}{10}$$

7.16 problem 16

Internal problem ID [614]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

Problem number: 16.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$4y'' - y = 0$$

With initial conditions

$$[y(-2) = 1, y'(-2) = -1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 21

dsolve([4*diff(y(x),x\$2) -y(x) = 0,y(-2) = 1, D(y)(-2) = -1],y(x), singsol=all)

$$y(x) = -\frac{e^{1+\frac{x}{2}}}{2} + \frac{3e^{-1-\frac{x}{2}}}{2}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 24

 $DSolve[\{4*y''[x]-y[x]==0,\{y[-2]==1,y'[-2]==-1\}\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \cosh\left(\frac{x+2}{2}\right) - 2\sinh\left(\frac{x+2}{2}\right)$$

7.17 problem 19

Internal problem ID [615]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

Problem number: 19.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - y = 0$$

With initial conditions

$$y(0) = \frac{5}{4}, y'(0) = -\frac{3}{4}$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 13

dsolve([diff(y(x),x\$2) -y(x) = 0,y(0) = 5/4, D(y)(0) = -3/4],y(x), singsol=all)

$$y(x) = e^{-x} + \frac{e^x}{4}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 18

 $DSolve[\{y''[x]-y[x]==0,\{y[0]==5/4,y'[0]==-3/4\}\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to e^{-x} + \frac{e^x}{4}$$

7.18 problem 20

Internal problem ID [616]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section:}\ {\bf Chapter}\ 3,\ {\bf Second}\ {\bf order}\ {\bf linear}\ {\bf equations},\ 3.1\ {\bf Homogeneous}\ {\bf Equations}\ {\bf with}\ {\bf Constant}$

Coefficients, page 144

Problem number: 20.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$2y'' - 3y' + y = 0$$

With initial conditions

$$y(0) = 2, y'(0) = \frac{1}{2}$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 15

dsolve([2*diff(y(x),x\$2) -3*diff(y(x),x)+y(x) = 0,y(0) = 2, D(y)(0) = 1/2],y(x), singsol=all)

$$y(x) = 3e^{\frac{x}{2}} - e^x$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 20

$$y(x) \to 3e^{x/2} - e^x$$

7.19 problem 21

Internal problem ID [617]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

Problem number: 21.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - y' - 2y = 0$$

With initial conditions

$$[y(0) = \alpha, y'(0) = 2]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 25

dsolve([diff(y(x),x\$2) - diff(y(x),x)-2*y(x) = 0,y(0) = alpha, D(y)(0) = 2],y(x), singsol=all)

$$y(x) = \frac{(2\alpha - 2)e^{-x}}{3} + \frac{e^{2x}(\alpha + 2)}{3}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 29

$$y(x) \to \frac{1}{3}e^{-x}(2(\alpha - 1) + (\alpha + 2)e^{3x})$$

7.20 problem 22

Internal problem ID [618]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section:}\ {\bf Chapter}\ 3,\ {\bf Second}\ {\bf order}\ {\bf linear}\ {\bf equations},\ 3.1\ {\bf Homogeneous}\ {\bf Equations}\ {\bf with}\ {\bf Constant}$

Coefficients, page 144 **Problem number**: 22.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$4y'' - y = 0$$

With initial conditions

$$[y(0) = 2, y'(0) = \beta]$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 22

dsolve([4*diff(y(x),x\$2) -y(x) = 0,y(0) = 2, D(y)(0) = beta],y(x), singsol=all)

$$y(x) = (1+\beta) e^{\frac{x}{2}} - (\beta - 1) e^{-\frac{x}{2}}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 22

DSolve[{4*y''[x]-y[x]==0,{y[0]==2,y'[0]==\[Beta]}},y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to 2\left(\beta \sinh\left(\frac{x}{2}\right) + \cosh\left(\frac{x}{2}\right)\right)$$

7.21 problem 23

Internal problem ID [619]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant

Coefficients, page 144

Problem number: 23.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - (2\alpha - 1)y' + \alpha(\alpha - 1)y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 19

dsolve(diff(y(x),x\$2) - (2*alpha-1)*diff(y(x),x)+alpha*(alpha-1)*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{\alpha x} + c_2 e^{(\alpha - 1)x}$$

Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 24

$$y(x) \rightarrow c_1 e^{(\alpha-1)x} + c_2 e^{\alpha x}$$

7.22 problem 24

Internal problem ID [620]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant

Coefficients, page 144 **Problem number**: 24.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + (3 - \alpha)y' - 2(\alpha - 1)y = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 19

dsolve(diff(y(x),x\$2) + (3-alpha)*diff(y(x),x)-2*(alpha-1)*y(x) = 0,y(x), singsol=all)

$$y(x) = e^{-2x}c_1 + c_2e^{(\alpha - 1)x}$$

Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 24

 $DSolve[y''[x]+(3-\[Alpha])*y'[x]-2*(\[Alpha]-1)*y[x]==0,y[x],x,IncludeSingularSolutions -> Track Tr$

$$y(x) \rightarrow e^{-2x} \left(c_1 e^{\alpha x + x} + c_2 \right)$$

7.23 problem 25

Internal problem ID [621]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.1 Homogeneous Equations with Constant Coefficients, page 144

Problem number: 25.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$2y'' + 3y' - 2y = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = -\beta]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 28

dsolve([2*diff(y(x),x\$2) +3*diff(y(x),x)-2*y(x) = 0,y(0) = 1, D(y)(0) = -beta],y(x), singsol=

$$y(x) = -\frac{\left(2e^{\frac{5x}{2}}\beta - 4e^{\frac{5x}{2}} - 2\beta - 1\right)e^{-2x}}{5}$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 67

$$y(x) \to \frac{1}{34} e^{-\frac{1}{2} \left(3 + \sqrt{17}\right)x} \left(2\sqrt{17}\beta + \left(-2\sqrt{17}\beta + 3\sqrt{17} + 17\right)e^{\sqrt{17}x} - 3\sqrt{17} + 17\right)$$

7.24 problem 26

Internal problem ID [622]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section:}\ {\bf Chapter}\ 3,\ {\bf Second}\ {\bf order}\ {\bf linear}\ {\bf equations},\ 3.1\ {\bf Homogeneous}\ {\bf Equations}\ {\bf with}\ {\bf Constant}$

Coefficients, page 144

Problem number: 26.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 5y' + 6y = 0$$

With initial conditions

$$[y(0) = 2, y'(0) = \beta]$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 23

dsolve([diff(y(x),x\$2) +5*diff(y(x),x)+6*y(x) = 0,y(0) = 2, D(y)(0) = beta],y(x), singsol=all

$$y(x) = e^{-2x}(6+\beta) + (-\beta - 4)e^{-3x}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 23

$$y(x) \to e^{-3x}(-\beta + (\beta + 6)e^x - 4)$$

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8.1 problem 7

Internal problem ID [623]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 7.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - 2y' + 2y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

dsolve(diff(y(x),x\$2) -2*diff(y(x),x)+2*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 \sin(x) e^x + c_2 \cos(x) e^x$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 20

DSolve[y''[x]-2*y'[x]+2*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \rightarrow e^x(c_2\cos(x) + c_1\sin(x))$$

8.2 problem 8

Internal problem ID [624]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 8.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - 2y' + 6y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 25

dsolve(diff(y(x),x\$2) -2*diff(y(x),x)+6*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^x \sin\left(\sqrt{5}x\right) + c_2 e^x \cos\left(\sqrt{5}x\right)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 32

DSolve[y''[x]-2*y'[x]+6*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^x \Big(c_2 \cos \Big(\sqrt{5}x \Big) + c_1 \sin \Big(\sqrt{5}x \Big) \Big)$$

8.3 problem 9

Internal problem ID [625]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} \hbox{: } {\bf Chapter \ 3, \ Second \ order \ linear \ equations, \ 3.3 \ Complex \ Roots \ of \ the \ Characteristic}$

Equation, page 164 Problem number: 9.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 2y' - 8y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

dsolve(diff(y(x),x\$2) +2*diff(y(x),x)-8*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-4x} + c_2 e^{2x}$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 22

DSolve[y''[x]+2*y'[x]-8*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-4x} (c_2 e^{6x} + c_1)$$

8.4 problem 10

Internal problem ID [626]

 $\mathbf{Book} \text{: } \mathbf{Elementary \ differential \ equations \ and \ boundary \ value \ problems, \ 10th \ ed., \ Boyce \ and }$

DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic

Equation , page 164

Problem number: 10.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 2y' + 2y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 21

dsolve(diff(y(x),x\$2) +2*diff(y(x),x)+2*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-x} \sin(x) + c_2 e^{-x} \cos(x)$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 22

DSolve[y''[x]+2*y'[x]+2*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-x}(c_2 \cos(x) + c_1 \sin(x))$$

8.5 problem 11

Internal problem ID [627]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic

Equation , page 164

Problem number: 11.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 6y' + 13y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 25

dsolve(diff(y(x),x\$2) +6*diff(y(x),x)+13*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-3x} \sin(2x) + c_2 e^{-3x} \cos(2x)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 26

DSolve[y''[x]+6*y'[x]+13*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-3x}(c_2\cos(2x) + c_1\sin(2x))$$

8.6 problem 12

Internal problem ID [628]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 12.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$4y'' + 9y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

dsolve(4*diff(y(x),x\$2) +9*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 \sin\left(\frac{3x}{2}\right) + c_2 \cos\left(\frac{3x}{2}\right)$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 20

DSolve[y''[x]+9*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to c_1 \cos(3x) + c_2 \sin(3x)$$

8.7 problem 13

Internal problem ID [629]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic

Equation, page 164 Problem number: 13.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 2y' + \frac{5y}{4} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 25

dsolve(diff(y(x),x\$2) +2*diff(y(x),x)+125/100*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-x} \sin\left(\frac{x}{2}\right) + c_2 e^{-x} \cos\left(\frac{x}{2}\right)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 30

 $DSolve[y''[x]+2*y'[x]+125/100*y[x]==0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) o e^{-x} \Big(c_2 \cos \Big(rac{x}{2} \Big) + c_1 \sin \Big(rac{x}{2} \Big) \Big)$$

8.8 problem 14

Internal problem ID [630]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic

Equation , page 164

Problem number: 14.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$9y'' + 9y' - 4y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

dsolve(9*diff(y(x),x\$2) + 9*diff(y(x),x) - 4*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-\frac{4x}{3}} + c_2 e^{\frac{x}{3}}$$

Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 26

DSolve [9*y''[x]+9*y'[x]-4*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-4x/3} (c_2 e^{5x/3} + c_1)$$

8.9 problem 15

Internal problem ID [631]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 15.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + y' + \frac{5y}{4} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 21

dsolve(diff(y(x),x\$2) + diff(y(x),x) + 125/100*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-\frac{x}{2}} \sin(x) + c_2 e^{-\frac{x}{2}} \cos(x)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 24

 $DSolve[y''[x]+y'[x]+125/100*y[x]==0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to e^{-x/2}(c_2\cos(x) + c_1\sin(x))$$

8.10 problem 16

Internal problem ID [632]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 16.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 4y' + \frac{25y}{4} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 25

dsolve(diff(y(x),x\$2) + 4*diff(y(x),x)+625/100*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-2x} \sin\left(\frac{3x}{2}\right) + c_2 e^{-2x} \cos\left(\frac{3x}{2}\right)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 30

DSolve[y''[x]+4*y'[x]+625/100*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-2x} \left(c_2 \cos \left(\frac{3x}{2} \right) + c_1 \sin \left(\frac{3x}{2} \right) \right)$$

8.11 problem 17

Internal problem ID [633]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} \hbox{: } {\bf Chapter \ 3, \ Second \ order \ linear \ equations, \ 3.3 \ Complex \ Roots \ of \ the \ Characteristic}$

Equation , page 164

Problem number: 17.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 4y = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 10

dsolve([diff(y(x),x\$2)+ 4*y(x) = 0,y(0) = 0, D(y)(0) = 1],y(x), singsol=all)

$$y(x) = \frac{\sin(2x)}{2}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 10

 $DSolve[\{y''[x]+4*y[x]==0,\{y[0]==0,y'[0]==1\}\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \sin(x)\cos(x)$$

8.12 problem 18

Internal problem ID [634]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic

Equation , page 164

Problem number: 18.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 4y' + 5y = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 16

$$y(x) = e^{-2x}(2\sin(x) + \cos(x))$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 18

DSolve[$\{y''[x]+4*y'[x]+5*y[x]==0,\{y[0]==1,y'[0]==0\}\},y[x],x,IncludeSingularSolutions -> True$]

$$y(x) \to e^{-2x}(2\sin(x) + \cos(x))$$

8.13 problem 19

Internal problem ID [635]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic

Equation , page 164

Problem number: 19.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - 2y' + 5y = 0$$

With initial conditions

$$\left[y\left(\frac{\pi}{2}\right) = 0, y'\left(\frac{\pi}{2}\right) = 2\right]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 16

$$y(x) = -\sin(2x) e^{-\frac{\pi}{2} + x}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 20

DSolve[{y''[x]-2*y'[x]+5*y[x]==0,{y[Pi/2]==0,y'[Pi/2]==2}},y[x],x,IncludeSingularSolutions ->

$$y(x) \rightarrow -e^{x-\frac{\pi}{2}}\sin(2x)$$

8.14 problem 20

Internal problem ID [636]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 20.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + y = 0$$

With initial conditions

$$\left[y\left(\frac{\pi}{3}\right) = 2, y'\left(\frac{\pi}{3}\right) = -4\right]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 23

dsolve([diff(y(x),x\$2)+y(x) = 0,y(1/3*Pi) = 2, D(y)(1/3*Pi) = -4],y(x), singsol=all)

$$y(x) = (\sin(x) + 2\cos(x))\sqrt{3} + \cos(x) - 2\sin(x)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 28

 $DSolve[\{y''[x]+y[x]==0,\{y[Pi/3]==2,y'[Pi/3]==-4\}\},y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \rightarrow \left(\sqrt{3} - 2\right)\sin(x) + \left(1 + 2\sqrt{3}\right)\cos(x)$$

8.15 problem 21

Internal problem ID [637]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic

Equation , page 164

Problem number: 21.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + y' + \frac{5y}{4} = 0$$

With initial conditions

$$[y(0) = 3, y'(0) = 1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 19

$$y(x) = \frac{e^{-\frac{x}{2}}(5\sin(x) + 6\cos(x))}{2}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 25

 $DSolve[\{y''[x]+y'[x]+125/100*y[x]==0,\{y[0]==3,y'[0]==1\}\},y[x],x,IncludeSingularSolutions \rightarrow T \}$

$$y(x) \to \frac{1}{2}e^{-x/2}(5\sin(x) + 6\cos(x))$$

8.16 problem 22

Internal problem ID [638]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section:}\ {\bf Chapter}\ 3,\ {\bf Second}\ {\bf order}\ {\bf linear}\ {\bf equations},\ 3.3\ {\bf Complex}\ {\bf Roots}\ {\bf of}\ {\bf the}\ {\bf Characteristic}$

Equation , page 164

Problem number: 22.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 2y' + 2y = 0$$

With initial conditions

$$\left[y\left(\frac{\pi}{4}\right) = 2, y'\left(\frac{\pi}{4}\right) = -2\right]$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 21

 $dsolve([diff(y(x),x\$2)+\ 2*diff(y(x),x)+2*y(x)=0,y(1/4*Pi)=2,\ D(y)(1/4*Pi)=-2],y(x),\ sin(x)=0$

$$y(x) = \sqrt{2} e^{-x + \frac{\pi}{4}} (\cos(x) + \sin(x))$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 27

DSolve[{y''[x]+2*y'[x]+2*y[x]==0,{y[Pi/4]==2,y'[Pi/4]==-2}},y[x],x,IncludeSingularSolutions -

$$y(x) \to \sqrt{2}e^{\frac{\pi}{4} - x}(\sin(x) + \cos(x))$$

8.17 problem 23

Internal problem ID [639]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic

Equation , page 164

Problem number: 23.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$u'' - u' + 2u = 0$$

With initial conditions

$$[u(0) = 2, u'(0) = 0]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 31

 $dsolve([diff(u(x),x\$2)-diff(u(x),x)+2*u(x)=0,u(0)=2,\ D(u)(0)=0],u(x),\ singsol=all)$

$$u(x) = -\frac{2e^{\frac{x}{2}}\left(\sqrt{7}\sin\left(\frac{\sqrt{7}x}{2}\right) - 7\cos\left(\frac{\sqrt{7}x}{2}\right)\right)}{7}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 19

DSolve[{u''[x]+4*u'[x]+5*u[x]==0,{u[0]==2,u'[0]==0}},u[x],x,IncludeSingularSolutions -> True]

$$u(x) \to 2e^{-2x}(2\sin(x) + \cos(x))$$

8.18 problem 24

Internal problem ID [640]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 24.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$5u'' + 2u' + 7u = 0$$

With initial conditions

$$[u(0) = 2, u'(0) = 1]$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 32

dsolve([5*diff(u(x),x\$2)+ 2*diff(u(x),x)+7*u(x) = 0,u(0) = 2, D(u)(0) = 1],u(x), singsol=all)

$$u(x) = \frac{e^{-\frac{x}{5}} \left(7\sqrt{34} \sin\left(\frac{\sqrt{34}x}{5}\right) + 68\cos\left(\frac{\sqrt{34}x}{5}\right)\right)}{34}$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 48

DSolve[{5*u''[x]+2*u'[x]+7*u[x]==0,{u[0]==2,u'[0]==1}},u[x],x,IncludeSingularSolutions -> Tru

$$u(x) \rightarrow \frac{1}{34}e^{-x/5} \left(7\sqrt{34}\sin\left(\frac{\sqrt{34}x}{5}\right) + 68\cos\left(\frac{\sqrt{34}x}{5}\right)\right)$$

8.19 problem 25

Internal problem ID [641]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 25.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 2y' + 6y = 0$$

With initial conditions

$$[y(0) = 2, y'(0) = \alpha]$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 32

$$y(x) = \frac{\left(\sqrt{5}\left(\alpha + 2\right)\sin\left(\sqrt{5}x\right) + 10\cos\left(\sqrt{5}x\right)\right)e^{-x}}{5}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 42

$$y(x) \to \frac{1}{5}e^{-x} \left(\sqrt{5}(\alpha+2)\sin\left(\sqrt{5}x\right) + 10\cos\left(\sqrt{5}x\right)\right)$$

8.20 problem 26

Internal problem ID [642]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section:}\ {\bf Chapter}\ 3,\ {\bf Second}\ {\bf order}\ {\bf linear}\ {\bf equations},\ 3.3\ {\bf Complex}\ {\bf Roots}\ {\bf of}\ {\bf the}\ {\bf Characteristic}$

Equation , page 164

Problem number: 26.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 2ay' + (a^2 + 1) y = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 17

 $dsolve([diff(y(x),x$2)+ 2*a*diff(y(x),x)+(a^2+1)*y(x) = 0,y(0) = 1, D(y)(0) = 0],y(x), singso$

$$y(x) = e^{-ax}(a\sin(x) + \cos(x))$$

✓ Solution by Mathematica

Time used: 0.01 (sec). Leaf size: 54

 $DSolve[\{y''[x]+2*a*y'[x]+(a^1+1)*y[x]==0,\{y[0]==1,y'[0]==0\}\},y[x],x,IncludeSingularSolutions]$

$$y(x) \to e^{-ax} \left(\frac{a \sinh\left(\sqrt{(a-1)a-1}x\right)}{\sqrt{(a-1)a-1}} + \cosh\left(\sqrt{(a-1)a-1}x\right) \right)$$

8.21 problem 35

Internal problem ID [643]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic

Equation , page 164

Problem number: 35.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler], [_2nd_order, _linear, '_with_symmetry_[0,F(

$$t^2y'' + ty' + y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

 $dsolve(t^2*diff(y(t),t^2)+t*diff(y(t),t)+y(t) = 0,y(t), singsol=all)$

$$y(t) = c_1 \sin \left(\ln \left(t\right)\right) + c_2 \cos \left(\ln \left(t\right)\right)$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 18

DSolve[t^2*y''[t]+t*y'[t]+y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow c_1 \cos(\log(t)) + c_2 \sin(\log(t))$$

8.22 problem 36

Internal problem ID [644]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 36.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _homogeneous]]

$$t^2y'' + 4ty' + 2y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

 $dsolve(t^2*diff(y(t),t^2)+ 4*t*diff(y(t),t)+2*y(t) = 0,y(t), singsol=all)$

$$y(t) = \frac{c_1}{t} + \frac{c_2}{t^2}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 34

DSolve[t^2*y''[t]+4*t*y'[t]+y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) o t^{-\frac{3}{2} - \frac{\sqrt{5}}{2}} \Big(c_2 t^{\sqrt{5}} + c_1 \Big)$$

8.23 problem 37

Internal problem ID [645]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 37.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$t^2y'' + 3ty' + \frac{5y}{4} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 25

 $dsolve(t^2*diff(y(t),t)^2) + 3*t*diff(y(t),t) + 125/100*y(t) = 0,y(t), singsol=all)$

$$y(t) = rac{c_1 \sin\left(rac{\ln(t)}{2}
ight)}{t} + rac{c_2 \cos\left(rac{\ln(t)}{2}
ight)}{t}$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 30

 $DSolve[t^2*y''[t]+3*t*y'[t]+125/100*y[t]==0,y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) o rac{c_2 \cos\left(\frac{\log(t)}{2}\right) + c_1 \sin\left(\frac{\log(t)}{2}\right)}{t}$$

8.24 problem 38

Internal problem ID [646]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 38.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _homogeneous]]

$$t^2y'' - 4ty' - 6y = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 15

 $dsolve(t^2*diff(y(t),t^2)-4*t*diff(y(t),t)-6*y(t) = 0,y(t), singsol=all)$

$$y(t) = \frac{c_1}{t} + c_2 t^6$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 18

DSolve[t^2*y''[t]-4*t*y'[t]-6*y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{c_2 t^7 + c_1}{t}$$

8.25 problem 39

Internal problem ID [647]

 \mathbf{Book} : Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic

Equation , page 164

Problem number: 39.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler], [_2nd_order, _linear, '_with_symmetry_[0,F(

$$t^2y'' - 4ty' + 6y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

 $dsolve(t^2*diff(y(t),t^2)-4*t*diff(y(t),t)+6*y(t) = 0,y(t), singsol=all)$

$$y(t) = c_1 t^3 + c_2 t^2$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 16

 $DSolve[t^2*y''[t]-4*t*y'[t]+6*y[t]==0,y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \to t^2(c_2t + c_1)$$

8.26 problem 40

Internal problem ID [648]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 40.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$t^2y'' - ty' + 5y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 21

 $dsolve(t^2*diff(y(t),t^2)-t*diff(y(t),t)+5*y(t) = 0,y(t), singsol=all)$

$$y(t) = c_1 t \sin(2 \ln(t)) + c_2 t \cos(2 \ln(t))$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 24

DSolve[t^2*y''[t]-t*y'[t]+5*y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow t(c_2 \cos(2\log(t)) + c_1 \sin(2\log(t)))$$

8.27 problem 41

Internal problem ID [649]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 41.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$t^2y'' + 3ty' - 3y = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 13

 $dsolve(t^2*diff(y(t),t^2)+ 3*t*diff(y(t),t)-3*y(t) = 0,y(t), singsol=all)$

$$y(t) = \frac{c_1}{t^3} + c_2 t$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 16

DSolve[t^2*y''[t]+3*t*y'[t]-3*y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{c_1}{t^3} + c_2 t$$

8.28 problem 42

Internal problem ID [650]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 42.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$t^2y'' + 7ty' + 10y = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 21

 $dsolve(t^2*diff(y(t),t)^2) + 7*t*diff(y(t),t)^2) = 0,y(t), singsol=all)$

$$y(t) = \frac{c_1 \sin(\ln(t))}{t^3} + \frac{c_2 \cos(\ln(t))}{t^3}$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 22

DSolve[t^2*y''[t]+7*t*y'[t]+10*y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow \frac{c_2 \cos(\log(t)) + c_1 \sin(\log(t))}{t^3}$$

8.29 problem 44

Internal problem ID [651]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 44.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries], [_2nd_order, _linear, '

$$y'' + ty' + e^{-t^2}y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 65

 $dsolve(diff(y(t),t$2)+ t*diff(y(t),t)+exp(-t^2)*y(t) = 0,y(t), singsol=all)$

$$y(t) = c_1 \sin\left(\frac{\sqrt{2} e^{\frac{t^2}{2}} \sqrt{\pi} \operatorname{erf}\left(\frac{t\sqrt{2}}{2}\right)}{2\sqrt{e^{t^2}}}\right) + c_2 \cos\left(\frac{\sqrt{2} e^{\frac{t^2}{2}} \sqrt{\pi} \operatorname{erf}\left(\frac{t\sqrt{2}}{2}\right)}{2\sqrt{e^{t^2}}}\right)$$

✓ Solution by Mathematica

Time used: 0.012 (sec). Leaf size: 102

 $DSolve[y''[t]+t*y'[t]+exp(-t^2)*y[t]==0,y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \rightarrow e^{-\frac{1}{4}(\sqrt{4\exp+1}+1)t^2} \left(c_1 \operatorname{HermiteH} \left(-\frac{1}{2} - \frac{1}{2\sqrt{4\exp+1}}, \frac{\sqrt[4]{4\exp+1}t}{\sqrt{2}} \right) + c_2 \operatorname{Hypergeometric1F1} \left(\frac{1}{4} \left(1 + \frac{1}{\sqrt{4\exp+1}} \right), \frac{1}{2}, \frac{1}{2} \sqrt{4\exp+1}t^2 \right) \right)$$

8.30 problem 46

Internal problem ID [652]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.3 Complex Roots of the Characteristic Equation , page 164

Problem number: 46.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$ty'' + (t^2 - 1)y' + yt^3 = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 39

 $dsolve(t*diff(y(t),t$2)+ (t^2-1)*diff(y(t),t)+t^3*y(t) = 0,y(t), singsol=all)$

$$y(t) = c_1 e^{-\frac{t^2}{4}} \cos\left(\frac{t^2\sqrt{3}}{4}\right) + c_2 e^{-\frac{t^2}{4}} \sin\left(\frac{t^2\sqrt{3}}{4}\right)$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 48

 $DSolve[t*y''[t]+(t^2-1)*y'[t]+t^3*y[t] == 0, y[t], t, IncludeSingularSolutions \rightarrow True]$

$$y(t)
ightarrow e^{-rac{t^2}{4}} \Biggl(c_2 \cos \left(rac{\sqrt{3}t^2}{4}
ight) + c_1 \sin \left(rac{\sqrt{3}t^2}{4}
ight) \Biggr)$$

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9.1 problem 1

Internal problem ID [653]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 1.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - 2y' + y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 14

dsolve(diff(y(x),x\$2)-2*diff(y(x),x)+y(x) = 0,y(x), singsol=all)

$$y(x) = e^x c_1 + c_2 e^x x$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 16

DSolve[y''[x]-2*y'[x]+y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \rightarrow e^x(c_2x + c_1)$$

9.2 problem 2

Internal problem ID [654]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 2.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$9y'' + 6y' + y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 18

dsolve(9*diff(y(x),x\$2)+6*diff(y(x),x)+y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-\frac{x}{3}} + c_2 e^{-\frac{x}{3}} x$$

Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 20

DSolve[9*y''[x]+6*y'[x]+y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-x/3}(c_2x + c_1)$$

9.3 problem 3

Internal problem ID [655]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 3.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$4y'' - 4y' - 3y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

dsolve(4*diff(y(x),x\$2)-4*diff(y(x),x)-3*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{\frac{3x}{2}} + c_2 e^{-\frac{x}{2}}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 24

DSolve[4*y''[x]-4*y'[x]-3*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-x/2} (c_2 e^{2x} + c_1)$$

9.4 problem 4

Internal problem ID [656]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 4.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$4y'' + 12y' + 9y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 18

dsolve(4*diff(y(x),x\$2)+12*diff(y(x),x)+9*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-\frac{3x}{2}} + c_2 e^{-\frac{3x}{2}} x$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 20

 $DSolve[4*y''[x]+12*y'[x]+9*y[x]==0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to e^{-3x/2}(c_2x + c_1)$$

9.5 problem 5

Internal problem ID [657]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${f Section}$: Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 5.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - 2y' + 10y = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 21

dsolve(diff(y(x),x\$2)-2*diff(y(x),x)+10*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^x \sin(3x) + c_2 e^x \cos(3x)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 24

 $DSolve[y''[x]-2*y'[x]+10*y[x]==0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to e^x(c_2\cos(3x) + c_1\sin(3x))$$

9.6 problem 6

Internal problem ID [658]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 6.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - 6y' + 9y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 18

dsolve(diff(y(x),x\$2)-6*diff(y(x),x)+9*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{3x} + c_2 e^{3x} x$$

Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 18

DSolve[y''[x]-6*y'[x]+9*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{3x}(c_2x + c_1)$$

9.7 problem 7

Internal problem ID [659]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 7.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$4y'' + 17y' + 4y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

dsolve(4*diff(y(x),x\$2)+17*diff(y(x),x)+4*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-4x} + c_2 e^{-\frac{x}{4}}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 24

DSolve[4*y''[x]+17*y'[x]+4*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-4x} (c_1 e^{15x/4} + c_2)$$

9.8 problem 8

Internal problem ID [660]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${f Section}$: Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 8.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$16y'' + 24y' + 9y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 18

dsolve(16*diff(y(x),x\$2)+24*diff(y(x),x)+9*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-\frac{3x}{4}} + c_2 e^{-\frac{3x}{4}} x$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 20

DSolve [16*y''[x]+24*y'[x]+9*y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) \to e^{-3x/4}(c_2x + c_1)$$

9.9 problem 9

Internal problem ID [661]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 9.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$25y'' - 20y' + 4y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 18

dsolve(25*diff(y(x),x\$2)-20*diff(y(x),x)+4*y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{\frac{2x}{5}} + c_2 e^{\frac{2x}{5}} x$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 20

 $DSolve[25*y''[x]-20*y'[x]+4*y[x]==0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to e^{2x/5}(c_2x + c_1)$$

9.10 problem 10

Internal problem ID [662]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 10.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$2y'' + 2y' + y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 25

dsolve(2*diff(y(x),x\$2)+2*diff(y(x),x)+y(x) = 0,y(x), singsol=all)

$$y(x) = c_1 e^{-\frac{x}{2}} \sin\left(\frac{x}{2}\right) + c_2 e^{-\frac{x}{2}} \cos\left(\frac{x}{2}\right)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 32

DSolve[2*y''[x]+2*y'[x]+y[x]==0,y[x],x,IncludeSingularSolutions -> True]

$$y(x) o e^{-x/2} \Big(c_2 \cos\left(\frac{x}{2}\right) + c_1 \sin\left(\frac{x}{2}\right) \Big)$$

9.11 problem 11

Internal problem ID [663]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 11.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$9y'' - 12y' + 4y = 0$$

With initial conditions

$$[y(0) = 2, y'(0) = -1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 14

$$y(t) = -\frac{e^{\frac{2t}{3}}(-6+7t)}{3}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 15

DSolve[{9*y''[t]-12*y'[t]+4*y[t]==0,{y[0]==0,y'[0]==-1}},y[t],t,IncludeSingularSolutions -> T

$$y(t) \rightarrow -e^{2t/3}t$$

9.12 problem 12

Internal problem ID [664]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 12.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - 6y' + 9y = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 2]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 11

dsolve([diff(y(t),t\$2)-6*diff(y(t),t)+9*y(t) = 0,y(0) = 0, D(y)(0) = 2],y(t), singsol=all)

$$y(t) = 2e^{3t}t$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 13

DSolve[{y''[t]-6*y'[t]+9*y[t]==0,{y[0]==0,y'[0]==2}},y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to 2e^{3t}t$$

9.13 problem 13

Internal problem ID [665]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 13.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$9y'' + 6y' + 82y = 0$$

With initial conditions

$$[y(0) = -1, y'(0) = 2]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 23

$$y(t) = \frac{e^{-\frac{t}{3}}(5\sin(3t) - 9\cos(3t))}{9}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 29

 $DSolve[{9*y''[t]+6*y'[t]+82*y[t]==0, {y[0]==-1,y'[0]==2}}, y[t], t, IncludeSingularSolutions -> T(0) = 0$

$$y(t) \to \frac{1}{9}e^{-t/3}(5\sin(3t) - 9\cos(3t))$$

9.14 problem 14

Internal problem ID [666]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 14.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' + 4y' + 4y = 0$$

With initial conditions

$$[y(-1) = 2, y'(-1) = 1]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 16

dsolve([diff(y(x),x\$2)+4*diff(y(x),x)+4*y(x) = 0,y(-1) = 2, D(y)(-1) = 1],y(x), singsol=all)

$$y(x) = e^{-2x-2}(5x+7)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 18

DSolve[{y''[x]+4*y'[x]+4*y[x]==0,{y[-1]==2,y'[-1]==1}},y[x],x,IncludeSingularSolutions -> Tru

$$y(x) \to e^{-2(x+1)}(5x+7)$$

9.15 problem 15

Internal problem ID [667]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} \colon$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 15.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$4y'' + 12y' + 9y = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = -4]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 14

dsolve([4*diff(y(t),t\$2)+12*diff(y(t),t)+9*y(t) = 0,y(0) = 1, D(y)(0) = -4],y(t), singsol=all = 0

$$y(t) = -\frac{e^{-\frac{3t}{2}}(-2+5t)}{2}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 21

DSolve[{4*y''[t]+12*y'[t]+9*y[t]==0,{y[0]==1,y'[0]==-4}},y[t],t,IncludeSingularSolutions -> T

$$y(t) \to \frac{1}{2}e^{-3t/2}(2-5t)$$

9.16 problem 16

Internal problem ID [668]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 16.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - y' + \frac{y}{4} = 0$$

With initial conditions

$$[y(0) = 2, y'(0) = b]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 16

dsolve([diff(y(t),t\$2)-diff(y(t),t)+25/100*y(t) = 0,y(0) = 2, D(y)(0) = b],y(t), singsol=all)

$$y(t) = e^{\frac{t}{2}}(2 + t(b-1))$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 20

$$y(t) \to e^{t/2}((b-1)t+2)$$

9.17 problem 23

Internal problem ID [669]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 23.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler], [_2nd_order, _linear, '_with_symmetry_[0,F(

$$t^2y'' - 4ty' + 6y = 0$$

Given that one solution of the ode is

$$y_1 = t^2$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

 $dsolve([t^2*diff(y(t),t^2)-4*t*diff(y(t),t)+6*y(t)=0,t^2],y(t), singsol=all)$

$$y(t) = c_1 t^3 + c_2 t^2$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 16

DSolve[t^2*y''[t]-4*t*y'[t]+6*y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to t^2(c_2t + c_1)$$

9.18 problem 24

Internal problem ID [670]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 24.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$t^2y'' + 2ty' - 2y = 0$$

Given that one solution of the ode is

$$y_1 = t$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 13

 $dsolve([t^2*diff(y(t),t^2)+2*t*diff(y(t),t)-2*y(t)=0,t],y(t), singsol=all)$

$$y(t) = \frac{c_1}{t^2} + c_2 t$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 16

DSolve[t^2*y''[t]+2*t*y'[t]-2*y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{c_1}{t^2} + c_2 t$$

9.19 problem 25

Internal problem ID [671]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 25.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _homogeneous]]

$$t^2y'' + 3ty' + y = 0$$

Given that one solution of the ode is

$$y_1 = rac{1}{t}$$

Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

 $dsolve([t^2*diff(y(t),t)^2)+3*t*diff(y(t),t)+y(t)=0,1/t],y(t), singsol=all)$

$$y(t) = \frac{c_1}{t} + \frac{c_2 \ln(t)}{t}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 17

DSolve[t^2*y''[t]+3*t*y'[t]+y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) o rac{c_2 \log(t) + c_1}{t}$$

9.20 problem 26

Internal problem ID [672]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} \colon$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 26.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$t^{2}y'' - t(2+t)y' + (2+t)y = 0$$

Given that one solution of the ode is

$$y_1 = t$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 13

 $dsolve([t^2*diff(y(t),t^2)-t*(t+2)*diff(y(t),t)+(t+2)*y(t)=0,t],y(t), singsol=all)$

$$y(t) = c_1 t + c_2 t e^t$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 16

 $DSolve[t^2*y''[t]-t*(t+2)*y'[t]+(t+2)*y[t]==0,y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) o t ig(c_2 e^t + c_1 ig)$$

9.21 problem 27

Internal problem ID [673]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} \colon$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 27.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler], [_2nd_order, _linear, '_with_symmetry_[0,F(

$$xy'' - y' + 4x^3y = 0$$

Given that one solution of the ode is

$$y_1 = \sin\left(x^2\right)$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

 $dsolve([x*diff(y(x),x$2)-diff(y(x),x)+4*x^3*y(x)=0,sin(x^2)],y(x), singsol=all)$

$$y(x) = c_1 \sin(x^2) + c_2 \cos(x^2)$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 20

DSolve $[x*y''[x]-y'[x]+4*x^3*y[x]==0,y[x],x$, IncludeSingularSolutions -> True]

$$y(x) \to c_1 \cos(x^2) + c_2 \sin(x^2)$$

9.22 problem 28

Internal problem ID [674]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} \colon$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 28.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(x-1)y''-y'x+y=0$$

Given that one solution of the ode is

$$y_1 = e^x$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 12

dsolve([(x-1)*diff(y(x),x\$2)-x*diff(y(x),x)+y(x)=0,exp(x)],y(x), singsol=all)

$$y(x) = c_1 x + e^x c_2$$

✓ Solution by Mathematica

Time used: 0.014 (sec). Leaf size: 17

 $DSolve[(x-1)*y''[x]-x*y'[x]+y[x]==0,y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to c_1 e^x - c_2 x$$

9.23 problem 29

Internal problem ID [675]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 29.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$x^2y'' - \left(x - \frac{3}{16}\right)y = 0$$

Given that one solution of the ode is

$$y_1 = x^{\frac{1}{4}} e^{2\sqrt{x}}$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 27

 $dsolve([x^2*diff(y(x),x$2)-(x-1875/10000)*y(x)=0,x^(1/4)*exp(2*sqrt(x))],y(x), singsol=all)$

$$y(x) = c_1 x^{\frac{1}{4}} \sinh\left(2\sqrt{x}\right) + c_2 x^{\frac{1}{4}} \cosh\left(2\sqrt{x}\right)$$

✓ Solution by Mathematica

Time used: 0.017 (sec). Leaf size: 41

 $DSolve[x^2*y''[x]-(x-1875/10000)*y[x] == 0, y[x], x, IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{1}{2} e^{-2\sqrt{x}} \sqrt[4]{x} \left(2c_1 e^{4\sqrt{x}} - c_2 \right)$$

9.24 problem 30

Internal problem ID [676]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 30.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$x^{2}y'' + y'x + \left(x^{2} - \frac{1}{4}\right)y = 0$$

Given that one solution of the ode is

$$y_1 = \frac{\sin\left(x\right)}{\sqrt{x}}$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 19

 $dsolve([x^2*diff(y(x),x$2)+x*diff(y(x),x)+(x^2-25/100)*y(x)=0,x^{(-1/2)}*sin(x)],y(x), singsol=0,x^{(-1/2)}*sin(x)=0,x^{(-1/$

$$y(x) = \frac{c_1 \sin(x)}{\sqrt{x}} + \frac{c_2 \cos(x)}{\sqrt{x}}$$

✓ Solution by Mathematica

Time used: 0.016 (sec). Leaf size: 39

 $DSolve[x^2*y''[x]+x*y'[x]+(x^2-25/100)*y[x] == 0, y[x], x, IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{e^{-ix}(2c_1 - ic_2e^{2ix})}{2\sqrt{x}}$$

9.25 problem 40

Internal problem ID [677]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} \colon$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 40.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler], [_2nd_order, _linear, '_with_symmetry_[0,F(

$$t^2y'' - 3ty' + 4y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

 $dsolve(t^2*diff(y(t),t)^2)-3*t*diff(y(t),t)+4*y(t)=0,y(t), singsol=all)$

$$y(t) = c_1 t^2 + c_2 t^2 \ln{(t)}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 18

DSolve[t^2*y''[t]-3*t*y'[t]+4*y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to t^2 (2c_2 \log(t) + c_1)$$

9.26 problem 41

Internal problem ID [678]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 41.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$t^2y'' + 2ty' + \frac{y}{4} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

 $dsolve(t^2*diff(y(t),t^2)+2*t*diff(y(t),t)+25/100*y(t)=0,y(t), singsol=all)$

$$y(t) = \frac{c_1}{\sqrt{t}} + \frac{c_2 \ln(t)}{\sqrt{t}}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 24

DSolve[t^2*y''[t]+2*t*y'[t]+25/100*y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) o rac{c_2 \log(t) + 2c_1}{2\sqrt{t}}$$

9.27 problem 42

Internal problem ID [679]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 42.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$2t^2y'' - 5ty' + 5y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 13

 $dsolve(2*t^2*diff(y(t),t^2)-5*t*diff(y(t),t)+5*y(t)=0,y(t), singsol=all)$

$$y(t) = c_1 t^{\frac{5}{2}} + c_2 t$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 18

DSolve[2*t^2*y''[t]-5*t*y'[t]+5*y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to t \left(c_2 t^{3/2} + c_1 \right)$$

9.28 problem 43

Internal problem ID [680]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 43.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _homogeneous]]

$$t^2y'' + 3ty' + y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

 $dsolve(t^2*diff(y(t),t)^2)+3*t*diff(y(t),t)+y(t)=0,y(t), singsol=all)$

$$y(t) = \frac{c_1}{t} + \frac{c_2 \ln (t)}{t}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 17

DSolve[t^2*y''[t]+3*t*y'[t]+y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) o rac{c_2 \log(t) + c_1}{t}$$

9.29 problem 44

Internal problem ID [681]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 44.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$4t^2y'' - 8ty' + 9y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

 $dsolve(4*t^2*diff(y(t),t\$2)-8*t*diff(y(t),t)+9*y(t)=0,y(t), singsol=all)$

$$y(t) = c_1 t^{\frac{3}{2}} + c_2 t^{\frac{3}{2}} \ln(t)$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 25

DSolve[4*t^2*y''[t]-8*t*y'[t]+9*y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{1}{2} t^{3/2} (3c_2 \log(t) + 2c_1)$$

9.30 problem 45

Internal problem ID [682]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

 ${\bf Section} :$ Chapter 3, Second order linear equations, 3.4 Repeated roots, reduction of order , page 172

Problem number: 45.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$t^2y'' + 5ty' + 13y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 25

 $dsolve(t^2*diff(y(t),t^2)+5*t*diff(y(t),t)+13*y(t)=0,y(t), singsol=all)$

$$y(t) = \frac{c_1 \sin(3 \ln(t))}{t^2} + \frac{c_2 \cos(3 \ln(t))}{t^2}$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 26

DSolve[t^2*y''[t]+5*t*y'[t]+13*y[t]==0,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{c_2 \cos(3 \log(t)) + c_1 \sin(3 \log(t))}{t^2}$$

10	Chapter 3, Second order linear equations, section
	3.6, Variation of Parameters. page 190

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10.1 problem 1

Internal problem ID [683]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 1.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$y'' - 5y' + 6y - 2e^t = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 19

dsolve(diff(y(t),t\$2)-5*diff(y(t),t)+6*y(t) = 2*exp(t),y(t), singsol=all)

$$y(t) = c_2 e^{3t} + c_1 e^{2t} + e^t$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 24

 $DSolve[y''[t]-5*y'[t]+6*y[t] == 2*Exp[t],y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \rightarrow e^t \left(1 + e^t \left(c_2 e^t + c_1\right)\right)$$

10.2 problem 2

Internal problem ID [684]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 2.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$y'' - y' - 2y - 2e^{-t} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 24

 $dsolve(diff(y(t),t)^2)-diff(y(t),t)^2*y(t) = 2*exp(-t),y(t), singsol=all)$

$$y(t) = c_2 e^{-t} + c_1 e^{2t} - \frac{2t e^{-t}}{3}$$

✓ Solution by Mathematica

Time used: 0.012 (sec). Leaf size: 32

DSolve[y''[t]-y'[t]-2*y[t] == 2*Exp[-t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{1}{9}e^{-t}(-6t + 9c_2e^{3t} - 2 + 9c_1)$$

10.3 problem 3

Internal problem ID [685]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 3.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$y'' + 2y' + y - 3e^{-t} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 27

dsolve(diff(y(t),t\$2)+2*diff(y(t),t)+y(t) = 3*exp(-t),y(t), singsol=all)

$$y(t) = c_2 e^{-t} + t e^{-t} c_1 + \frac{3 e^{-t} t^2}{2}$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 29

 $DSolve[y''[t]+2*y'[t]+y[t] == 3*Exp[-t],y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \to \frac{1}{2}e^{-t}(3t^2 + 2c_2t + 2c_1)$$

10.4 problem 4

Internal problem ID [686]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 4.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$4y'' - 4y' + y - 16e^{\frac{t}{2}} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 27

dsolve(4*diff(y(t),t\$2)-4*diff(y(t),t)+y(t) = 16*exp(t/2),y(t), singsol=all)

$$y(t) = c_2 e^{\frac{t}{2}} + t e^{\frac{t}{2}} c_1 + 2t^2 e^{\frac{t}{2}}$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 24

DSolve[4*y''[t]-4*y'[t]+y[t]== 16*Exp[t/2],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to e^{t/2}(t(2t+c_2)+c_1)$$

10.5 problem 5

Internal problem ID [687]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 5.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$y'' + y - \tan(t) = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 23

dsolve(diff(y(t),t\$2)+y(t) = tan(t),y(t), singsol=all)

$$y(t) = c_2 \sin(t) + \cos(t) c_1 - \cos(t) \ln(\sec(t) + \tan(t))$$

✓ Solution by Mathematica

Time used: 0.015 (sec). Leaf size: 22

DSolve[y''[t]+y[t] == Tan[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow \cos(t)(-\arctanh(\sin(t)) + c_1) + c_2\sin(t)$$

10.6 problem 6

Internal problem ID [688]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 6.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$y'' + 9y - 9\sec(3t)^2 = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 33

 $dsolve(diff(y(t),t\$2)+9*y(t) = 9*sec(3*t)^2,y(t), singsol=all)$

$$y(t) = c_2 \sin(3t) + c_1 \cos(3t) + \ln(\sec(3t) + \tan(3t)) \sin(3t) - 1$$

✓ Solution by Mathematica

Time used: 0.053 (sec). Leaf size: 27

 $DSolve[y''[t]+9*y[t] == 9*Sec[3*t]^2,y[t],t,IncludeSingularSolutions -> True]$

$$y(t) \rightarrow \sin(3t)(\operatorname{arctanh}(\sin(3t)) + c_2) + c_1\cos(3t) - 1$$

10.7 problem 7

Internal problem ID [689]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 7.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$y'' + 4y' + 4y - \frac{e^{-2t}}{t^2} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 28

 $\label{eq:diff} $$ $$ $ dsolve(diff(y(t),t)+4*y(t) = t^{(-2)*exp(-2*t)}, y(t), $$ singsol=all)$ $$$

$$y(t) = e^{-2t}c_2 + e^{-2t}tc_1 - (\ln(t) + 1)e^{-2t}$$

✓ Solution by Mathematica

Time used: 0.009 (sec). Leaf size: 23

 $DSolve[y''[t]+4*y'[t]+4*y[t] == t^{(-2)*Exp[-2*t]}, y[t], t, IncludeSingularSolutions \rightarrow True]$

$$y(t) \to e^{-2t}(-\log(t) + c_2t - 1 + c_1)$$

10.8 problem 8

Internal problem ID [690]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 8.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$y'' + 4y - 3\csc\left(2t\right) = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 35

dsolve(diff(y(t),t\$2)+4*y(t) = 3*csc(2*t),y(t), singsol=all)

$$y(t) = c_2 \sin(2t) + c_1 \cos(2t) - \frac{3\ln(\csc(2t))\sin(2t)}{4} - \frac{3\cos(2t)t}{2}$$

✓ Solution by Mathematica

Time used: 0.016 (sec). Leaf size: 47

DSolve[y''[t]+4*y[t] ==3*Csc[2*t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{1}{4}((-6t + 4c_1)\cos(2t) + \sin(2t)(3\log(\tan(2t)) + 3\log(\cos(2t)) + 4c_2))$$

10.9 problem 9

Internal problem ID [691]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 9.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$y'' + y - 2\sec\left(\frac{t}{2}\right) = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 43

dsolve(diff(y(t),t\$2)+y(t) = 2*sec(t/2),y(t), singsol=all)

$$y(t) = c_2 \sin(t) + \cos(t) c_1 + \cos\left(\frac{t}{2}\right) \left(-8\left(\ln(2) + \ln\left(\csc(t)\sin\left(\frac{t}{2}\right)\left(\sin\left(\frac{t}{2}\right) + 1\right)\right)\right) \sin\left(\frac{t}{2}\right) + 8\right)$$

✓ Solution by Mathematica

Time used: 0.054 (sec). Leaf size: 34

DSolve[y''[t]+y[t] == 2*Sec[t/2],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \sin(t) \left(-4 \operatorname{arctanh} \left(\sin\left(\frac{t}{2}\right) \right) + c_2 \right) + 8 \cos\left(\frac{t}{2}\right) + c_1 \cos(t)$$

10.10 problem 10

Internal problem ID [692]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 10.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$y'' - 2y' + y - \frac{e^t}{t^2 + 1} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 30

 $\label{eq:diff} \\ \text{dsolve}(\text{diff}(y(t),t\$2)-2*\text{diff}(y(t),t)+y(t) = \exp(t)/(1+t^2),\\ y(t), \text{ singsol=all}) \\$

$$y(t) = c_2 e^t + t e^t c_1 + e^t \left(-\frac{\ln(t^2 + 1)}{2} + t \arctan(t) \right)$$

✓ Solution by Mathematica

Time used: 0.01 (sec). Leaf size: 33

DSolve[y''[t]-2*y'[t]+y[t] == Exp[t]/(1+t^2),y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{1}{2}e^{t}(-\log(t^{2}+1) + 2(t(\arctan(t) + c_{2}) + c_{1}))$$

10.11 problem 11

Internal problem ID [693]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 11.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$y'' - 5y' + 6y - g(t) = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 46

 $dsolve(diff(y(t),t)^2)-5*diff(y(t),t)+6*y(t) = g(t),y(t), singsol=all)$

$$y(t) = c_2 e^{3t} + c_1 e^{2t} + \left(\int g(t) e^{-3t} dt \right) e^{3t} - \left(\int g(t) e^{-2t} dt \right) e^{2t}$$

✓ Solution by Mathematica

Time used: 0.026 (sec). Leaf size: 56

DSolve[y''[t]-5*y'[t]+6*y[t] == g[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to e^{2t} \left(\int_1^t -e^{-2K[1]} g(K[1]) dK[1] + e^t \left(\int_1^t e^{-3K[2]} g(K[2]) dK[2] + c_2 \right) + c_1 \right)$$

10.12 problem 12

Internal problem ID [694]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 12.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$y'' + 4y - g(t) = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 47

dsolve(diff(y(t),t\$2)+4*y(t) = g(t),y(t), singsol=all)

$$y(t) = c_2 \sin(2t) + c_1 \cos(2t) + \frac{\left(\int \cos(2t) g(t) dt\right) \sin(2t)}{2} - \frac{\left(\int \sin(2t) g(t) dt\right) \cos(2t)}{2}$$

✓ Solution by Mathematica

Time used: 0.039 (sec). Leaf size: 59

DSolve[y''[t]+4*y[t] == g[t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \sin(2t) \left(\int_1^t \frac{1}{2} \cos(2K[2]) g(K[2]) dK[2] + c_2 \right)$$
$$+ \cos(2t) \left(\int_1^t -\cos(K[1]) g(K[1]) \sin(K[1]) dK[1] + c_1 \right)$$

10.13 problem 13

Internal problem ID [695]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 13.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _nonhomogeneous]]

$$t^2y'' - 2y - 3t^2 + 1 = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 22

 $dsolve(t^2*diff(y(t),t^2)-2*y(t) = 3*t^2-1,y(t), singsol=all)$

$$y(t) = c_2 t^2 + t^2 \ln(t) + \frac{1}{2} + \frac{c_1}{t}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 31

 $DSolve[t^2*y''[t]-2*y[t] == 3*t^2-1,y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \to t^2 \log(t) + \left(-\frac{1}{3} + c_2\right) t^2 + \frac{c_1}{t} + \frac{1}{2}$$

10.14 problem 14

Internal problem ID [696]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 14.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$t^{2}y'' - t(2+t)y' + (2+t)y - 2t^{3} = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 18

 $dsolve(t^2*diff(y(t),t^2)-t*(t+2)*diff(y(t),t)+(t+2)*y(t) = 2*t^3,y(t), singsol=all)$

$$y(t) = c_2 t + t e^t c_1 - 2t^2$$

Solution by Mathematica

Time used: 0.008 (sec). Leaf size: 20

 $DSolve[t^2*y''[t]-t*(t+2)*y'[t]+(t+2)*y[t] == 2*t^3,y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \to t(-2t + c_2e^t - 2 + c_1)$$

10.15 problem 15

Internal problem ID [697]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 15.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$ty'' - (t+1)y' + y - e^{2t}t^2 = 0$$

Solution by Maple

Time used: 0.016 (sec). Leaf size: 23

 $dsolve(t*diff(y(t),t$2)-(1+t)*diff(y(t),t)+y(t) = t^2*exp(2*t),y(t), singsol=all)$

$$y(t) = (t+1) c_2 + c_1 e^t + \frac{(t-1) e^{2t}}{2}$$

✓ Solution by Mathematica

Time used: 0.029 (sec). Leaf size: 31

 $DSolve[t*y''[t]-(1+t)*y'[t]+y[t] == t^2*Exp[2*t],y[t],t,IncludeSingularSolutions \rightarrow True]$

$$y(t) \to \frac{1}{2}e^{2t}(t-1) + c_1e^t - c_2(t+1)$$

10.16 problem 16

Internal problem ID [698]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 16.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(-t+1)y'' + ty' - y - 2(t-1)^{2}e^{-t} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 23

 $dsolve((1-t)*diff(y(t),t\$2)+t*diff(y(t),t)-y(t) = 2*(t-1)^2*exp(-t),y(t), singsol=all)$

$$y(t) = c_2 t + c_1 e^t - \frac{(2t-1)e^{-t}}{2}$$

✓ Solution by Mathematica

Time used: 0.035 (sec). Leaf size: 30

 $DSolve[(1-t)*y''[t]+t*y'[t]-y[t] == 2*(t-1)^2*Exp[-t], y[t], t, IncludeSingularSolutions -> True$

$$y(t)
ightarrow e^{-t} \left(rac{1}{2} - t
ight) + c_1 e^t - c_2 t$$

10.17 problem 17

Internal problem ID [699]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 17.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$x^{2}y'' - 3y'x + 4y - \ln(x) x^{2} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 26

 $dsolve(x^2*diff(y(x),x^2)-3*x*diff(y(x),x)+4*y(x) = x^2*ln(x),y(x), singsol=all)$

$$y(x) = x^{2}c_{2} + \ln(x) c_{1}x^{2} + \frac{\ln(x)^{3} x^{2}}{6}$$

✓ Solution by Mathematica

Time used: 0.011 (sec). Leaf size: 27

 $DSolve[x^2*y''[x]-3*x*y'[x]+4*y[x] == x^2*Log[x],y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{1}{6}x^2 (\log^3(x) + 12c_2 \log(x) + 6c_1)$$

10.18 problem 20

Internal problem ID [700]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 20.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$x^{2}y'' + y'x + \left(x^{2} - \frac{1}{4}\right)y - g(x) = 0$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 51

 $dsolve(x^2*diff(y(x),x$2)+x*diff(y(x),x)+(x^2-25/100)*y(x) = g(x),y(x), singsol=all)$

$$y(x) = \frac{\sin(x) c_2}{\sqrt{x}} + \frac{\cos(x) c_1}{\sqrt{x}} + \frac{\left(\int \frac{\cos(x)g(x)}{x^{\frac{3}{2}}} dx\right) \sin(x) - \left(\int \frac{\sin(x)g(x)}{x^{\frac{3}{2}}} dx\right) \cos(x)}{\sqrt{x}}$$

✓ Solution by Mathematica

Time used: 0.096 (sec). Leaf size: 96 $\,$

 $DSolve[x^2*y''[x]+x*y'[x]+(x^2-25/100)*y[x] == g[x],y[x],x,IncludeSingularSolutions \rightarrow True]$

$$y(x) \to \frac{e^{-ix} \left(2 \left(\int_{1}^{x} \frac{ie^{iK[1]}g(K[1])}{2K[1]^{3/2}} dK[1] + c_{1} \right) - ie^{2ix} \left(\int_{1}^{x} \frac{e^{-iK[2]}g(K[2])}{K[2]^{3/2}} dK[2] + c_{2} \right) \right)}{2\sqrt{x}}$$

10.19 problem 29

Internal problem ID [701]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 29.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$t^2y'' - 2ty' + 2y - 4t^2 = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 22

 $dsolve(t^2*diff(y(t),t\$2)-2*t*diff(y(t),t)+2*y(t) = 4*t^2,y(t), singsol=all)$

$$y(t) = c_2 t^2 + c_1 t + 4t^2 (-1 + \ln(t))$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 21

DSolve[t^2*y''[t]-2*t*y'[t]+2*y[t] ==4*t^2,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to t(4t \log(t) + (-4 + c_2)t + c_1)$$

10.20 problem 30

Internal problem ID [702]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 30.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _nonhomogeneous]]

$$\boxed{t^2y'' + 7ty' + 5y - t = 0}$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 33

 $dsolve(t^2*diff(y(t),t)^2)+7*t*diff(y(t),t)+5*y(t) = t,y(t), singsol=all)$

$$y(t) = \frac{c_2 + \frac{2\left(c_1 + \frac{t^2}{2}\right)^3}{3} - c_1\left(c_1 + \frac{t^2}{2}\right)^2}{t^5}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 23

DSolve[t^2*y''[t]+7*t*y'[t]+5*y[t] ==t,y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{c_1}{t^5} + \frac{t}{12} + \frac{c_2}{t}$$

10.21 problem 31

Internal problem ID [703]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 31.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$ty'' - (t+1)y' + y - e^{2t}t^2 = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 23

 $dsolve(t*diff(y(t),t$2)-(1+t)*diff(y(t),t)+y(t) = t^2*exp(2*t),y(t), singsol=all)$

$$y(t) = (t+1) c_2 + c_1 e^t + \frac{(t-1) e^{2t}}{2}$$

✓ Solution by Mathematica

Time used: 0.011 (sec). Leaf size: 31

DSolve[t*y''[t]-(1+t)*y'[t]+y[t] ==t^2*Exp[2*t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \to \frac{1}{2}e^{2t}(t-1) + c_1e^t - c_2(t+1)$$

10.22 problem 32

Internal problem ID [704]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, section 3.6, Variation of Parameters. page 190

Problem number: 32.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(-t+1)y'' + ty' - y - 2(t-1)e^{-t} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 46

dsolve((1-t)*diff(y(t),t\$2)+t*diff(y(t),t)-y(t) = 2*(t-1)*exp(-t),y(t), singsol=all)

$$y(t) = c_2 t + c_1 e^t - 2\left(t e^{t-1} \operatorname{Ei}_1(t-1) - e^{2t-2} \operatorname{Ei}_1(2t-2) - \frac{1}{2}\right) e^{-t}$$

✓ Solution by Mathematica

Time used: 0.085 (sec). Leaf size: 47

DSolve[(1-t)*y''[t]+t*y'[t]-y[t] ==2*(t-1)*Exp[-t],y[t],t,IncludeSingularSolutions -> True]

$$y(t) \rightarrow -2e^{t-2} \text{ExpIntegralEi}(2-2t) + \frac{2t \text{ExpIntegralEi}(1-t)}{e} + e^{-t} + c_1e^t - c_2t$$

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11.1 problem 28

Internal problem ID [705]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.7 Mechanical and Electrical Vibrations. page 203

Problem number: 28.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$u'' + 2u = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 21

dsolve(diff(u(t),t\$2)+2*u(t) = 0,u(t), singsol=all)

$$u(t) = c_1 \sin\left(t\sqrt{2}\right) + c_2 \cos\left(t\sqrt{2}\right)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 28

DSolve[u''[t]+2*u[t] ==0,u[t],t,IncludeSingularSolutions -> True]

$$u(t) \to c_1 \cos\left(\sqrt{2}t\right) + c_2 \sin\left(\sqrt{2}t\right)$$

11.2 problem 29

Internal problem ID [706]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.7 Mechanical and Electrical Vibrations. page 203

Problem number: 29.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$u'' + \frac{u'}{4} + 2u = 0$$

With initial conditions

$$[u(0) = 0, u'(0) = 2]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 20

dsolve([diff(u(t),t\$2)+1/4*diff(u(t),t)+2*u(t) = 0,u(0) = 0, D(u)(0) = 2],u(t), singsol=all)

$$u(t) = \frac{16\sqrt{127} e^{-\frac{t}{8}} \sin\left(\frac{\sqrt{127}t}{8}\right)}{127}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 30

DSolve[{u''[t]+1/4*u'[t]+2*u[t] ==0,{u[0]==0,u'[0]==2}},u[t],t,IncludeSingularSolutions -> Tr

$$u(t)
ightarrow rac{16e^{-t/8}\sin\left(rac{\sqrt{127}t}{8}
ight)}{\sqrt{127}}$$

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12.1 problem 21

Internal problem ID [707]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.7 Forced Vibrations. page 217

Problem number: 21.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$u'' + \frac{u'}{8} + 4u - 3\cos\left(\frac{t}{4}\right) = 0$$

With initial conditions

$$[u(0) = 2, u'(0) = 0]$$

✓ Solution by Maple

Time used: 0.046 (sec). Leaf size: 46

$$dsolve([diff(u(t),t\$2)+125/1000*diff(u(t),t)+4*u(t) = 3*cos(t/4),u(0) = 2, D(u)(0) = 0],u(t),u(t) = 0$$

$$u(t) = \frac{19274 \,\mathrm{e}^{-\frac{t}{16}} \sqrt{1023} \, \sin\left(\frac{\sqrt{1023} \, t}{16}\right)}{16242171} + \frac{19658 \,\mathrm{e}^{-\frac{t}{16}} \cos\left(\frac{\sqrt{1023} \, t}{16}\right)}{15877} + \frac{96 \sin\left(\frac{t}{4}\right)}{15877} + \frac{12096 \cos\left(\frac{t}{4}\right)}{15877} + \frac{12096 \cos\left(\frac{t}{4}\right)}{16242171} + \frac{12096 \cos\left(\frac{t}{4}\right)}{1624217} + \frac{12096 \cos\left(\frac{t}{4}\right)}{162421} + \frac{12096 \cos$$

✓ Solution by Mathematica

Time used: 0.01 (sec). Leaf size: 68

DSolve[{u''[t]+125/1000*u'[t]+4*u[t] ==3*Cos[t/4],{u[0]==0,u'[0]==0}},u[t],t,IncludeSingularS

$$u(t) \rightarrow \frac{32 \left(1023 \left(\sin\left(\frac{t}{4}\right) + 126\cos\left(\frac{t}{4}\right)\right) - 2e^{-t/16} \left(65\sqrt{1023}\sin\left(\frac{\sqrt{1023}t}{16}\right) + 64449\cos\left(\frac{\sqrt{1023}t}{16}\right)\right)\right)}{5414057}$$

12.2 problem 22

Internal problem ID [708]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.7 Forced Vibrations. page 217

Problem number: 22.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$u'' + \frac{u'}{8} + 4u - 3\cos(2t) = 0$$

With initial conditions

$$[u(0) = 2, u'(0) = 0]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 40

dsolve([diff(u(t),t\$2)+125/1000*diff(u(t),t)+4*u(t) = 3*cos(2*t),u(0) = 2, D(u)(0) = 0],u(t),

$$u(t) = -\frac{382 e^{-\frac{t}{16}} \sqrt{1023} \sin\left(\frac{\sqrt{1023}t}{16}\right)}{1023} + 2 e^{-\frac{t}{16}} \cos\left(\frac{\sqrt{1023}t}{16}\right) + 12 \sin\left(2t\right)$$

✓ Solution by Mathematica

Time used: 0.008 (sec). Leaf size: 39

DSolve[{u''[t]+125/1000*u'[t]+4*u[t] ==3*Cos[2*t],{u[0]==0,u'[0]==0}},u[t],t,IncludeSingularS

$$u(t) \to 12\sin(2t) - 128\sqrt{\frac{3}{341}}e^{-t/16}\sin\left(\frac{\sqrt{1023}t}{16}\right)$$

12.3 problem 23

Internal problem ID [709]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 3, Second order linear equations, 3.7 Forced Vibrations. page 217

Problem number: 23.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _linear, _nonhomogeneous]]

$$u'' + \frac{u'}{8} + 4u - 3\cos(6t) = 0$$

With initial conditions

$$[u(0) = 2, u'(0) = 0]$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 46

$$dsolve([diff(u(t),t\$2)+125/1000*diff(u(t),t)+4*u(t) = 3*cos(6*t),u(0) = 2, D(u)(0) = 0],u(t),u(t) = 0$$

$$u(t) = \frac{2806 \,\mathrm{e}^{-\frac{t}{16}} \sqrt{1023} \,\sin\left(\frac{\sqrt{1023} \,t}{16}\right)}{1524549} + \frac{34322 \,\mathrm{e}^{-\frac{t}{16}} \cos\left(\frac{\sqrt{1023} \,t}{16}\right)}{16393} + \frac{36 \sin\left(6t\right)}{16393} - \frac{1536 \cos\left(6t\right)}{16393}$$

Solution by Mathematica

Time used: 0.01 (sec). Leaf size: 63

$$u(t) \to \frac{4\left(3069\sin(6t) - 130944\cos(6t) + 32e^{-t/16}\left(4092\cos\left(\frac{\sqrt{1023}t}{16}\right) - 5\sqrt{1023}\sin\left(\frac{\sqrt{1023}t}{16}\right)\right)\right)}{5590013}$$

12.4 problem 24

Internal problem ID [710]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 3, Second order linear equations, 3.7 Forced Vibrations. page 217

Problem number: 24.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [NONE]

$$u'' + u' + \frac{u^3}{5} - \cos(t) = 0$$

With initial conditions

$$[u(0) = 2, u'(0) = 0]$$

X Solution by Maple

 $dsolve([diff(u(t),t$2)+diff(u(t),t)+1/5*u(t)^3 = cos(t),u(0) = 2, D(u)(0) = 0],u(t), singsol=0$

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

 $DSolve[\{u''[t]+u'[t]+1/5*u[t]^3 == 3*Cos[t], \{u[0]==0,u'[0]==0\}\}, u[t], t, IncludeSingularSolution]$

Not solved

13 Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

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13.1 problem 1

Internal problem ID [711]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 1.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _missing_x]]

$$y'' - y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 34

Order:=6; dsolve(diff(y(x),x\$2)-y(x)=0,y(x),type='series',x=0);

$$y(x) = \left(1 + \frac{1}{2}x^2 + \frac{1}{24}x^4\right)y(0) + \left(x + \frac{1}{6}x^3 + \frac{1}{120}x^5\right)D(y)\left(0\right) + O\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 42

AsymptoticDSolveValue[$y''[x]-y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \rightarrow c_2 \left(\frac{x^5}{120} + \frac{x^3}{6} + x\right) + c_1 \left(\frac{x^4}{24} + \frac{x^2}{2} + 1\right)$$

13.2 problem 2

Internal problem ID [712]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 2.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _homogeneous]]

$$y'' - y'x - y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 34

Order:=6; dsolve(diff(y(x),x\$2)-x*diff(y(x),x)-y(x)=0,y(x),type='series',x=0);

$$y(x) = \left(1 + \frac{1}{2}x^2 + \frac{1}{8}x^4\right)y(0) + \left(x + \frac{1}{3}x^3 + \frac{1}{15}x^5\right)D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 42

AsymptoticDSolveValue[$y''[x]-x*y'[x]-y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \rightarrow c_2 \left(\frac{x^5}{15} + \frac{x^3}{3} + x\right) + c_1 \left(\frac{x^4}{8} + \frac{x^2}{2} + 1\right)$$

13.3 problem 4

Internal problem ID [713]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 4.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$y'' + k^2 x^2 y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 30

Order:=6; dsolve(diff(y(x),x\$2)+k^2*x^2*y(x)=0,y(x),type='series',x=0);

$$y(x) = \left(1 - \frac{k^2 x^4}{12}\right) y(0) + \left(x - \frac{1}{20} k^2 x^5\right) D(y)\left(0\right) + O\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 34

AsymptoticDSolveValue[$y''[x]+k^2*x^2*y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \to c_2 \left(x - \frac{k^2 x^5}{20} \right) + c_1 \left(1 - \frac{k^2 x^4}{12} \right)$$

13.4 problem 5

Internal problem ID [714]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 5.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$(1-x)y'' + y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 49

Order:=6; dsolve((1-x)*diff(y(x),x\$2)+y(x)=0,y(x),type='series',x=0);

$$y(x) = \left(1 - \frac{1}{2}x^2 - \frac{1}{6}x^3 - \frac{1}{24}x^4 - \frac{1}{60}x^5\right)y(0) + \left(x - \frac{1}{6}x^3 - \frac{1}{12}x^4 - \frac{1}{24}x^5\right)D(y)\left(0\right) + O\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 63

AsymptoticDSolveValue[$(1-x)*y''[x]+y[x]==0,y[x],\{x,0,5\}$]

$$y(x)
ightarrow c_2 igg(-rac{x^5}{24} - rac{x^4}{12} - rac{x^3}{6} + x igg) + c_1 igg(-rac{x^5}{60} - rac{x^4}{24} - rac{x^3}{6} - rac{x^2}{2} + 1 igg)$$

13.5 problem 6

Internal problem ID [715]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 6.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(x^2 + 2) y'' - y'x + 4y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 34

Order:=6; $dsolve((2+x^2)*diff(y(x),x$2)-x*diff(y(x),x)+4*y(x)=0,y(x),type='series',x=0);$

$$y(x) = \left(1 - x^2 + \frac{1}{6}x^4\right)y(0) + \left(x - \frac{1}{4}x^3 + \frac{7}{160}x^5\right)D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 40

AsymptoticDSolveValue[$(2+x^2)*y''[x]-x*y'[x]+4*y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \rightarrow c_2 \left(\frac{7x^5}{160} - \frac{x^3}{4} + x\right) + c_1 \left(\frac{x^4}{6} - x^2 + 1\right)$$

13.6 problem 7

Internal problem ID [716]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 7.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$y'' + y'x + 2y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 34

Order:=6; dsolve(diff(y(x),x\$2)+x*diff(y(x),x)+2*y(x)=0,y(x),type='series',x=0);

$$y(x) = \left(1 - x^2 + \frac{1}{3}x^4\right)y(0) + \left(x - \frac{1}{2}x^3 + \frac{1}{8}x^5\right)D(y)\left(0\right) + O\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 40

AsymptoticDSolveValue[$y''[x]+x*y'[x]+2*y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \to c_2 \left(\frac{x^5}{8} - \frac{x^3}{2} + x\right) + c_1 \left(\frac{x^4}{3} - x^2 + 1\right)$$

13.7 problem 9

Internal problem ID [717]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 9.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(x^2 + 1) y'' - 4y'x + 6y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 25

Order:=6; $dsolve((1+x^2)*diff(y(x),x$2)-4*x*diff(y(x),x)+6*y(x)=0,y(x),type='series',x=0);$

$$y(x) = y(0) + D(y)(0)x - 3y(0)x^{2} - \frac{D(y)(0)x^{3}}{3}$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 26

AsymptoticDSolveValue[$(1+x^2)*y''[x]-4*x*y'[x]+6*y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \to c_2 \left(x - \frac{x^3}{3} \right) + c_1 \left(1 - 3x^2 \right)$$

13.8 problem 10

Internal problem ID [718]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 10.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _homogeneous]]

$$(-x^2 + 4) y'' + 2y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 29

Order:=6; $dsolve((4-x^2)*diff(y(x),x$2)+2*y(x)=0,y(x),type='series',x=0);$

$$y(x) = \left(-\frac{x^2}{4} + 1\right)y(0) + \left(x - \frac{1}{12}x^3 - \frac{1}{240}x^5\right)D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 35

AsymptoticDSolveValue[$(4-x^2)*y''[x]+2*y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \to c_1 \left(1 - \frac{x^2}{4}\right) + c_2 \left(-\frac{x^5}{240} - \frac{x^3}{12} + x\right)$$

13.9 problem 11

Internal problem ID [719]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 11.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _homogeneous]]

$$(-x^2+3)y'' - 3y'x - y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 34

Order:=6; dsolve($(3-x^2)*diff(y(x),x$2)-3*x*diff(y(x),x)-y(x)=0,y(x),type='series',x=0);$

$$y(x) = \left(1 + \frac{1}{6}x^2 + \frac{1}{24}x^4\right)y(0) + \left(x + \frac{2}{9}x^3 + \frac{8}{135}x^5\right)D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 70

AsymptoticDSolveValue[$(3-x^2)*y''[x]-3*y'[x]-y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \rightarrow c_1 \left(\frac{13x^5}{1080} + \frac{x^4}{36} + \frac{x^3}{18} + \frac{x^2}{6} + 1 \right) + c_2 \left(\frac{49x^5}{1080} + \frac{7x^4}{72} + \frac{2x^3}{9} + \frac{x^2}{2} + x \right)$$

13.10 problem 12

Internal problem ID [720]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 12.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(1-x)y'' + y'x - y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Order:=6;

Time used: 0.016 (sec). Leaf size: 34

 $\label{eq:decomposition} \\ \text{dsolve}((1-x)*\text{diff}(y(x),x\$2)+x*\text{diff}(y(x),x)-y(x)=0,y(x),\\ \text{type='series',x=0)};$

$$y(x) = \left(1 + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5\right)y(0) + D(y)(0)x + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 41

AsymptoticDSolveValue[$(1-x)*y''[x]+x*y'[x]-y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \to c_1 \left(\frac{x^5}{120} + \frac{x^4}{24} + \frac{x^3}{6} + \frac{x^2}{2} + 1 \right) + c_2 x$$

13.11 problem 13

Internal problem ID [721]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 13.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$2y'' + y'x + 3y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 34

Order:=6; dsolve(2*diff(y(x),x\$2)+x*diff(y(x),x)+3*y(x)=0,y(x),type='series',x=0);

$$y(x) = \left(1 - \frac{3}{4}x^2 + \frac{5}{32}x^4\right)y(0) + \left(x - \frac{1}{3}x^3 + \frac{1}{20}x^5\right)D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 42

AsymptoticDSolveValue[$2*y''[x]+x*y'[x]+3*y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \rightarrow c_2 \left(\frac{x^5}{20} - \frac{x^3}{3} + x\right) + c_1 \left(\frac{5x^4}{32} - \frac{3x^2}{4} + 1\right)$$

13.12 problem 15

Internal problem ID [722]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 15.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _homogeneous]]

$$y'' - y'x - y = 0$$

With initial conditions

$$[y(0) = 2, y'(0) = 1]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 20

Order:=6; dsolve([diff(y(x),x\$2)-x*diff(y(x),x)-y(x)=0,y(0) = 2, D(y)(0) = 1],y(x),type='series',x=0);

$$y(x) = 2 + x + x^2 + \frac{1}{3}x^3 + \frac{1}{4}x^4 + \frac{1}{15}x^5 + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 30

$$y(x) \rightarrow \frac{x^5}{15} + \frac{x^4}{4} + \frac{x^3}{3} + x^2 + x + 2$$

13.13 problem 16

Internal problem ID [723]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 16.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(x^{2} + 2) y'' - y'x + 4y = 0$$

With initial conditions

$$[y(0) = -1, y'(0) = 3]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Order:=6;

Time used: 0.0 (sec). Leaf size: 20

dsolve([(2+x^2)*diff(y(x),x\$2)-x*diff(y(x),x)+4*y(x)=0,y(0) = -1, D(y)(0) = 3],y(x),type='ser

$$y(x) = -1 + 3x + x^2 - \frac{3}{4}x^3 - \frac{1}{6}x^4 + \frac{21}{160}x^5 + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 32

AsymptoticDSolveValue[$\{(2+x^2)*y''[x]-x*y'[x]+4*y[x]==0,\{y[0]==-1,y'[0]==3\}\},y[x],\{x,0,5\}$]

$$y(x) \rightarrow \frac{21x^5}{160} - \frac{x^4}{6} - \frac{3x^3}{4} + x^2 + 3x - 1$$

13.14 problem 17

Internal problem ID [724]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 17.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$y'' + y'x + 2y = 0$$

With initial conditions

$$[y(0) = 4, y'(0) = -1]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Order:=6;

Time used: 0.0 (sec). Leaf size: 20

Time asea. 0.0 (see). Bear size. 20

 $\frac{\text{dsolve}([\text{diff}(y(x),x\$2)+x*\text{diff}(y(x),x)+2*y(x)=0,y(0) = 4, D(y)(0) = -1],y(x),type=}{\text{series',x=0}}$

$$y(x) = 4 - x - 4x^{2} + \frac{1}{2}x^{3} + \frac{4}{3}x^{4} - \frac{1}{8}x^{5} + O(x^{6})$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 34

$$y(x) \rightarrow -\frac{x^5}{8} + \frac{4x^4}{3} + \frac{x^3}{2} - 4x^2 - x + 4$$

13.15 problem 18

Internal problem ID [725]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 18.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(1-x)y'' + y'x - y = 0$$

With initial conditions

$$[y(0) = -3, y'(0) = 2]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 20

Order:=6; dsolve([(1-x)*diff(y(x),x\$2)+x*diff(y(x),x)-y(x)=0,y(0) = -3, D(y)(0) = 2],y(x),type='series'

$$y(x) = -3 + 2x - \frac{3}{2}x^2 - \frac{1}{2}x^3 - \frac{1}{8}x^4 - \frac{1}{40}x^5 + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 36

AsymptoticDSolveValue[$\{(1-x)*y''[x]+x*y'[x]-y[x]==0,\{y[0]==-3,y'[0]==2\}\},y[x],\{x,0,5\}$]

$$y(x) \rightarrow -\frac{x^5}{40} - \frac{x^4}{8} - \frac{x^3}{2} - \frac{3x^2}{2} + 2x - 3$$

13.16 problem 21

Internal problem ID [726]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 21.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$y'' - 2y'x + \lambda y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 63

Order:=6; dsolve(diff(y(x),x\$2)-2*x*diff(y(x),x)+lambda*y(x)=0,y(x),type='series',x=0);

$$y(x) = \left(1 - \frac{\lambda x^2}{2} + \frac{\lambda(\lambda - 4) x^4}{24}\right) y(0) + \left(x - \frac{(\lambda - 2) x^3}{6} + \frac{(\lambda - 2) (-6 + \lambda) x^5}{120}\right) D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 80

 $AsymptoticDSolveValue[y''[x]-2*x*y'[x]+\\[Lambda]*y[x]==0,y[x],\{x,0,5\}]$

$$y(x)
ightarrow c_2 \left(rac{\lambda^2 x^5}{120} - rac{\lambda x^5}{15} + rac{x^5}{10} - rac{\lambda x^3}{6} + rac{x^3}{3} + x
ight) + c_1 \left(rac{\lambda^2 x^4}{24} - rac{\lambda x^4}{6} - rac{\lambda x^2}{2} + 1
ight)$$

13.17 problem 23

Internal problem ID [727]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 23.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _homogeneous]]

$$y'' - y'x - y = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = 0]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 14

Time about one (bee). Boar size: 11

Order:=6; dsolve([diff(y(x),x\$2)-x*diff(y(x),x)-y(x)=0,y(0) = 1, D(y)(0) = 0],y(x),type='series',x=0);

$$y(x) = 1 + \frac{1}{2}x^2 + \frac{1}{8}x^4 + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 19

$$y(x) \to \frac{x^4}{8} + \frac{x^2}{2} + 1$$

13.18 problem 24

Internal problem ID [728]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 24.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(x^2 + 2) y'' - y'x + 4y = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = 0]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 14

Order:=6; $dsolve([(2+x^2)*diff(y(x),x$2)-x*diff(y(x),x)+4*y(x)=0,y(0) = 1, D(y)(0) = 0],y(x),type='seri'$

$$y(x) = 1 - x^2 + \frac{1}{6}x^4 + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 17

AsymptoticDSolveValue[$\{(2+x^2)*y''[x]-x*y'[x]+4*y[x]==0,\{y[0]==1,y'[0]==0\}\},y[x],\{x,0,5\}$]

$$y(x) \to \frac{x^4}{6} - x^2 + 1$$

13.19 problem 25

Internal problem ID [729]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 25.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$y'' + y'x + 2y = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Order:=6;

Time used: 0.0 (sec). Leaf size: 14

Time about 0.0 (Boo). Boot Bize. II

dsolve([diff(y(x),x\$2)+x*diff(y(x),x)+2*y(x)=0,y(0) = 0, D(y)(0) = 1],y(x),type='series',x=0)

$$y(x) = x - \frac{1}{2}x^3 + \frac{1}{8}x^5 + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 19

 $\label{eq:asymptoticDSolveValue} A symptotic DSolveValue [\{y''[x]+x*y'[x]+2*y[x]==0,\{y[0]==0,y'[0]==1\}\},y[x],\{x,0,5\}]$

$$y(x) \to \frac{x^5}{8} - \frac{x^3}{2} + x$$

13.20 problem 26

Internal problem ID [730]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 26.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(-x^2 + 4) y'' + y'x + 2y = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 14

Order:=6;

dsolve([(4-x^2)*diff(y(x),x\$2)+x*diff(y(x),x)+2*y(x)=0,y(0) = 0, D(y)(0) = 1],y(x),type='seri

$$y(x) = x - \frac{1}{8}x^3 - \frac{1}{640}x^5 + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 19

AsymptoticDSolveValue[$\{(4-x^2)*y''[x]+x*y'[x]+2*y[x]==0,\{y[0]==0,y'[0]==1\}\},y[x],\{x,0,5\}$]

$$y(x) \to -\frac{x^5}{640} - \frac{x^3}{8} + x$$

13.21 problem 27

Internal problem ID [731]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 27.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$y'' + x^2y = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = 0]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 12

Order:=6; $dsolve([diff(y(x),x$2)+x^2*y(x)=0,y(0) = 1, D(y)(0) = 0],y(x),type='series',x=0);$

$$y(x) = 1 - \frac{1}{12}x^4 + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 12

AsymptoticDSolveValue[$\{y''[x]+x^2*y[x]==0,\{y[0]==1,y'[0]==0\}\},y[x],\{x,0,5\}$]

$$y(x) \to 1 - \frac{x^4}{12}$$

13.22 problem 28

Internal problem ID [732]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 5.2, Series Solutions Near an Ordinary Point, Part I. page 263

Problem number: 28.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries], [_2nd_order, _linear, '

$$(1-x)y'' + y'x - 2y = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 16

Order:=6;

dsolve([(1-x)*diff(y(x),x\$2)+x*diff(y(x),x)-2*y(x)=0,y(0) = 0, D(y)(0) = 1],y(x), type='series

$$y(x) = x + \frac{1}{6}x^3 + \frac{1}{12}x^4 + \frac{1}{24}x^5 + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 26

AsymptoticDSolveValue[$\{(1-x)*y''[x]+x*y'[x]-2*y[x]==0,\{y[0]==0,y'[0]==1\}\},y[x],\{x],0,5\}$]

$$y(x) \to \frac{x^5}{24} + \frac{x^4}{12} + \frac{x^3}{6} + x$$

14 Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

14.1 problem 1
14.2 problem 2
14.3 problem 3
14.4 problem 4
14.5 problem 5. case $x_0 = 0 \dots 32$
14.6 problem 5. case $x_0=4$
14.7 problem 6. case $x_0 = 0 \dots 32$
14.8 problem 6. case $x_0 = 4$ only $\dots 32$
14.9 problem 6. case $x_0 = -4$
14.10 problem 7. case $x_0 = 0 \ldots 33$
14.11 problem 7. case $x_0 = 2 \dots 33$
14.12 problem 8
14.13 problem 10
14.14 problem 16
14.15 problem 17
14.16 problem 19
14.17 problem 22

14.1 problem 1

Internal problem ID [733]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 1.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _homogeneous]]

$$y'' + y'x + y = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = 0]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 14

Order:=6; dsolve([diff(y(x),x\$2)+x*diff(y(x),x)+y(x)=0,y(0) = 1, D(y)(0) = 0],y(x),type='series',x=0);

$$y(x) = 1 - \frac{1}{2}x^2 + \frac{1}{8}x^4 + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 19

$$y(x) \to \frac{x^4}{8} - \frac{x^2}{2} + 1$$

14.2 problem 2

Internal problem ID [734]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 2.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _exact, _linear, _homogeneous]]

$$y'' + \sin(x)y' + \cos(x)y = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 14

Order:=6;

dsolve([diff(y(x),x\$2)+sin(x)*diff(y(x),x)+cos(x)*y(x)=0,y(0) = 0, D(y)(0) = 1],y(x),type='se

$$y(x) = x - \frac{1}{3}x^3 + \frac{1}{10}x^5 + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 19

AsymptoticDSolveValue[$\{y''[x]+Sin[x]*y'[x]+Cos[x]*y[x]==0,\{y[0]==0,y'[0]==1\}\},y[x],\{x,0,5\}$]

$$y(x) \to \frac{x^5}{10} - \frac{x^3}{3} + x$$

14.3 problem 3

Internal problem ID [735]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 3.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$x^{2}y'' + (x+1)y' + 3\ln(x)y = 0$$

With initial conditions

$$[y(1) = 2, y'(1) = 0]$$

With the expansion point for the power series method at x = 1.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 16

Order:=6;

 $\frac{\text{dsolve}([x^2*\text{diff}(y(x),x\$2)+(1+x)*\text{diff}(y(x),x)+3*\text{ln}(x)*y(x)=0,y(1)=2,\ D(y)(1)=0],y(x),\text{type}}{\text{dsolve}([x^2*\text{diff}(y(x),x\$2)+(1+x)*\text{diff}(y(x),x)+3*\text{ln}(x)*y(x)=0,y(1)=2,\ D(y)(1)=0],y(x),\text{type}}$

$$y(x) = 2 - (x - 1)^3 + \frac{7}{4}(x - 1)^4 - \frac{49}{20}(x - 1)^5 + O((x - 1)^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 30

AsymptoticDSolveValue[$\{x^2*y''[x]+(1+x)*y'[x]+3*Log[x]*y[x]==0,\{y[1]==2,y'[1]==0\}$ },y[x], $\{x,1,y''[x]=0$

$$y(x) \rightarrow -\frac{49}{20}(x-1)^5 + \frac{7}{4}(x-1)^4 - (x-1)^3 + 2$$

14.4 problem 4

Internal problem ID [736]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 4.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$y'' + y'x^2 + \sin(x)y = 0$$

With initial conditions

$$[y(0) = a_0, y'(0) = a_1]$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 24

Order:=6; dsolve([diff(y(x),x\$2)+x^2*diff(y(x),x)+sin(x)*y(x)=0,y(0) = a__0, D(y)(0) = a__1],y(x),type=

$$y(x) = a_0 + a_1 x - \frac{1}{6}a_0 x^3 - \frac{1}{6}a_1 x^4 + \frac{1}{120}a_0 x^5 + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 32

AsymptoticDSolveValue[$\{y''[x]+x^2*y'[x]+Sin[x]*y[x]==0,\{y[0]==a0,y'[0]==a1\}\},y[x],\{x,0,5\}$]

$$y(x) \rightarrow \frac{a0x^5}{120} - \frac{a0x^3}{6} + a0 - \frac{a1x^4}{6} + a1x$$

14.5 problem **5.** case $x_0 = 0$

Internal problem ID [737]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 5. case $x_0 = 0$.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$y'' + 4y' + 6yx = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 47

Order:=6; dsolve(diff(y(x),x\$2)+4*diff(y(x),x)+6*x*y(x)=0,y(x),type='series',x=0);

$$y(x) = \left(1 - x^3 + x^4 - \frac{4}{5}x^5\right)y(0) + \left(x - 2x^2 + \frac{8}{3}x^3 - \frac{19}{6}x^4 + \frac{47}{15}x^5\right)D(y)\left(0\right) + O\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 55

AsymptoticDSolveValue[$y''[x]+4*y'[x]+6*x*y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \rightarrow c_1 \left(-\frac{4x^5}{5} + x^4 - x^3 + 1 \right) + c_2 \left(\frac{47x^5}{15} - \frac{19x^4}{6} + \frac{8x^3}{3} - 2x^2 + x \right)$$

14.6 problem **5.** case $x_0 = 4$

Internal problem ID [738]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 5. case $x_0 = 4$.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$y'' + 4y' + 6yx = 0$$

With the expansion point for the power series method at x = 4.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 54

Order:=6; dsolve(diff(y(x),x\$2)+4*diff(y(x),x)+6*x*y(x)=0,y(x),type='series',x=4);

$$y(x) = \left(1 - 12(x - 4)^2 + 15(x - 4)^3 + 9(x - 4)^4 - \frac{108(x - 4)^5}{5}\right)y(4)$$
$$+ \left(x - 4 - 2(x - 4)^2 - \frac{4(x - 4)^3}{3} + \frac{29(x - 4)^4}{6} - \frac{5(x - 4)^5}{3}\right)D(y)(4) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 79

 $A symptotic D Solve Value [y''[x]+4*y'[x]+6*x*y[x]==0,y[x],\{x,4,5\}]$

$$y(x) \to c_1 \left(-\frac{108}{5} (x-4)^5 + 9(x-4)^4 + 15(x-4)^3 - 12(x-4)^2 + 1 \right)$$
$$+ c_2 \left(-\frac{5}{3} (x-4)^5 + \frac{29}{6} (x-4)^4 - \frac{4}{3} (x-4)^3 - 2(x-4)^2 + x - 4 \right)$$

14.7 problem 6. case $x_0 = 0$

Internal problem ID [739]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 6. case $x_0 = 0$.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(x^2 - 2x - 3)y'' + y'x + 4y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 49

Order:=6; $dsolve((x^2-2*x-3)*diff(y(x),x$2)+x*diff(y(x),x)+4*y(x)=0,y(x),type='series',x=0);$

$$y(x) = \left(1 + \frac{2}{3}x^2 - \frac{4}{27}x^3 + \frac{16}{81}x^4 - \frac{1}{9}x^5\right)y(0) + \left(x + \frac{5}{18}x^3 - \frac{5}{54}x^4 + \frac{7}{72}x^5\right)D(y)\left(0\right) + O\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 63

AsymptoticDSolveValue[$(x^2-2*x-3)*y''[x]+x*y'[x]+4*y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \rightarrow c_2 \left(\frac{7x^5}{72} - \frac{5x^4}{54} + \frac{5x^3}{18} + x\right) + c_1 \left(-\frac{x^5}{9} + \frac{16x^4}{81} - \frac{4x^3}{27} + \frac{2x^2}{3} + 1\right)$$

14.8 problem **6.** case $x_0 = 4$ only

Internal problem ID [740]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 6. case $x_0 = 4$ only.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(x^2 - 2x - 3)y'' + y'x + 4y = 0$$

With the expansion point for the power series method at x = 4.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 54

Order:=6; $dsolve((x^2-2*x-3)*diff(y(x),x$2)+x*diff(y(x),x)+4*y(x)=0,y(x),type='series',x=4);$

$$y(x) = \left(1 - \frac{2(x-4)^2}{5} + \frac{4(x-4)^3}{15} - \frac{4(x-4)^4}{25} + \frac{199(x-4)^5}{1875}\right)y(4)$$

$$+ \left(x - 4 - \frac{2(x-4)^2}{5} + \frac{(x-4)^3}{10} - \frac{2(x-4)^4}{75} + \frac{157(x-4)^5}{15000}\right)D(y)(4) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 87

$$y(x) \to c_1 \left(\frac{199(x-4)^5}{1875} - \frac{4}{25}(x-4)^4 + \frac{4}{15}(x-4)^3 - \frac{2}{5}(x-4)^2 + 1 \right)$$

+ $c_2 \left(\frac{157(x-4)^5}{15000} - \frac{2}{75}(x-4)^4 + \frac{1}{10}(x-4)^3 - \frac{2}{5}(x-4)^2 + x - 4 \right)$

14.9 problem 6. case $x_0 = -4$

Internal problem ID [741]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 6. case $x_0 = -4$.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(x^2 - 2x - 3)y'' + y'x + 4y = 0$$

With the expansion point for the power series method at x = -4.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 54

Order:=6; $dsolve((x^2-2*x-3)*diff(y(x),x$2)+x*diff(y(x),x)+4*y(x)=0,y(x),type='series',x=-4);$

$$y(x) = \left(1 - \frac{2(x+4)^2}{21} - \frac{4(x+4)^3}{189} - \frac{4(x+4)^4}{1323} - \frac{(x+4)^5}{3087}\right)y(-4) + \left(x+4 + \frac{2(x+4)^2}{21} - \frac{(x+4)^3}{54} - \frac{11(x+4)^4}{1323} - \frac{157(x+4)^5}{74088}\right)D(y)(-4) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 87

AsymptoticDSolveValue[$(x^2-2*x-3)*y''[x]+x*y'[x]+4*y[x]==0,y[x],\{x,-4,5\}$]

$$y(x) \to c_1 \left(-\frac{(x+4)^5}{3087} - \frac{4(x+4)^4}{1323} - \frac{4}{189}(x+4)^3 - \frac{2}{21}(x+4)^2 + 1 \right)$$

+ $c_2 \left(-\frac{157(x+4)^5}{74088} - \frac{11(x+4)^4}{1323} - \frac{1}{54}(x+4)^3 + \frac{2}{21}(x+4)^2 + x + 4 \right)$

14.10 problem 7. case $x_0 = 0$

Internal problem ID [742]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 7. case $x_0 = 0$.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(x^3 + 1) y'' + 4y'x + y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 39

Order:=6; $dsolve((1+x^3)*diff(y(x),x$2)+4*x*diff(y(x),x)+y(x)=0,y(x),type='series',x=0);$

$$y(x) = \left(1 - \frac{1}{2}x^2 + \frac{3}{8}x^4 + \frac{1}{20}x^5\right)y(0) + \left(x - \frac{5}{6}x^3 + \frac{13}{24}x^5\right)D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 49

AsymptoticDSolveValue[$(1+x^3)*y''[x]+4*x*y'[x]+y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \rightarrow c_2 \left(\frac{13x^5}{24} - \frac{5x^3}{6} + x\right) + c_1 \left(\frac{x^5}{20} + \frac{3x^4}{8} - \frac{x^2}{2} + 1\right)$$

14.11 problem 7. case $x_0 = 2$

Internal problem ID [743]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 7. case $x_0 = 2$.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_2nd_order, _with_linear_symmetries]]

$$(x^3 + 1) y'' + 4y'x + y = 0$$

With the expansion point for the power series method at x = 2.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 54

Order:=6; dsolve($(1+x^3)*diff(y(x),x$2)+4*x*diff(y(x),x)+y(x)=0,y(x),type='series',x=2);$

$$y(x) = \left(1 - \frac{(-2+x)^2}{18} + \frac{10(-2+x)^3}{243} - \frac{451(-2+x)^4}{17496} + \frac{1151(-2+x)^5}{78732}\right)y(2)$$

$$+ \left(-2 + x - \frac{4(-2+x)^2}{9} + \frac{115(-2+x)^3}{486} - \frac{271(-2+x)^4}{2187} + \frac{9713(-2+x)^5}{157464}\right)D(y)(2)$$

$$+ O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 87

AsymptoticDSolveValue[$(1+x^3)*y''[x]+4*x*y'[x]+y[x]==0,y[x],\{x,2,5\}$]

$$y(x) \to c_1 \left(\frac{1151(x-2)^5}{78732} - \frac{451(x-2)^4}{17496} + \frac{10}{243}(x-2)^3 - \frac{1}{18}(x-2)^2 + 1 \right)$$
$$+ c_2 \left(\frac{9713(x-2)^5}{157464} - \frac{271(x-2)^4}{2187} + \frac{115}{486}(x-2)^3 - \frac{4}{9}(x-2)^2 + x - 2 \right)$$

14.12 problem 8

Internal problem ID [744]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 8.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$xy'' + y = 0$$

With the expansion point for the power series method at x = 1.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 49

Order:=6; dsolve(x*diff(y(x),x\$2)+y(x)=0,y(x),type='series',x=1);

$$y(x) = \left(1 - \frac{(x-1)^2}{2} + \frac{(x-1)^3}{6} - \frac{(x-1)^4}{24} + \frac{(x-1)^5}{60}\right)y(1) + \left(x - 1 - \frac{(x-1)^3}{6} + \frac{(x-1)^4}{12} - \frac{(x-1)^5}{24}\right)D(y)(1) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 78

AsymptoticDSolveValue[$x*y''[x]+y[x]==0,y[x],\{x,1,5\}$]

$$y(x) \to c_1 \left(\frac{1}{60} (x-1)^5 - \frac{1}{24} (x-1)^4 + \frac{1}{6} (x-1)^3 - \frac{1}{2} (x-1)^2 + 1 \right)$$
$$+ c_2 \left(-\frac{1}{24} (x-1)^5 + \frac{1}{12} (x-1)^4 - \frac{1}{6} (x-1)^3 + x - 1 \right)$$

14.13 problem 10

Internal problem ID [745]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 10.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [_Gegenbauer, [_2nd_order, _linear, '_with_symmetry_[0,F(x)]']]

$$(-x^{2}+1)y'' - y'x + \alpha^{2}y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 71

Order:=6; $dsolve((1-x^2)*diff(y(x),x$2)-x*diff(y(x),x)+alpha^2*y(x)=0,y(x),type='series',x=0);$

$$y(x) = \left(1 - \frac{\alpha^2 x^2}{2} + \frac{\alpha^2 (\alpha^2 - 4) x^4}{24}\right) y(0) + \left(x - \frac{(\alpha^2 - 1) x^3}{6} + \frac{(\alpha^4 - 10\alpha^2 + 9) x^5}{120}\right) D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 88

 $AsymptoticDSolveValue[(1-x^2)*y''[x]-x*y'[x]+\\[Alpha]^2*y[x]==0,y[x],\{x,0,5\}]$

$$y(x)
ightarrow c_2 \left(rac{lpha^4 x^5}{120} - rac{lpha^2 x^5}{12} + rac{3 x^5}{40} - rac{lpha^2 x^3}{6} + rac{x^3}{6} + x
ight) + c_1 \left(rac{lpha^4 x^4}{24} - rac{lpha^2 x^4}{6} - rac{lpha^2 x^2}{2} + 1
ight)$$

14.14 problem 16

Internal problem ID [746]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 16.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 34

Order:=6;
dsolve(diff(y(x),x)-y(x)=0,y(x),type='series',x=0);

$$y(x) = \left(1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5\right)y(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 37

AsymptoticDSolveValue[$y'[x]-y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \to c_1 \left(\frac{x^5}{120} + \frac{x^4}{24} + \frac{x^3}{6} + \frac{x^2}{2} + x + 1 \right)$$

14.15 problem 17

Internal problem ID [747]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 17.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [_separable]

$$-yx + y' = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 21

Order:=6; dsolve(diff(y(x),x)-x*y(x)=0,y(x),type='series',x=0);

$$y(x) = \left(1 + \frac{1}{2}x^2 + \frac{1}{8}x^4\right)y(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 22

AsymptoticDSolveValue[$y'[x]-x*y[x]==0,y[x],\{x,0,5\}$]

$$y(x) \to c_1 \left(\frac{x^4}{8} + \frac{x^2}{2} + 1 \right)$$

14.16 problem 19

Internal problem ID [748]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 19.

ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y'(1-x) - y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 26

Order:=6; dsolve((1-x)*diff(y(x),x)=y(x),y(x),type='series',x=0);

$$y(x) = (x^5 + x^4 + x^3 + x^2 + x + 1) y(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 21

AsymptoticDSolveValue[$(1-x)*y'[x]==y[x],y[x],\{x,0,5\}$]

$$y(x) \to c_1 (x^5 + x^4 + x^3 + x^2 + x + 1)$$

14.17 problem 22

Internal problem ID [749]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 5.3, Series Solutions Near an Ordinary Point, Part II. page 269

Problem number: 22.

ODE order: 2. ODE degree: 1.

CAS Maple gives this as type [_Gegenbauer]

$$(-x^{2}+1) y'' - 2y'x + \alpha(\alpha+1) y = 0$$

With the expansion point for the power series method at x = 0.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 101

Order:=6; dsolve((1-x^2)*diff(y(x),x\$2)-2*x*diff(y(x),x)+alpha*(alpha+1)*y(x)=0,y(x),type='series',x=0)

$$y(x) = \left(1 - \frac{\alpha(1+\alpha)x^{2}}{2} + \frac{\alpha(\alpha^{3} + 2\alpha^{2} - 5\alpha - 6)x^{4}}{24}\right)y(0) + \left(x - \frac{(\alpha^{2} + \alpha - 2)x^{3}}{6} + \frac{(\alpha^{4} + 2\alpha^{3} - 13\alpha^{2} - 14\alpha + 24)x^{5}}{120}\right)D(y)(0) + O(x^{6})$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 127

$$y(x) \to c_2 \left(\frac{1}{60} \left(-\alpha^2 - \alpha \right) x^5 - \frac{1}{120} \left(-\alpha^2 - \alpha \right) \left(\alpha^2 + \alpha \right) x^5 - \frac{1}{10} \left(\alpha^2 + \alpha \right) x^5 + \frac{x^5}{5} - \frac{1}{6} \left(\alpha^2 + \alpha \right) x^3 + \frac{x^3}{3} + x \right) + c_1 \left(\frac{1}{24} \left(\alpha^2 + \alpha \right)^2 x^4 - \frac{1}{4} \left(\alpha^2 + \alpha \right) x^4 - \frac{1}{2} \left(\alpha^2 + \alpha \right) x^2 + 1 \right)$$

15	Chapter 7.5, Homogeneous Linear Systems with	1												
Constant Coefficients. page 407														
15.1	problem 30	340												

15.1 problem 30

Internal problem ID [750]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.5, Homogeneous Linear Systems with Constant Coefficients. page 407

Problem number: 30.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = -\frac{x_1(t)}{10} + \frac{3x_2(t)}{40}$$
$$x'_2(t) = \frac{x_1(t)}{10} - \frac{x_2(t)}{5}$$

With initial conditions

$$[x_1(0) = -17, x_2(0) = -21]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 34

 $dsolve([diff(x_1(t),t) = -1/10*x_1(t)+3/40*x_2(t), diff(x_2(t),t) = 1/10*x_1(t)-1/5*x_2(t), diff(x_1(t),t) = 1/10*x_1(t)-1/5*x_1(t)-1/5*x_2(t), diff(x_1(t),t) = 1/10*x_1(t)-1/5*x_1(t)$

$$x_1(t) = \frac{29 e^{-\frac{t}{4}}}{8} - \frac{165 e^{-\frac{t}{20}}}{8}$$

$$x_2(t) = -\frac{29 e^{-\frac{t}{4}}}{4} - \frac{55 e^{-\frac{t}{20}}}{4}$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 52

DSolve[{x1'[t]==-1/10*x1[t]+3/40*x2[t],x2'[t]==1/10*x1[t]-1/5*x2[t]},{x1[0]==-17,x2[0]==-21},

$$x1(t) \rightarrow \frac{1}{8}e^{-t/4}(29 - 165e^{t/5})$$

$$x2(t) \rightarrow -\frac{1}{4}e^{-t/4}(55e^{t/5} + 29)$$

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16.1 problem 1

Internal problem ID [751]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 1.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = 3x_1(t) - 2x_2(t)$$

$$x'_2(t) = 4x_1(t) - x_2(t)$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 54

$$x_1(t) = \frac{e^t(c_1 \sin(2t) - c_2 \sin(2t) + c_1 \cos(2t) + c_2 \cos(2t))}{2}$$

$$x_2(t) = e^t(c_1 \sin(2t) + c_2 \cos(2t))$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 58

$$x1(t) \to e^t(c_1 \cos(2t) + (c_1 - c_2)\sin(2t))$$

 $x2(t) \to e^t(c_2 \cos(2t) + (2c_1 - c_2)\sin(2t))$

16.2 problem 2

Internal problem ID [752]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 2.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = -x_1(t) - 4x_2(t)$$

$$x'_2(t) = x_1(t) - x_2(t)$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 46

 $dsolve([diff(x_1(t),t)=-1*x_1(t)-4*x_2(t),diff(x_2(t),t)=1*x_1(t)-1*x_2(t)],[x_1(t),x_2(t)]$

$$x_1(t) = -2e^{-t}(c_2\sin(2t) - c_1\cos(2t))$$

$$x_2(t) = e^{-t}(c_1 \sin(2t) + c_2 \cos(2t))$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 55

DSolve[{x1'[t]==-1*x1[t]-4*x2[t],x2'[t]==1*x1[t]-1*x2[t]},{x1[t],x2[t]},t,IncludeSingularSolu

$$x1(t) \to e^{-t}(c_1 \cos(2t) - 2c_2 \sin(2t))$$

$$x2(t) \rightarrow \frac{1}{2}e^{-t}(2c_2\cos(2t) + c_1\sin(2t))$$

16.3 problem 3

Internal problem ID [753]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 3.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = 2x_1(t) - 5x_2(t)$$

$$x_2'(t) = x_1(t) - 2x_2(t)$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 37

 $dsolve([diff(x_{1}(t),t)=2*x_{1}(t)-5*x_{2}(t),diff(x_{2}(t),t)=1*x_{1}(t)-2*x_{2}(t)],[x_{1}(t),x_{2}(t),t)=1*x_{2}(t),t)=1*x_{3}(t)-2*x_{4}(t),t)=1*x_{4}(t)-2*x_{4}(t),t)=1*x_{4}(t)-2*x_{4}(t)-2*x_{4}(t),t)=1*x_{4}(t)-2*x_{4}(t)-2*x_{4}(t),t)=1*x_{4}(t)-2*x_{4$

$$x_1(t) = \cos(t) c_1 - c_2 \sin(t) + 2c_1 \sin(t) + 2c_2 \cos(t)$$

$$x_2(t) = c_1 \sin(t) + c_2 \cos(t)$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 41

DSolve[{x1'[t]==2*x1[t]-5*x2[t],x2'[t]==1*x1[t]-2*x2[t]},{x1[t],x2[t]},t,IncludeSingularSolut

$$x1(t) \to c_1(2\sin(t) + \cos(t)) - 5c_2\sin(t)$$

$$x2(t) \rightarrow c_2 \cos(t) + (c_1 - 2c_2) \sin(t)$$

16.4 problem 4

Internal problem ID [754]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 4.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = 2x_1(t) - \frac{5x_2(t)}{2}$$
$$x_2'(t) = \frac{9x_1(t)}{5} - x_2(t)$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 58

 $dsolve([diff(x_1(t),t)=2*x_1(t)-5/2*x_2(t),diff(x_2(t),t)=9/5*x_1(t)-1*x_2(t)],[x_1(t)-1*x_2(t)]$

$$x_1(t) = \frac{5 e^{\frac{t}{2}} \left(\sin\left(\frac{3t}{2}\right) c_1 - \sin\left(\frac{3t}{2}\right) c_2 + \cos\left(\frac{3t}{2}\right) c_1 + \cos\left(\frac{3t}{2}\right) c_2\right)}{6}$$

$$x_2(t) = e^{\frac{t}{2}} \left(\sin\left(\frac{3t}{2}\right) c_1 + \cos\left(\frac{3t}{2}\right) c_2 \right)$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 84

 $DSolve[{x1'[t] == 2*x1[t] - 5/2*x2[t], x2'[t] == 9/5*x1[t] - 1*x2[t]}, {x1[t], x2[t]}, t, IncludeSingularSin$

$$\mathrm{x1}(t)
ightarrow rac{1}{3} e^{t/2} igg(3c_1 \cos \left(rac{3t}{2}
ight) + (3c_1 - 5c_2) \sin \left(rac{3t}{2}
ight) igg)$$

$$x2(t) \rightarrow \frac{1}{5}e^{t/2} \left(5c_2 \cos\left(\frac{3t}{2}\right) + (6c_1 - 5c_2)\sin\left(\frac{3t}{2}\right)\right)$$

16.5 problem 5

Internal problem ID [755]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 5.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = x_1(t) - x_2(t)$$

$$x'_2(t) = 5x_1(t) - 3x_2(t)$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 48

$$x_1(t) = \frac{e^{-t}(\cos(t) c_1 - c_2 \sin(t) + 2c_1 \sin(t) + 2c_2 \cos(t))}{5}$$

$$x_2(t) = e^{-t}(c_1 \sin(t) + c_2 \cos(t))$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 55

$$x1(t) \to e^{-t}(c_1 \cos(t) + (2c_1 - c_2)\sin(t))$$

 $x2(t) \to e^{-t}(5c_1 \sin(t) + c_2(\cos(t) - 2\sin(t)))$

16.6 problem 6

Internal problem ID [756]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 6.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = x_1(t) + 2x_2(t)$$

$$x'_2(t) = -5x_1(t) - x_2(t)$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 50

$$x_1(t) = -\frac{3c_1\cos(3t)}{5} + \frac{3c_2\sin(3t)}{5} - \frac{c_1\sin(3t)}{5} - \frac{c_2\cos(3t)}{5}$$

$$x_2(t) = c_1 \sin(3t) + c_2 \cos(3t)$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 54

DSolve[{x1'[t]==1*x1[t]+2*x2[t],x2'[t]==-5*x1[t]-1*x2[t]},{x1[t],x2[t]},t,IncludeSingularSolu

$$x1(t) \rightarrow c_1 \cos(3t) + \frac{1}{3}(c_1 + 2c_2)\sin(3t)$$

$$x2(t) \rightarrow c_2 \cos(3t) - \frac{1}{3}(5c_1 + c_2)\sin(3t)$$

16.7 problem 7

Internal problem ID [757]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 7.

ODE order: 1.
ODE degree: 1.

Solve

$$x'_1(t) = x_1(t)$$

$$x'_2(t) = 2x_1(t) + x_2(t) - 2x_3(t)$$

$$x'_3(t) = 3x_1(t) + 2x_2(t) + x_3(t)$$

✓ Solution by Maple

Time used: 0.062 (sec). Leaf size: 54

$$dsolve([diff(x_1(t),t)=1*x_1(t)+0*x_2(t)+0*x_3(t),diff(x_2(t),t)=2*x_1(t)+1*x_2(t)-2*x_1(t)+1*x_2(t)+1*x_1(t)$$

$$x_1(t) = c_1 e^t$$

$$x_2(t) = -\frac{e^t(2c_3\sin(2t) - 2c_2\cos(2t) + 3c_1)}{2}$$

$$x_3(t) = e^t(c_2 \sin(2t) + c_3 \cos(2t) + c_1)$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 95

$$DSolve[{x1'[t] == 1*x1[t] + 0*x2[t] + 0*x3[t], x2'[t] == 2*x1[t] + 1*x2[t] - 2*x3[t], x3'[t] == 3*x1[t] + 2*x2[t] + 1*x2[t] + 1*x2[t]$$

$$x1(t) \to c_1 e^t$$

$$x2(t) \to \frac{1}{2} e^t ((3c_1 + 2c_2)\cos(2t) + 2(c_1 - c_3)\sin(2t) - 3c_1)$$

$$x3(t) \to \frac{1}{2} e^t (2(c_3 - c_1)\cos(2t) + (3c_1 + 2c_2)\sin(2t) + 2c_1)$$

16.8 problem 8

Internal problem ID [758]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 8.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = -3x_1(t) + 2x_3(t)$$

$$x'_2(t) = x_1(t) - x_2(t)$$

$$x'_3(t) = -2x_1(t) - x_2(t)$$

✓ Solution by Maple

Time used: 0.062 (sec). Leaf size: 174

$$dsolve([diff(x_{1}(t),t)=-3*x_{1}(t)+0*x_{2}(t)+2*x_{3}(t),diff(x_{2}(t),t)=1*x_{1}(t)-1*x_{2}(t)-0*x_{3}(t),diff(x_{1}(t),t)=1*x_{1}(t)-1*x_{2}(t)-0*x_{3}(t),diff(x_{1}(t),t)=1*x_{1}(t)-1*x_{2}(t)-0*x_{3}(t),diff(x_{1}(t),t)=1*x_{3}(t)-1*x_{4}(t)-1*x$$

$$x_1(t) = 2c_1 e^{-2t} + \frac{2c_2 e^{-t} \sin(t\sqrt{2})}{3} - \frac{c_2 e^{-t} \sqrt{2} \cos(t\sqrt{2})}{3} + \frac{2c_3 e^{-t} \cos(t\sqrt{2})}{3} + \frac{c_3 e^{-t} \sqrt{2} \sin(t\sqrt{2})}{3}$$

$$x_2(t) = -2c_1 e^{-2t} - \frac{c_2 e^{-t} \sin(t\sqrt{2})}{3} - \frac{c_2 e^{-t} \sqrt{2} \cos(t\sqrt{2})}{3} - \frac{c_3 e^{-t} \cos(t\sqrt{2})}{3} + \frac{c_3 e^{-t} \sqrt{2} \sin(t\sqrt{2})}{3}$$

$$x_3(t) = c_1 e^{-2t} + c_2 e^{-t} \sin(t\sqrt{2}) + c_3 e^{-t} \cos(t\sqrt{2})$$

✓ Solution by Mathematica

Time used: 0.039 (sec). Leaf size: 231

$$\begin{split} \mathbf{x}1(t) &\to \frac{1}{3}e^{-2t} \Big(e^t \Big((c_1 + 2(c_2 + c_3)) \cos \Big(\sqrt{2}t \Big) - \sqrt{2}(2c_1 + c_2 - 2c_3) \sin \Big(\sqrt{2}t \Big) \Big) + 2(c_1 - c_2 - c_3) \Big) \\ \mathbf{x}2(t) &\to \frac{1}{6}e^{-2t} \Big(e^t \Big(2(2c_1 + c_2 - 2c_3) \cos \Big(\sqrt{2}t \Big) + \sqrt{2}(c_1 + 2(c_2 + c_3)) \sin \Big(\sqrt{2}t \Big) \Big) \\ &\quad + 4(-c_1 + c_2 + c_3) \Big) \\ \mathbf{x}3(t) &\to \frac{1}{6}e^{-2t} \Big(e^t \Big(2(-c_1 + c_2 + 4c_3) \cos \Big(\sqrt{2}t \Big) + \sqrt{2}(-5c_1 - 4c_2 + 2c_3) \sin \Big(\sqrt{2}t \Big) \Big) \\ &\quad + 2(c_1 - c_2 - c_3) \Big) \end{split}$$

16.9 problem 9

Internal problem ID [759]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 9.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = x_1(t) - 5x_2(t)$$

$$x_2'(t) = x_1(t) - 3x_2(t)$$

With initial conditions

$$[x_1(0) = 1, x_2(0) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 32

 $dsolve([diff(x_1(t),t) = x_1(t)-5*x_2(t), diff(x_2(t),t) = x_1(t)-3*x_2(t), x_1(0) = 1)$

$$x_1(t) = e^{-t}(\cos(t) - 3\sin(t))$$

$$x_2(t) = e^{-t}(-\sin(t) + \cos(t))$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 34

DSolve[{x1'[t]==1*x1[t]-5*x2[t],x2'[t]==1*x1[t]-3*x2[t]},{x1[0]==1,x2[0]==1},{x1[t],x2[t]},t,

$$x1(t) \to e^{-t}(\cos(t) - 3\sin(t))$$

$$x2(t) \rightarrow e^{-t}(\cos(t) - \sin(t))$$

16.10 problem 10

Internal problem ID [760]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 10.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = -3x_1(t) + 2x_2(t)$$

$$x'_2(t) = -x_1(t) - x_2(t)$$

With initial conditions

$$[x_1(0) = 1, x_2(0) = -2]$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 37

 $dsolve([diff(x_1(t),t) = -3*x_1(t)+2*x_2(t), diff(x_2(t),t) = -x_1(t)-x_2(t), x_1(0) = -x_1(t)-x$

$$x_1(t) = -e^{-2t}(-\cos(t) + 5\sin(t))$$

$$x_2(t) = e^{-2t}(-3\sin(t) - 2\cos(t))$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 27

 $DSolve[{x1'[t] == -3*x1[t] + 2*x2[t], x2'[t] == -1*x1[t] - 1*x2[t]}, {x1[0] == 1, x2[0] == 1}, {x1[t], x2[t]},$

$$x1(t) \to e^{-2t}(\sin(t) + \cos(t))$$
$$x2(t) \to e^{-2t}\cos(t)$$

16.11 problem 11

Internal problem ID [761]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 11.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = \frac{3x_1(t)}{4} - 2x_2(t)$$

$$x_2'(t) = x_1(t) - \frac{5x_2(t)}{4}$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 45

 $dsolve([diff(x_1(t),t)=3/4*x_1(t)-2*x_2(t),diff(x_2(t),t)=1*x_1(t)-5/4*x_2(t)],[x_1(t)-2*x_2(t)]$

$$x_1(t) = e^{-\frac{t}{4}}(\cos(t) c_1 + c_2 \cos(t) + c_1 \sin(t) - c_2 \sin(t))$$

$$x_2(t) = e^{-\frac{t}{4}}(c_1 \sin(t) + c_2 \cos(t))$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 56

 $DSolve[{x1'[t] == 3/4*x1[t] - 2*x2[t], x2'[t] == 1*x1[t] - 5/4*x2[t]}, {x1[t], x2[t]}, t, IncludeSingularSin$

$$x1(t) \rightarrow e^{-t/4}(c_1 \cos(t) + (c_1 - 2c_2)\sin(t))$$

$$x2(t) \to e^{-t/4}(c_2\cos(t) + (c_1 - c_2)\sin(t))$$

16.12 problem 12

Internal problem ID [762]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 12.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = -\frac{4x_1(t)}{5} + 2x_2(t)$$
$$x_2'(t) = -x_1(t) + \frac{6x_2(t)}{5}$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 48

 $dsolve([diff(x_1(t),t)=-4/5*x_1(t)+2*x_2(t),diff(x_2(t),t)=-1*x_1(t)+6/5*x_2(t)],[x_1(t)+6/5*x_2(t)]$

$$x_1(t) = -e^{\frac{t}{5}}(\cos(t)c_1 - c_2\cos(t) - c_1\sin(t) - c_2\sin(t))$$

$$x_2(t) = e^{\frac{t}{5}}(c_1 \sin(t) + c_2 \cos(t))$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 56

DSolve[{x1'[t]==-4/5*x1[t]+2*x2[t],x2'[t]==-1*x1[t]+6/5*x2[t]},{x1[t],x2[t]},t,IncludeSingula

$$x1(t) \rightarrow e^{t/5}(c_1 \cos(t) - (c_1 - 2c_2)\sin(t))$$

$$x2(t) \rightarrow e^{t/5}(c_2(\sin(t) + \cos(t)) - c_1\sin(t))$$

16.13 problem 23

Internal problem ID [763]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 23.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = -\frac{x_1(t)}{4} + x_2(t)$$
$$x'_2(t) = -x_1(t) - \frac{x_2(t)}{4}$$
$$x'_3(t) = -\frac{x_3(t)}{4}$$

Solution by Maple

Time used: 0.031 (sec). Leaf size: 47

dsolve([diff(x_1(t),t)=-1/4*x_1(t)+1*x_2(t)+0*x_3(t),diff(x_2(t),t)=-1*x_1(t)-1/4*x_2(t)+0*x_3(t),diff(x_1(t),t)=-1*x_1(t)-1/4*x_2(t)+0*x_1(t)+1*x_2(t)+1*x_3(t)+1*x_1(t)+1*x_2(t)+1*x_3(t)+1*x

$$x_1(t) = -e^{-\frac{t}{4}}(\cos(t) c_1 - c_2 \sin(t))$$

$$x_2(t) = e^{-\frac{t}{4}}(c_1 \sin(t) + c_2 \cos(t))$$

$$x_3(t) = c_3 e^{-\frac{t}{4}}$$

✓ Solution by Mathematica

Time used: 0.021 (sec). Leaf size: 110

 $DSolve[{x1'[t] == -1/4*x1[t] + 1*x2[t] + 0*x3[t], x2'[t] == -1*x1[t] - 1/4*x2[t] + 0*x3[t], x3'}[t] == 0*x1[t]$

$$x1(t) \to e^{-t/4}(c_1 \cos(t) + c_2 \sin(t))$$

$$x2(t) \to e^{-t/4}(c_2 \cos(t) - c_1 \sin(t))$$

$$x3(t) \to c_3 e^{-t/4}$$

$$x1(t) \to e^{-t/4}(c_1 \cos(t) + c_2 \sin(t))$$

$$x2(t) \to e^{-t/4}(c_2 \cos(t) - c_1 \sin(t))$$

$$x3(t) \to 0$$

16.14 problem 24

Internal problem ID [764]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 24.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = -\frac{x_1(t)}{4} + x_2(t)$$
$$x'_2(t) = -x_1(t) - \frac{x_2(t)}{4}$$
$$x'_3(t) = \frac{x_3(t)}{10}$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 47

 $dsolve([diff(x_1(t),t)=-1/4*x_1(t)+1*x_2(t)+0*x_3(t),diff(x_2(t),t)=-1*x_1(t)-1/4*x_2(t)+0*x_3(t),diff(x_2(t),t)=-1*x_1(t)-1/4*x_2(t)+0*x_3(t)+0*$

$$x_1(t) = -e^{-\frac{t}{4}}(\cos(t) c_1 - c_2 \sin(t))$$

$$x_2(t) = e^{-\frac{t}{4}}(c_1 \sin(t) + c_2 \cos(t))$$

$$x_3(t) = c_3 e^{\frac{t}{10}}$$

✓ Solution by Mathematica

Time used: 0.022 (sec). Leaf size: 110

 $DSolve[{x1'[t] == -1/4*x1[t] + 1*x2[t] + 0*x3[t], x2'[t] == -1*x1[t] - 1/4*x2[t] + 0*x3[t], x3'}[t] == 0*x1[t]$

$$x1(t) \to e^{-t/4}(c_1 \cos(t) + c_2 \sin(t))$$

$$x2(t) \to e^{-t/4}(c_2 \cos(t) - c_1 \sin(t))$$

$$x3(t) \to c_3 e^{t/10}$$

$$x1(t) \to e^{-t/4}(c_1 \cos(t) + c_2 \sin(t))$$

$$x2(t) \to e^{-t/4}(c_2 \cos(t) - c_1 \sin(t))$$

$$x3(t) \to 0$$

16.15 problem 25

Internal problem ID [765]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.6, Complex Eigenvalues. page 417

Problem number: 25.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = -\frac{x_1(t)}{2} - \frac{x_2(t)}{8}$$
$$x'_2(t) = 2x_1(t) - \frac{x_2(t)}{2}$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 46

dsolve([diff(x_1(t),t)=-1/2*x_1(t)-1/8*x_2(t),diff(x_2(t),t)=2*x_1(t)-1/2*x_2(t)],[x_1

$$x_1(t) = \frac{e^{-\frac{t}{2}} \left(\cos\left(\frac{t}{2}\right) c_1 - \sin\left(\frac{t}{2}\right) c_2\right)}{4}$$

$$x_2(t) = \mathrm{e}^{-\frac{t}{2}} igg(c_2 \cos \left(rac{t}{2}
ight) + c_1 \sin \left(rac{t}{2}
ight) igg)$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 68

 $DSolve[{x1'[t]==-1/2*x1[t]-1/8*x2[t],x2'[t]==2*x1[t]-1/2*x2[t]},{x1[t],x2[t]},t,IncludeSingularing the context of the contex$

$$x1(t) \rightarrow \frac{1}{4}e^{-t/2}\left(4c_1\cos\left(\frac{t}{2}\right) - c_2\sin\left(\frac{t}{2}\right)\right)$$

$$x2(t) \rightarrow e^{-t/2} \left(c_2 \cos\left(\frac{t}{2}\right) + 4c_1 \sin\left(\frac{t}{2}\right) \right)$$

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17.1 problem 1

Internal problem ID [766]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.8, Repeated Eigenvalues. page 436

Problem number: 1.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = 3x_1(t) - 4x_2(t)$$

$$x_2'(t) = x_1(t) - x_2(t)$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 28

$$x_1(t) = e^t(2c_2t + 2c_1 + c_2)$$

$$x_2(t) = e^t(c_2t + c_1)$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 41

$$x1(t) \to e^t(2c_1t - 4c_2t + c_1)$$

$$x2(t) \to e^t((c_1 - 2c_2)t + c_2)$$

17.2 problem 2

Internal problem ID [767]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.8, Repeated Eigenvalues. page 436

Problem number: 2.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = 4x_1(t) - 2x_2(t)$$

$$x_2'(t) = 8x_1(t) - 4x_2(t)$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 24

 $dsolve([diff(x_{1}(t),t)=4*x_{1}(t)-2*x_{2}(t),diff(x_{2}(t),t)=8*x_{1}(t)-4*x_{2}(t)],[x_{1}(t),x_{2}(t)]$

$$x_1(t) = \frac{1}{8}c_1 + \frac{1}{2}c_1t + \frac{1}{2}c_2$$

$$x_2(t) = c_1 t + c_2$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 34

$$x1(t) \to 4c_1t - 2c_2t + c_1$$

$$x2(t) \rightarrow 8c_1t - 4c_2t + c_2$$

17.3 problem 3

Internal problem ID [768]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.8, Repeated Eigenvalues. page 436

Problem number: 3.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = -\frac{3x_1(t)}{2} + x_2(t)$$
$$x_2'(t) = -\frac{x_1(t)}{4} - \frac{x_2(t)}{2}$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 32

 $dsolve([diff(x_1(t),t)=-3/2*x_1(t)+1*x_2(t),diff(x_2(t),t)=-1/4*x_1(t)-1/2*x_2(t)],[x_1(t)+1/2*x_2(t)]$

$$x_1(t) = 2e^{-t}(c_2t + c_1 - 2c_2)$$

$$x_2(t) = e^{-t}(c_2t + c_1)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 52

 $DSolve[{x1'[t] == -3/2*x1[t] + 1*x2[t], x2'[t] == -1/4*x1[t] - 1/2*x2[t]}, {x1[t], x2[t]}, t, IncludeSingular = -1/4*x1[t] - 1/2*x2[t]}, {x1[t], x2[t]}, {$

$$x1(t) \to \frac{1}{2}e^{-t}(2c_2t - c_1(t-2))$$

$$x2(t) \to \frac{1}{4}e^{-t}(2c_2(t+2) - c_1t)$$

17.4 problem 4

Internal problem ID [769]

 \mathbf{Book} : Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.8, Repeated Eigenvalues. page 436

Problem number: 4.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = -3x_1(t) + \frac{5x_2(t)}{2}$$
$$x_2'(t) = -\frac{5x_1(t)}{2} + 2x_2(t)$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 35

dsolve([diff(x_1(t),t)=-3*x_1(t)+5/2*x_2(t),diff(x_2(t),t)=-5/2*x_1(t)+2*x_2(t)],[x_1(t)+2*x_2(t)]

$$x_1(t) = \frac{e^{-\frac{t}{2}}(5c_2t + 5c_1 - 2c_2)}{5}$$

$$x_2(t) = e^{-\frac{t}{2}}(c_2t + c_1)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 58

DSolve[{x1'[t]==-3*x1[t]+5/2*x2[t],x2'[t]==-5/2*x1[t]+2*x2[t]},{x1[t],x2[t]},t,IncludeSingula

$$x1(t) \to \frac{1}{2}e^{-t/2}(c_1(2-5t) + 5c_2t)$$

$$x2(t) \rightarrow \frac{1}{2}e^{-t/2}(c_2(5t+2) - 5c_1t)$$

17.5 problem 5

Internal problem ID [770]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.8, Repeated Eigenvalues. page 436

Problem number: 5.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = x_1(t) + x_2(t) + x_3(t)$$

$$x'_2(t) = 2x_1(t) + x_2(t) - x_3(t)$$

$$x'_3(t) = -x_2(t) + x_3(t)$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 76

$$x_1(t) = -\frac{3e^{-t}c_1}{2} - c_3e^{2t}$$

$$x_2(t) = 2e^{-t}c_1 - c_2e^{2t} - e^{2t}c_3t - c_3e^{2t}$$

$$x_3(t) = e^{-t}c_1 + c_2e^{2t} + e^{2t}c_3t$$

✓ Solution by Mathematica

Time used: 0.012 (sec). Leaf size: 151

DSolve[{x1'[t]==1*x1[t]+1*x2[t]+1*x3[t],x2'[t]==2*x1[t]+1*x2[t]-1*x3[t],x3'[t]==0*x1[t]-1*x2[

$$x1(t) \to \frac{1}{3}e^{-t} \left(c_1 \left(2e^{3t} + 1 \right) + \left(c_2 + c_3 \right) \left(e^{3t} - 1 \right) \right)$$

$$x2(t) \to \frac{1}{9}e^{-t} \left(e^{3t} \left(c_1 (6t + 4) + c_2 (3t + 5) + c_3 (3t - 4) \right) + 4(-c_1 + c_2 + c_3) \right)$$

$$x3(t) \to \frac{1}{9}e^{-t} \left(2(-c_1 + c_2 + c_3) - e^{3t} \left(c_1 (6t - 2) + c_2 (3t + 2) + c_3 (3t - 7) \right) \right)$$

17.6 problem 6

Internal problem ID [771]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.8, Repeated Eigenvalues. page 436

Problem number: 6.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = x_2(t) + x_3(t)$$

$$x_2'(t) = x_1(t) + x_3(t)$$

$$x_3'(t) = x_1(t) + x_2(t)$$

✓ Solution by Maple

Time used: 0.063 (sec). Leaf size: 64

 $dsolve([diff(x_1(t),t)=0*x_1(t)+1*x_2(t)+1*x_3(t),diff(x_2(t),t)=1*x_1(t)+0*x_2(t)+1*x_3(t),diff(x_2(t),t)=1*x_1(t)+0*x_2(t)+1*x_3(t)+0*x_1(t)+0*x_2(t)+1*x_3(t)+0*x_1(t)+0*x_2(t)+1*x_3(t)+0*x_1(t)+0*x_2(t)+1*x_3(t)+0*x_1(t)+0*x_2(t)+1*x_3(t)+0*x_1(t)+0*x_2(t)+1*x_3(t)+0*x_1(t)+0*x_1(t)+0*x_2(t)+0*x_1(t)+0*$

$$x_1(t) = c_2 e^{2t} - 2c_3 e^{-t} - e^{-t}c_1$$

$$x_2(t) = c_2 e^{2t} + c_3 e^{-t} + e^{-t} c_1$$

$$x_3(t) = c_2 e^{2t} + c_3 e^{-t}$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 114

DSolve[{x1'[t]==0*x1[t]+1*x2[t]+1*x3[t],x2'[t]==1*x1[t]+0*x2[t]+1*x3[t],x3'[t]==1*x1[t]+1*x2[

$$x1(t) \rightarrow \frac{1}{3}e^{-t}(c_1(e^{3t}+2)+(c_2+c_3)(e^{3t}-1))$$

$$x2(t) \rightarrow \frac{1}{3}e^{-t}((c_1+c_2+c_3)e^{3t}-c_1+2c_2-c_3)$$

$$x3(t) \rightarrow \frac{1}{3}e^{-t}((c_1+c_2+c_3)e^{3t}-c_1-c_2+2c_3)$$

17.7 problem 7

Internal problem ID [772]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.8, Repeated Eigenvalues. page 436

Problem number: 7.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = x_1(t) - 4x_2(t)$$

$$x_2'(t) = 4x_1(t) - 7x_2(t)$$

With initial conditions

$$[x_1(0) = 3, x_2(0) = 2]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 29

 $dsolve([diff(x_{1}(t),t) = x_{1}(t)-4*x_{2}(t), diff(x_{2}(t),t) = 4*x_{1}(t)-7*x_{2}(t), x_{1}(0) = 4*x_{1}(t)-7*x_{2}(t), x_{1}(0) = 4*x_{1}(t)-7*x_{2}(t), x_{1}(0) = 4*x_{1}(t)-7*x_{2}(t), x_{1}(0) = 4*x_{1}(t)-7*x_{2}(t), x_{1}(t)-7*x_{2}(t), x_{2}(t), x_{3}(t) = 4*x_{3}(t)-7*x_{4}(t)-7*x_{4}(t), x_{3}(t) = 4*x_{4}(t)-7*x_{4}(t)-7*x_{4}(t), x_{4}(t)-7*x_{4}(t), x_{4}(t)-7*x_{4}($

$$x_1(t) = \frac{e^{-3t}(16t + 12)}{4}$$

$$x_2(t) = e^{-3t}(4t+2)$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 34

 $DSolve[{x1'[t] == 1 * x1[t] - 4 * x2[t], x2'[t] == 1 * x1[t] - 4 * x2[t]}, {x1[0] == 3, x2[0] == 2}, {x1[t], x2[t]}, t, {x2[t], x2[t]}, {x2[t], x2[t]}, {x3[t], x2[t]}, {x3[t], x3[t]}, {x3[$

$$x1(t) \to \frac{5e^{-3t}}{3} + \frac{4}{3}$$

$$x2(t) \to \frac{5e^{-3t}}{3} + \frac{1}{3}$$

17.8 problem 8

Internal problem ID [773]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.8, Repeated Eigenvalues. page 436

Problem number: 8.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = -\frac{5x_1(t)}{2} + \frac{3x_2(t)}{2}$$
$$x'_2(t) = -\frac{3x_1(t)}{2} + \frac{x_2(t)}{2}$$

With initial conditions

$$[x_1(0) = 3, x_2(0) = -1]$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 29

dsolve([diff(x_1(t),t) = -5/2*x_1(t)+3/2*x_2(t), diff(x_2(t),t) = -3/2*x_1(t)+1/2*x_2(t)

$$x_1(t) = \frac{e^{-t}(-18t + 9)}{3}$$

$$x_2(t) = e^{-t}(-6t - 1)$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 31

DSolve[{x1'[t]==-5/2*x1[t]+3/2*x2[t],x2'[t]==-3/2*x1[t]+1/2*x2[t]},{x1[0]==3,x2[0]==-1},{x1[t]

$$x1(t) \to e^{-t}(3-6t)$$

$$x2(t) \to -e^{-t}(6t+1)$$

17.9 problem 9

Internal problem ID [774]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.8, Repeated Eigenvalues. page 436

Problem number: 9.

ODE order: 1.
ODE degree: 1.

Solve

$$x_1'(t) = 2x_1(t) + \frac{3x_2(t)}{2}$$
$$x_2'(t) = -\frac{3x_1(t)}{2} - x_2(t)$$

With initial conditions

$$[x_1(0) = 3, x_2(0) = -2]$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 29

 $dsolve([diff(x_1(t),t) = 2*x_1(t)+3/2*x_2(t), diff(x_2(t),t) = -3/2*x_1(t)-x_2(t), x_1(t)-x_2(t), x_2(t), x_3(t)-x_3(t)$

$$x_1(t) = -\frac{e^{\frac{t}{2}}\left(-\frac{9t}{2} - 9\right)}{3}$$

$$x_2(t) = e^{\frac{t}{2}} \left(-\frac{3t}{2} - 2 \right)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 38

DSolve[{x1'[t]==2*x1[t]+3/2*x2[t],x2'[t]==-3/2*x1[t]-1*x2[t]},{x1[0]==3,x2[0]==-2},{x1[t],x2[

$$x1(t) \to \frac{3}{2}e^{t/2}(t+2)$$

$$x2(t) \rightarrow -\frac{1}{2}e^{t/2}(3t+4)$$

17.10 problem 10

Internal problem ID [775]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 7.8, Repeated Eigenvalues. page 436

Problem number: 10.

ODE order: 1.
ODE degree: 1.

Solve

$$x_1'(t) = 3x_1(t) + 9x_2(t)$$

$$x_2'(t) = -x_1(t) - 3x_2(t)$$

With initial conditions

$$[x_1(0) = 2, x_2(0) = 4]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 18

$$dsolve([diff(x_1(t),t) = 3*x_1(t)+9*x_2(t), diff(x_2(t),t) = -x_1(t)-3*x_2(t), x_1(0))$$

$$x_1(t) = 42t + 2$$

$$x_2(t) = -14t + 4$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 18

$$DSolve[{x1'[t] == 3*x1[t] + 9*x2[t], x2'[t] == -1*x1[t] - 3*x2[t]}, {x1[0] == 2, x2[0] == 4}, {x1[t], x2[t]}, t= -1*x1[t] - 3*x2[t]}, {x1[0] == 2, x2[0] == 4}, {x1[t], x2[t]}, {x2[t]}, {x2[t]}, {x2[t]}, {x2[t]}, {x3[t], x2[t]}, {x3[t], x3[t]}, {x3[t],$$

$$x1(t) \rightarrow 42t + 2$$

$$x2(t) \rightarrow 4 - 14t$$

17.11 problem 11

Internal problem ID [776]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.8, Repeated Eigenvalues. page 436

Problem number: 11.

ODE order: 1.
ODE degree: 1.

Solve

$$x'_1(t) = x_1(t)$$

$$x'_2(t) = -4x_1(t) + x_2(t)$$

$$x'_3(t) = 3x_1(t) + 6x_2(t) + 2x_3(t)$$

With initial conditions

$$[x_1(0) = -1, x_2(0) = 2, x_3(0) = -30]$$

✓ Solution by Maple

Time used: 0.063 (sec). Leaf size: 40

$$dsolve([diff(x_1(t),t) = x_1(t), diff(x_2(t),t) = -4*x_1(t)+x_2(t), diff(x_3(t),t) = 3*$$

$$x_1(t) = -e^t$$

$$x_2(t) = -\frac{e^t(-192t - 96)}{48}$$

$$x_3(t) = 3e^{2t} - 33e^t - 24te^t$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 39

DSolve[{x1'[t]==1*x1[t]+0*x2[t]+0*x3[t],x2'[t]==-4*x1[t]+1*x2[t]+0*x3[t],x3'[t]==3*x1[t]+6*x2

$$\begin{aligned} &\mathbf{x}1(t) \rightarrow -e^t \\ &\mathbf{x}2(t) \rightarrow 2e^t(2t+1) \\ &\mathbf{x}3(t) \rightarrow 3e^t \big(-8t + e^t - 11 \big) \end{aligned}$$

17.12 problem 12

Internal problem ID [777]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.8, Repeated Eigenvalues. page 436

Problem number: 12.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = -\frac{5x_1(t)}{2} + x_2(t) + x_3(t)$$

$$x'_2(t) = x_1(t) - \frac{5x_2(t)}{2} + x_3(t)$$

$$x'_3(t) = x_1(t) + x_2(t) - \frac{5x_3(t)}{2}$$

With initial conditions

$$[x_1(0) = 2, x_2(0) = 3, x_3(0) = -1]$$

✓ Solution by Maple

Time used: 0.078 (sec). Leaf size: 50

$$dsolve([diff(x_1(t),t) = -5/2*x_1(t)+x_2(t)+x_3(t), diff(x_2(t),t) = x_1(t)-5/2*x_2(t)$$

$$x_1(t) = \frac{2e^{-\frac{7t}{2}}}{3} + \frac{4e^{-\frac{t}{2}}}{3}$$

$$x_2(t) = \frac{5e^{-\frac{7t}{2}}}{3} + \frac{4e^{-\frac{t}{2}}}{3}$$

$$x_3(t) = -\frac{7e^{-\frac{7t}{2}}}{3} + \frac{4e^{-\frac{t}{2}}}{3}$$

✓ Solution by Mathematica

Time used: 0.009 (sec). Leaf size: 71

DSolve[{x1'[t]==-5/2*x1[t]+1*x2[t]+1*x3[t],x2'[t]==1*x1[t]-5/2*x2[t]+1*x3[t],x3'[t]==1*x1[t]+

$$x1(t) \to \frac{2}{3}e^{-7t/2}(2e^{3t}+1)$$

$$x2(t) \to \frac{1}{3}e^{-7t/2}(4e^{3t} + 5)$$

$$x3(t) \to \frac{1}{3}e^{-7t/2}(4e^{3t} - 7)$$

18 Chapter 7.9, Nonhomogeneous Linear Systems. page 447

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18.1 problem 1

Internal problem ID [778]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 1.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = 2x_1(t) - x_2(t) + e^t$$

$$x'_2(t) = 3x_1(t) - 2x_2(t) + t$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 54

 $dsolve([diff(x_1(t),t)=2*x_1(t)-1*x_2(t)+exp(t),diff(x_2(t),t)=3*x_1(t)-2*x_2(t)+t],[x_1(t)-2*x_2(t)+t]$

$$x_1(t) = \frac{c_2 e^{-t}}{3} + c_1 e^t + \frac{3t e^t}{2} - \frac{e^t}{4} + t$$

$$x_2(t) = c_2 e^{-t} + c_1 e^t + \frac{3t e^t}{2} - \frac{3 e^t}{4} + 2t - 1$$

✓ Solution by Mathematica

Time used: 0.125 (sec). Leaf size: 86

DSolve[{x1'[t]==2*x1[t]-1*x2[t]+Exp[t],x2'[t]==3*x1[t]-2*x2[t]+t},{x1[t],x2[t]},t,IncludeSing

$$x1(t) \to t + \frac{1}{4}e^{t}(6t - 1 + 6c_1 - 2c_2) + \frac{1}{2}(c_2 - c_1)e^{-t}$$
$$x2(t) \to \frac{1}{4}(8t + e^{t}(6t - 3 + 6c_1 - 2c_2) - 6(c_1 - c_2)e^{-t} - 4)$$

18.2 problem 2

Internal problem ID [779]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 2.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = x_1(t) + \sqrt{3} x_2(t) + e^t$$

$$x_2'(t) = \sqrt{3} x_1(t) - x_2(t) + \sqrt{3} e^{-t}$$

✓ Solution by Maple

Time used: 0.125 (sec). Leaf size: 67

 $dsolve([diff(x_{1}(t),t)=1*x_{1}(t)+sqrt(3)*x_{2}(t)+exp(t),diff(x_{2}(t),t)=sqrt(3)*x_{1}(t)-1*x_{2}(t)+exp(t),diff(x_{3}(t),t)=sqrt(3)*x_{3}(t)-1*x_{4}(t)+sqrt(3)*x_{4}(t)+sqrt(5)*x_{4}(t)+sqrt(5)*x_{4}(t)+sqrt(5)*x_{4}(t)+$

$$x_1(t) = e^{2t}\sqrt{3}c_2 - \frac{e^{-2t}\sqrt{3}c_1}{3} - \frac{2e^t}{3} - e^{-t}$$

$$x_2(t) = c_2 e^{2t} + c_1 e^{-2t} + \frac{2\sqrt{3} e^{-t}}{3} - \frac{e^t \sqrt{3}}{3}$$

✓ Solution by Mathematica

Time used: 2.472 (sec). Leaf size: 240

DSolve[{x1'[t]==1*x1[t]+Sqrt[4]*x2[t]+Exp[t],x2'[t]==Sqrt[3]*x1[t]-1*x2[t]+Sqrt[3]*Exp[-t]},{

$$x1(t) \to -\frac{e^{t}}{\sqrt{3}} + \sinh(t) - \cosh(t) + c_{1} \cosh\left(\sqrt{1 + 2\sqrt{3}t}\right) + \frac{(c_{1} + 2c_{2}) \sinh\left(\sqrt{1 + 2\sqrt{3}t}\right)}{\sqrt{1 + 2\sqrt{3}}}$$

$$x2(t) \to \frac{1}{4} \left(4e^{-t} - 2e^{t} + \frac{2\left(\left(6 + \sqrt{3}\right)c_{1} + \left(1 + 2\sqrt{3}\right)\left(\sqrt{1 + 2\sqrt{3}} - 1\right)c_{2}\right)e^{\sqrt{1 + 2\sqrt{3}t}}}{\left(1 + 2\sqrt{3}\right)^{3/2}} + \frac{\left(2\left(1 + 2\sqrt{3}\right)\left(1 + \sqrt{1 + 2\sqrt{3}}\right)c_{2} - 2\left(6 + \sqrt{3}\right)c_{1}\right)e^{-\sqrt{1 + 2\sqrt{3}t}}}{\left(1 + 2\sqrt{3}\right)^{3/2}}\right)$$

18.3 problem 3

Internal problem ID [780]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 3.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = 2x_1(t) - 5x_2(t) - \cos(t)$$

$$x_2'(t) = x_1(t) - 2x_2(t) + \sin(t)$$

✓ Solution by Maple

Time used: 0.063 (sec). Leaf size: 59

$$dsolve([diff(x_{1}(t),t)=2*x_{1}(t)-5*x_{2}(t)-cos(t),diff(x_{2}(t),t)=1*x_{1}(t)-2*x_{2}(t)+sin(t))$$

$$x_1(t) = c_2 \cos(t) - c_1 \sin(t) - \sin(t) t + 2c_2 \sin(t) + 2\cos(t) c_1 - 3\sin(t) + 2\cos(t) t$$

$$x_2(t) = c_2 \sin(t) + \cos(t) c_1 - \sin(t) + \cos(t) t$$

✓ Solution by Mathematica

Time used: 0.072 (sec). Leaf size: 61

 $DSolve[{x1'[t] == 2*x1[t] - 5*x2[t] - Cos[t], x2'[t] == 1*x1[t] - 2*x2[t] + Sin[t]}, {x1[t], x2[t]}, t, Include the context of the context$

$$x1(t) \to \left(2t - \frac{1}{2} + c_1\right)\cos(t) - (t - 1 - 2c_1 + 5c_2)\sin(t)$$

$$x2(t) \to (t - 1 + c_2)\cos(t) + \frac{1}{2}(1 + 2c_1 - 4c_2)\sin(t)$$

18.4 problem 4

Internal problem ID [781]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 4.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = x_1(t) + x_2(t) + e^{-2t}$$

 $x'_2(t) = 4x_1(t) - 2x_2(t) - 2e^t$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 45

 $dsolve([diff(x_1(t),t)=1*x_1(t)+1*x_2(t)+exp(-2*t),diff(x_2(t),t)=4*x_1(t)-2*x_2(t)-2*exp(-2*t),diff(x_2(t),t)=4*x_1(t)-2*exp(-2*t),diff$

$$x_1(t) = c_2 e^{2t} - \frac{c_1 e^{-3t}}{4} + \frac{e^t}{2}$$

$$x_2(t) = c_2 e^{2t} + c_1 e^{-3t} - e^{-2t}$$

✓ Solution by Mathematica

Time used: 0.584 (sec). Leaf size: 84

DSolve[{x1'[t]==1*x1[t]+1*x2[t]+Exp[-2*t],x2'[t]==4*x1[t]-2*x2[t]-2*Exp[t]},{x1[t],x2[t]},t,I

$$x1(t) \to \frac{e^t}{2} + \frac{1}{5}(c_1 - c_2)e^{-3t} + \frac{1}{5}(4c_1 + c_2)e^{2t}$$

$$x2(t) \rightarrow \frac{1}{5}e^{-3t}(-5e^t + (4c_1 + c_2)e^{5t} - 4c_1 + 4c_2)$$

18.5 problem 5

Internal problem ID [782]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 5.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = 4x_1(t) - 2x_2(t) + \frac{1}{t^3}$$
$$x'_2(t) = 8x_1(t) - 4x_2(t) - \frac{1}{t^2}$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 47

 $dsolve([diff(x_1(t),t)=4*x_1(t)-2*x_2(t)+1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-4*x_2(t)-1/(t^3),diff(x_2(t),t)=8*x_1(t)-1/(t)$

$$x_1(t) = \frac{c_1 t}{2} - 2 \ln(t) + \frac{c_1}{8} + \frac{c_2}{2} + \frac{2}{t} - \frac{1}{2t^2}$$

$$x_2(t) = \frac{5}{t} - 4\ln(t) + c_1t + c_2$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 61

 $DSolve[{x1'[t] == 4*x1[t] - 2*x2[t] + 1/(t^3), x2'[t] == 8*x1[t] - 4*x2[t] - 1/(t^2)}, {x1[t], x2[t]}, t, Inclear = 0$

$$x1(t) \rightarrow -\frac{1}{2t^2} + \frac{2}{t} - 2\log(t) + 4c_1t - 2c_2t - 2 + c_1$$

$$x2(t) \rightarrow \frac{5}{t} - 4\log(t) + 8c_1t - 4c_2t - 4 + c_2$$

18.6 problem 6

Internal problem ID [783]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 6.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = -4x_1(t) + 2x_2(t) + \frac{1}{t}$$
$$x'_2(t) = 2x_1(t) - x_2(t) + \frac{2}{t} + 4$$

✓ Solution by Maple

Time used: 0.063 (sec). Leaf size: 45

$$dsolve([diff(x_1(t),t)=-4*x_1(t)+2*x_2(t)+1/t,diff(x_2(t),t)=2*x_1(t)-1*x_2(t)+2/t+4],[x_1(t),x_2(t)+2/t+4]$$

$$x_1(t) = \frac{2e^{-5t}c_1}{5} + \ln(-5t) + \frac{c_2}{2} + \frac{8t}{5} - \frac{2}{5}$$

$$x_2(t) = 2\ln(-5t) - \frac{e^{-5t}c_1}{5} + \frac{16t}{5} + c_2$$

✓ Solution by Mathematica

Time used: 0.021 (sec). Leaf size: 83

$$x1(t) \rightarrow \frac{1}{25} (40t + 25\log(t) + 10(2c_1 - c_2)e^{-5t} - 8 + 5c_1 + 10c_2)$$

$$x2(t) \rightarrow 2\log(t) + \frac{1}{5}(c_2 - 2c_1)e^{-5t} + \frac{2}{25}(40t + 2 + 5c_1 + 10c_2)$$

18.7 problem 7

Internal problem ID [784]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 7.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = x_1(t) + x_2(t) + 2e^t$$

 $x'_2(t) = 4x_1(t) + x_2(t) - e^t$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 44

$$x_1(t) = -\frac{c_2 e^{-t}}{2} + \frac{c_1 e^{3t}}{2} + \frac{e^t}{4}$$

$$x_2(t) = c_2 e^{-t} + c_1 e^{3t} - 2 e^t$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 54

DSolve[{x1'[t]==1*x1[t]+1*x2[t]+2*Exp[t],x2'[t]==4*x1[t]+1*x2[t]-Exp[t]},{x1[t],x2[t]},t,Incl

$$x1(t) \to \frac{1}{4}e^t(4c_1\cosh(2t) + 2c_2\sinh(2t) + 1)$$

$$x2(t) \to e^t(c_2 \cosh(2t) + 2c_1 \sinh(2t) - 2)$$

18.8 problem 8

Internal problem ID [785]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 8.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = 2x_1(t) - x_2(t) + e^t$$

$$x'_2(t) = 3x_1(t) - 2x_2(t) - e^t$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 43

dsolve([diff(x_1(t),t)=2*x_1(t)-1*x_2(t)+exp(t),diff(x_2(t),t)=3*x_1(t)-2*x_2(t)-exp(t)

$$x_1(t) = \frac{c_2 e^{-t}}{3} + c_1 e^t + e^t + 2t e^t$$

$$x_2(t) = c_2 e^{-t} + c_1 e^t + 2t e^t$$

✓ Solution by Mathematica

Time used: 0.008 (sec). Leaf size: 80

 $DSolve[{x1'[t] == 2*x1[t] - 1*x2[t] + Exp[t], x2'[t] == 3*x1[t] - 2*x2[t] - Exp[t]}, {x1[t], x2[t]}, t, Include the context of the context$

$$x1(t) \to \frac{1}{2}e^{-t}(e^{2t}(4t - 1 + 3c_1 - c_2) - c_1 + c_2)$$

$$x2(t) \to \frac{1}{2}e^{-t}(e^{2t}(4t - 3 + 3c_1 - c_2) - 3c_1 + 3c_2)$$

18.9 problem 9

Internal problem ID [786]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

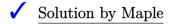
Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 9.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = -\frac{5x_1(t)}{4} + \frac{3x_2(t)}{4} + 2t$$
$$x_2'(t) = \frac{3x_1(t)}{4} - \frac{5x_2(t)}{4} + e^t$$



Time used: 0.062 (sec). Leaf size: 51

$$dsolve([diff(x_1(t),t)=-5/4*x_1(t)+3/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_2(t)+2*t,diff(x_2(t),t)=3/4*x_1(t)-5/4*x_1(t)-$$

$$x_1(t) = c_2 e^{-\frac{t}{2}} - c_1 e^{-2t} - \frac{17}{4} + \frac{e^t}{6} + \frac{5t}{2}$$

$$x_2(t) = c_2 e^{-\frac{t}{2}} + c_1 e^{-2t} + \frac{3t}{2} + \frac{e^t}{2} - \frac{15}{4}$$

✓ Solution by Mathematica

Time used: 0.346 (sec). Leaf size: 101

 $DSolve[{x1'[t] == -5/4*x1[t] + 3/4*x2[t] + 2*t, x2'[t] == 3/4*x1[t] - 5/4*x2[t] + Exp[t]}, {x1[t], x2[t]}, t,$

$$x1(t) \rightarrow \frac{1}{12} (30t + 2e^t + 6(c_1 - c_2)e^{-2t} + 6(c_1 + c_2)e^{-t/2} - 51)$$

$$x2(t) \rightarrow \frac{1}{4}e^{-2t}(3e^{2t}(2t-5)+2e^{3t}+2(c_1+c_2)e^{3t/2}-2c_1+2c_2)$$

18.10 problem 10

Internal problem ID [787]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 10.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = -3x_1(t) + \sqrt{2}x_2(t) + e^{-t}$$

$$x_2'(t) = \sqrt{2}x_1(t) - 2x_2(t) - e^{-t}$$

✓ Solution by Maple

Time used: 0.109 (sec). Leaf size: 91

$$x_1(t) = \frac{t e^{-t}}{3} + \frac{e^{-t}}{3} + \frac{e^{-t}\sqrt{2}c_1}{2} - \frac{t e^{-t}\sqrt{2}}{3} - \sqrt{2}e^{-4t}c_2 + \frac{\sqrt{2}e^{-t}}{6}$$

$$x_2(t) = e^{-4t}c_2 + e^{-t}c_1 + \frac{t e^{-t}\sqrt{2}}{3} - \frac{2t e^{-t}}{3}$$

✓ Solution by Mathematica

Time used: 0.035 (sec). Leaf size: 128

$$DSolve[{x1'[t] == -3*x1[t] + Sqrt[2]*x2[t] + Exp[-t], x2'[t] == Sqrt[2]*x1[t] - 2*x2[t] - Exp[-t]}, {x1[t], x2[t] == -3*x1[t] + Sqrt[2]*x2[t] + Exp[-t]}, {x1[t], x2[t] == -3*x1[t] + Sqrt[2]*x2[t] + Exp[-t], {x1[t], x2[t] == -3*x1[t] + Exp[-t]}, {x1[t], x2[t] == -3*x1[t] + Exp[-t]}, {x1[t], x2[t] == -3*x1[t] + Exp[-t], {x1[t], x2[t] == -3*x1[t] + Exp[-t]}, {x1[t], x2[t] == -3*x1[t] + Exp[-t], {x1[t], x2[t] == -3*x1[t] + Exp[-t]}, {x1[t], x2[t] == -3*x1[t]}, {x1[t], x2[t] == -3*x1[t]}, {x1[t], x2[t] == -3*x1[t]}, {x1[t], x2[t]}, {x1[t], x$$

$$x1(t) \to \frac{1}{9}e^{-4t} \left(e^{3t} \left(-3\left(\sqrt{2} - 1\right)t + \sqrt{2} + 2 + 3c_1 + 3\sqrt{2}c_2 \right) + 6c_1 - 3\sqrt{2}c_2 \right)$$

$$x2(t) \to \frac{1}{9}e^{-4t} \left(e^{3t} \left(3\left(\sqrt{2} - 2\right)t - \sqrt{2} - 1 + 3\sqrt{2}c_1 + 6c_2 \right) - 3\sqrt{2}c_1 + 3c_2 \right)$$

18.11 problem 11

Internal problem ID [788]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 11.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = 2x_1(t) - 5x_2(t)$$

$$x'_2(t) = x_1(t) - 2x_2(t) + \cos(t)$$

✓ Solution by Maple

Time used: 0.109 (sec). Leaf size: 60

$$dsolve([diff(x_1(t),t)=2*x_1(t)-5*x_2(t)+0,diff(x_2(t),t)=1*x_1(t)-2*x_2(t)+cos(t)],[x_1(t)-2*x_2(t)+cos(t)]$$

$$x_1(t) = 2\cos(t)c_1 + c_2\cos(t) - c_1\sin(t) + 2c_2\sin(t) - \frac{5\sin(t)t}{2} - \frac{5\cos(t)}{2}$$

$$x_2(t) = c_2 \sin(t) + \cos(t) c_1 + \frac{\cos(t) t}{2} - \cos(t) - \sin(t) t$$

✓ Solution by Mathematica

Time used: 0.025 (sec). Leaf size: 60

 $DSolve[{x1'[t] == 2*x1[t] - 5*x2[t] + 0, x2'[t] == 1*x1[t] - 2*x2[t] - Cos[t]}, {x1[t], x2[t]}, t, IncludeSing[t], {x1[$

$$x1(t) \to \left(\frac{5}{2} + c_1\right)\cos(t) + \frac{1}{2}(5t + 4c_1 - 10c_2)\sin(t)$$

$$x2(t) \to \left(-\frac{t}{2} + 1 + c_2\right)\cos(t) + (t + c_1 - 2c_2)\sin(t)$$

18.12 problem 12

Internal problem ID [789]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 12.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = 2x_1(t) - 5x_2(t) + \csc(t)$$

$$x'_2(t) = x_1(t) - 2x_2(t) + \sec(t)$$

✓ Solution by Maple

Time used: 0.39 (sec). Leaf size: 113

$$x_1(t) = -5\ln(\cos(t))\cos(t) + \cos(t)\ln(\sin(t)) + 2\cos(t)c_1 + c_2\cos(t) - 2\cos(t)t$$
$$+ 2\sin(t)\ln(\sin(t)) - c_1\sin(t) + 2c_2\sin(t) - 4\sin(t)t - 2\sin(t) - \sec(t) + \frac{\sin(t)^2}{\cos(t)}$$

$$x_2(t) = -2\ln(\cos(t))\cos(t) + \cos(t)c_1 - \ln(\cos(t))\sin(t) + \sin(t)\ln(\sin(t)) + c_2\sin(t) - 2\sin(t)t - \sin(t)$$

✓ Solution by Mathematica

Time used: 0.018 (sec). Leaf size: 79

$$DSolve[{x1'[t] == 2*x1[t] - 5*x2[t] + Csc[t], x2'[t] == 1*x1[t] - 2*x2[t] + Sec[t]}, {x1[t], x2[t]}, t, Include (a) = 1*x1[t] - 2*x2[t] + Sec[t]}, {x1[t], x2[t]}, t, Include (a) = 1*x1[t] - 2*x2[t] + Sec[t]}, {x1[t], x2[t]}, t, Include (a) = 1*x1[t] - 2*x2[t] + Sec[t]}, {x1[t], x2[t]}, t, Include (a) = 1*x1[t] - 2*x2[t] + Sec[t]}, {x1[t], x2[t]}, t, Include (a) = 1*x1[t] - 2*x2[t] + Sec[t]}, {x1[t], x2[t]}, t, Include (a) = 1*x1[t] - 2*x2[t] + Sec[t]}, {x1[t], x2[t]}, t, Include (a) = 1*x1[t] - 2*x2[t] + Sec[t]}, {x1[t], x2[t]}, t, Include (a) = 1*x1[t] - 2*x2[t] + Sec[t]}, {x1[t], x2[t]}, t, Include (a) = 1*x1[t] - 2*x2[t] + Sec[t]}, {x1[t], x2[t]}, t, Include (a) = 1*x1[t] - 2*x2[t] + Sec[t]}, {x1[t], x2[t]}, t, Include (a) = 1*x1[t] - 2*x2[t]}, {x1[t], x2[t]}, {x1[t]$$

$$x1(t) \to \cos(t)(-2t + \log(\tan(t)) - 4\log(\cos(t)) + c_1) + \sin(t)(-4t + 2\log(\tan(t)) + 2\log(\cos(t)) + 2c_1 - 5c_2)$$
$$x2(t) \to \cos(t)(-2\log(\cos(t)) + c_2) + \sin(t)(-2t + \log(\tan(t)) + c_1 - 2c_2)$$

18.13 problem 13

Internal problem ID [790]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 13.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = -\frac{x_1(t)}{2} - \frac{x_2(t)}{8} + \frac{e^{-\frac{t}{2}}}{2}$$
$$x_2'(t) = 2x_1(t) - \frac{x_2(t)}{2}$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 47

 $dsolve([diff(x_{1}(t),t)=-1/2*x_{1}(t)-1/8*x_{2}(t)+1/2*exp(-t/2),diff(x_{2}(t),t)=2*x_{1}(t)-1/2*x_{2}(t)+1/2*exp(-t/2),diff(x_{3}(t),t)=2*x_{3}(t)-1/2*x_{4}(t)-1/2*x_{4}(t)+1/2*exp(-t/2),diff(x_{4}(t),t)=2*x_{4}(t)-1/2*x_{4}(t)-1/2*x_{4}(t)+1/2*exp(-t/2),diff(x_{4}(t),t)=2*x_{4}(t)-1/2*x_{4}(t)-1/2*x_{4}(t)+1/2*exp(-t/2),diff(x_{4}(t),t)=2*x_{4}(t)-1/2*x_{4}(t)-1$

$$x_1(t) = \frac{e^{-\frac{t}{2}} \left(c_2 \cos\left(\frac{t}{2}\right) - c_1 \sin\left(\frac{t}{2}\right)\right)}{4}$$

$$x_2(t) = \mathrm{e}^{-\frac{t}{2}} \left(\cos \left(\frac{t}{2} \right) c_1 + \sin \left(\frac{t}{2} \right) c_2 + 4 \right)$$

✓ Solution by Mathematica

Time used: 0.024 (sec). Leaf size: 69

 $DSolve[{x1'[t] == -1/2*x1[t] - 1/8*x2[t] + 1/2*Exp[-t/2], x2'[t] == 2*x1[t] - 1/2*x2[t] + 0}, {x1[t], x2[t]}$

$$x1(t) \rightarrow \frac{1}{4}e^{-t/2}\left(4c_1\cos\left(\frac{t}{2}\right) - c_2\sin\left(\frac{t}{2}\right)\right)$$

$$x2(t) \rightarrow e^{-t/2} \left(c_2 \cos\left(\frac{t}{2}\right) + 4c_1 \sin\left(\frac{t}{2}\right) + 4 \right)$$

18.14 problem 18

Internal problem ID [791]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 7.9, Nonhomogeneous Linear Systems. page 447

Problem number: 18.

ODE order: 1. ODE degree: 1.

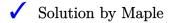
Solve

$$x'_1(t) = -2x_1(t) + x_2(t) + 2e^{-t}$$

$$x'_2(t) = x_1(t) - 2x_2(t) + 3t$$

With initial conditions

$$[x_1(0) = \alpha_1, x_2(0) = \alpha_2]$$



Time used: 0.063 (sec). Leaf size: 93

$$dsolve([diff(x_1(t),t) = -2*x_1(t)+x_2(t)+2*exp(-t), diff(x_2(t),t) = x_1(t)-2*x_2(t)+3*exp(-t), diff(x_2(t),t) = x_1(t)-2*x_2(t)+3*exp(-t)-$$

$$x_1(t) = \left(\frac{3}{2} + \frac{\alpha_2}{2} + \frac{\alpha_1}{2}\right) e^{-t} - \left(\frac{2}{3} + \frac{\alpha_2}{2} - \frac{\alpha_1}{2}\right) e^{-3t} + \frac{e^{-t}}{2} + t e^{-t} - \frac{4}{3} + t$$

$$x_2(t) = \left(\frac{3}{2} + \frac{\alpha_2}{2} + \frac{\alpha_1}{2}\right) e^{-t} + \left(\frac{2}{3} + \frac{\alpha_2}{2} - \frac{\alpha_1}{2}\right) e^{-3t} + t e^{-t} + 2t - \frac{5}{3} - \frac{e^{-t}}{2}$$

✓ Solution by Mathematica

Time used: 0.063 (sec). Leaf size: 94

$$DSolve[{x1'[t] == -2*x1[t] + 1*x2[t] + 2*Exp[-t], x2'[t] == 1*x1[t] - 2*x2[t] + 3*t}, {x1[0] == a1, x2[0] == a2}$$

$$x1(t) \to \frac{1}{6}e^{-3t}(3e^{2t}(a1+a2+2t+4)+3a1-3a2+2e^{3t}(3t-4)-4)$$

$$x2(t) \to \frac{1}{6}e^{-3t} (3e^{2t}(a1+a2+2t+2) - 3a1 + 3a2 + 2e^{3t}(6t-5) + 4)$$

19 Chapter 9.1, The Phase Plane: Linear Systems. page 505

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19.1 problem 1

Internal problem ID [792]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

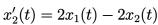
Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 1.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = 3x_1(t) - 2x_2(t)$$



Solution by Maple

Time used: 0.031 (sec). Leaf size: 36

dsolve([diff(x_1(t),t)=3*x_1(t)-2*x_2(t),diff(x_2(t),t)=2*x_1(t)-2*x_2(t)], [x_1(t), x_2(t), t]

$$x_1(t) = \frac{e^{-t}c_1}{2} + 2c_2e^{2t}$$

$$x_2(t) = e^{-t}c_1 + c_2e^{2t}$$

Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 73

 $DSolve[{x1'[t] == 3*x1[t] - 2*x2[t], x2'[t] == 2*x1[t] - 2*x2[t]}, {x1[t], x2[t]}, t, IncludeSingularSolut = 2*x1[t] - 2*x2[t]}, {x1[t], x2[t]}, {x$

$$x1(t) \to \frac{1}{3}e^{-t}(c_1(4e^{3t}-1)-2c_2(e^{3t}-1))$$

$$x2(t) \to \frac{1}{3}e^{-t}(2c_1(e^{3t}-1)-c_2(e^{3t}-4))$$

19.2 problem 2

Internal problem ID [793]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 2.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = 5x_1(t) - x_2(t)$$

$$x_2'(t) = 3x_1(t) + x_2(t)$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 35

$$x_1(t) = c_1 e^{4t} + \frac{c_2 e^{2t}}{3}$$

$$x_2(t) = c_1 e^{4t} + c_2 e^{2t}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 55

 $DSolve[{x1'[t] == 5*x1[t] - 1*x2[t], x2'[t] == 3*x1[t] + 1*x2[t]}, {x1[t], x2[t]}, t, IncludeSingularSolut}$

$$x1(t) \to e^{3t}(c_1 \cosh(t) + (2c_1 - c_2) \sinh(t))$$

$$x2(t) \to e^{3t}(3c_1\sinh(t) + c_2(\cosh(t) - 2\sinh(t)))$$

19.3 problem 3

Internal problem ID [794]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 3.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = 2x_1(t) - x_2(t)$$

$$x_2'(t) = 3x_1(t) - 2x_2(t)$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 31

$$x_1(t) = \frac{\mathrm{e}^{-t}c_1}{3} + c_2\mathrm{e}^t$$

$$x_2(t) = e^{-t}c_1 + c_2e^t$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 43

$$x1(t) \rightarrow c_1 \cosh(t) + (2c_1 - c_2) \sinh(t)$$

$$x2(t) \rightarrow 3c_1 \sinh(t) + c_2(\cosh(t) - 2\sinh(t))$$

19.4 problem 4

Internal problem ID [795]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 4.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = x_1(t) - 4x_2(t)$$

$$x_2'(t) = 4x_1(t) - 7x_2(t)$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 33

 $dsolve([diff(x_1(t),t)=1*x_1(t)-4*x_2(t),diff(x_2(t),t)=4*x_1(t)-7*x_2(t)],[x_1(t),x_2(t),t)=4*x_1(t)-7*x_2(t)],\\[2mm]$

$$x_1(t) = \frac{e^{-3t}(4c_2t + 4c_1 + c_2)}{4}$$

$$x_2(t) = e^{-3t}(c_2t + c_1)$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 46

 $DSolve[{x1'[t] == 1 * x1[t] - 4 * x2[t], x2'[t] == 4 * x1[t] - 7 * x2[t]}, {x1[t], x2[t]}, t, IncludeSingularSolut}$

$$x1(t) \to e^{-3t}(4c_1t - 4c_2t + c_1)$$

$$x2(t) \to e^{-3t}(4(c_1 - c_2)t + c_2)$$

19.5 problem 5

Internal problem ID [796]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 5.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = x_1(t) - 5x_2(t)$$

$$x_2'(t) = x_1(t) - 3x_2(t)$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 47

 $dsolve([diff(x_{1}(t),t)=1*x_{1}(t)-5*x_{2}(t),diff(x_{2}(t),t)=1*x_{1}(t)-3*x_{2}(t)], [x_{1}(t),x_{2}(t),t)=1*x_{2}(t), [x_{1}(t),x_{2}(t),t]=1*x_{3}(t), [x_{1}(t),x_{2}(t),t]=1*x_{4}(t), [x_{1}(t),x_{2}(t)$

$$x_1(t) = e^{-t}(\cos(t) c_1 - c_2 \sin(t) + 2c_1 \sin(t) + 2c_2 \cos(t))$$

$$x_2(t) = e^{-t}(c_1 \sin(t) + c_2 \cos(t))$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 54

DSolve[{x1'[t]==1*x1[t]-5*x2[t],x2'[t]==1*x1[t]-3*x2[t]},{x1[t],x2[t]},t,IncludeSingularSolut

$$x1(t) \to e^{-t}(c_1 \cos(t) + (2c_1 - 5c_2)\sin(t))$$

$$x2(t) \to e^{-t}(c_2\cos(t) + (c_1 - 2c_2)\sin(t))$$

19.6 problem 6

Internal problem ID [797]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 6.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = 2x_1(t) - 5x_2(t)$$

$$x_2'(t) = x_1(t) - 2x_2(t)$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 37

$$dsolve([diff(x_1(t),t)=2*x_1(t)-5*x_2(t),diff(x_2(t),t)=1*x_1(t)-2*x_2(t)],[x_1(t),x_2(t),t]=1*x_1(t)-2*x_2(t),\\$$

$$x_1(t) = \cos(t) c_1 - c_2 \sin(t) + 2c_1 \sin(t) + 2c_2 \cos(t)$$

$$x_2(t) = c_1 \sin(t) + c_2 \cos(t)$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 41

DSolve[{x1'[t]==2*x1[t]-5*x2[t],x2'[t]==1*x1[t]-2*x2[t]},{x1[t],x2[t]},t,IncludeSingularSolut

$$x1(t) \to c_1(2\sin(t) + \cos(t)) - 5c_2\sin(t)$$

$$x2(t) \rightarrow c_2 \cos(t) + (c_1 - 2c_2) \sin(t)$$

19.7 problem 7

Internal problem ID [798]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 7.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = 3x_1(t) - 2x_2(t)$$

$$x'_2(t) = 4x_1(t) - x_2(t)$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 54

$$x_1(t) = \frac{e^t(c_1 \sin(2t) - c_2 \sin(2t) + c_1 \cos(2t) + c_2 \cos(2t))}{2}$$

$$x_2(t) = e^t(c_1 \sin(2t) + c_2 \cos(2t))$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 58

$$x1(t) \to e^t(c_1 \cos(2t) + (c_1 - c_2)\sin(2t))$$

 $x2(t) \to e^t(c_2 \cos(2t) + (2c_1 - c_2)\sin(2t))$

19.8 problem 8

Internal problem ID [799]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 8.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = -x_1(t) - x_2(t)$$
$$x_2'(t) = -\frac{5x_2(t)}{2}$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 28

 $dsolve([diff(x_{1}(t),t)=-1*x_{1}(t)-1*x_{2}(t),diff(x_{2}(t),t)=0*x_{1}(t)-25/10*x_{2}(t)],[x_{1}(t)-1*x_{2}(t),diff(x_{3}(t),t)=0*x_{3}(t)-25/10*x_{4}(t)]$

$$x_1(t) = \frac{2c_2 e^{-\frac{5t}{2}}}{3} + e^{-t}c_1$$

$$x_2(t) = c_2 e^{-\frac{5t}{2}}$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 47

 $DSolve[{x1'[t] == -1 * x1[t] - 1 * x2[t], x2'[t] == 0 * x1[t] - 25/10 * x2[t]}, {x1[t], x2[t]}, t, IncludeSingular} \\$

$$x1(t) \to \left(c_1 - \frac{2c_2}{3}\right)e^{-t} + \frac{2}{3}c_2e^{-5t/2}$$

 $x2(t) \to c_2e^{-5t/2}$

19.9 problem 9

Internal problem ID [800]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 9.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = 3x_1(t) - 4x_2(t)$$
$$x_2'(t) = x_1(t) - x_2(t)$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 28

 $dsolve([diff(x_1(t),t)=3*x_1(t)-4*x_2(t),diff(x_2(t),t)=1*x_1(t)-1*x_2(t)], [x_1(t),x_2(t),x_2(t)]$

$$x_1(t) = e^t(2c_2t + 2c_1 + c_2)$$

$$x_2(t) = e^t(c_2t + c_1)$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 41

DSolve[{x1'[t]==3*x1[t]-4*x2[t],x2'[t]==1*x1[t]-1*x2[t]},{x1[t],x2[t]},t,IncludeSingularSolut

$$x1(t) \to e^t(2c_1t - 4c_2t + c_1)$$

$$x2(t) \to e^t((c_1 - 2c_2)t + c_2)$$

19.10 problem 10

Internal problem ID [801]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 10.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = x_1(t) + 2x_2(t)$$

$$x'_2(t) = -5x_1(t)$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 84

$$x_1(t) = \frac{e^{\frac{t}{2}} \left(\sin\left(\frac{\sqrt{39}t}{2}\right) \sqrt{39} c_2 - \cos\left(\frac{\sqrt{39}t}{2}\right) \sqrt{39} c_1 - \sin\left(\frac{\sqrt{39}t}{2}\right) c_1 - \cos\left(\frac{\sqrt{39}t}{2}\right) c_2 \right)}{10}$$

$$x_2(t) = e^{\frac{t}{2}} \left(\sin\left(\frac{\sqrt{39}t}{2}\right) c_1 + \cos\left(\frac{\sqrt{39}t}{2}\right) c_2 \right)$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 54

DSolve[{x1'[t]==1*x1[t]+2*x2[t],x2'[t]==-5*x1[t]-1*x2[t]},{x1[t],x2[t]},t,IncludeSingularSolu

$$x1(t) \to c_1 \cos(3t) + \frac{1}{3}(c_1 + 2c_2)\sin(3t)$$

$$x2(t) \rightarrow c_2 \cos(3t) - \frac{1}{3}(5c_1 + c_2)\sin(3t)$$

19.11 problem 11

Internal problem ID [802]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 11.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = -x_1(t)$$

$$x_2'(t) = -x_2(t)$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 20

$$x_1(t) = e^{-t}c_1$$

$$x_2(t) = c_2 \mathrm{e}^{-t}$$

✓ Solution by Mathematica

Time used: 0.035 (sec). Leaf size: 65

 $\textbf{DSolve}[\{x1'[t] == -1*x1[t] - 0*x2[t], x2'[t] == 0*x1[t] - 1*x2[t]\}, \{x1[t], x2[t]\}, t, Include \\ \textbf{Singular Solution of the property of$

$$x1(t) \rightarrow c_1 e^{-t}$$

$$x2(t) \rightarrow c_2 e^{-t}$$

$$x1(t) \rightarrow c_1 e^{-t}$$

$$x2(t) \to 0$$

$$x1(t) \rightarrow 0$$

$$x2(t) \rightarrow c_2 e^{-t}$$

$$x1(t) \rightarrow 0$$

$$x2(t) \to 0$$

19.12 problem 12

Internal problem ID [803]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and DiPrima

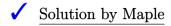
Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 12.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = 2x_1(t) - \frac{5x_2(t)}{2}$$
$$x_2'(t) = \frac{9x_1(t)}{5} - x_2(t)$$



Time used: 0.015 (sec). Leaf size: 58

$$dsolve([diff(x_1(t),t)=2*x_1(t)-5/2*x_2(t),diff(x_2(t),t)=9/5*x_1(t)-1*x_2(t)],[x_1(t)-1*x_2(t)]$$

$$x_1(t) = \frac{5 e^{\frac{t}{2}} \left(\sin\left(\frac{3t}{2}\right) c_1 - \sin\left(\frac{3t}{2}\right) c_2 + \cos\left(\frac{3t}{2}\right) c_1 + \cos\left(\frac{3t}{2}\right) c_2\right)}{6}$$

$$x_2(t) = e^{\frac{t}{2}} \left(\sin\left(\frac{3t}{2}\right) c_1 + \cos\left(\frac{3t}{2}\right) c_2 \right)$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 84

 $DSolve[{x1'[t] == 2*x1[t] - 5/2*x2[t], x2'[t] == 9/5*x1[t] - 1*x2[t]}, {x1[t], x2[t]}, t, IncludeSingularSin$

$$\mathrm{x1}(t)
ightarrow rac{1}{3} e^{t/2} igg(3c_1 \cos \left(rac{3t}{2}
ight) + (3c_1 - 5c_2) \sin \left(rac{3t}{2}
ight) igg)$$

$$\mathbf{x}2(t) \to \frac{1}{5}e^{t/2} \left(5c_2 \cos\left(\frac{3t}{2}\right) + (6c_1 - 5c_2)\sin\left(\frac{3t}{2}\right)\right)$$

19.13 problem 13

Internal problem ID [804]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 13.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = x_1(t) + x_2(t) - 2$$

$$x'_2(t) = x_1(t) - x_2(t)$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 70

 $dsolve([diff(x_1(t),t)=1*x_1(t)+1*x_2(t)-2,diff(x_2(t),t)=1*x_1(t)-1*x_2(t)],[x_1(t),t)=1*x_1(t)-1*x_2(t)]$

$$x_1(t) = \sqrt{2} e^{t\sqrt{2}} c_2 - \sqrt{2} e^{-t\sqrt{2}} c_1 + e^{t\sqrt{2}} c_2 + e^{-t\sqrt{2}} c_1 + 1$$

$$x_2(t) = e^{t\sqrt{2}}c_2 + e^{-t\sqrt{2}}c_1 + 1$$

✓ Solution by Mathematica

Time used: 0.103 (sec). Leaf size: 74

$$x1(t) \rightarrow c_1 \cosh\left(\sqrt{2}t\right) + \frac{(c_1 + c_2)\sinh\left(\sqrt{2}t\right)}{\sqrt{2}} + 1$$

$$x2(t) \rightarrow c_2 \cosh\left(\sqrt{2}t\right) + \frac{(c_1 - c_2)\sinh\left(\sqrt{2}t\right)}{\sqrt{2}} + 1$$

19.14 problem 14

Internal problem ID [805]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 14.

ODE order: 1. ODE degree: 1.

Solve

$$x'_1(t) = -2x_1(t) + x_2(t) - 2$$

$$x'_2(t) = x_1(t) - 2x_2(t) + 1$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 36

 $dsolve([diff(x_{1}(t),t)=-2*x_{1}(t)+1*x_{2}(t)-2,diff(x_{2}(t),t)=1*x_{1}(t)-2*x_{2}(t)+1],[x_{1}(t)+1*x_{2}(t)+1]$

$$x_1(t) = e^{-t}c_1 - c_2e^{-3t} - 1$$

$$x_2(t) = e^{-t}c_1 + c_2e^{-3t}$$

✓ Solution by Mathematica

Time used: 0.022 (sec). Leaf size: 57

DSolve[{x1'[t]==-2*x1[t]+1*x2[t]-2,x2'[t]==1*x1[t]-2*x2[t]+1},{x1[t],x2[t]},t,IncludeSingular

$$x1(t) \to \frac{1}{2}e^{-3t}(e^{2t}(-2e^t + c_1 + c_2) + c_1 - c_2)$$

$$x2(t) \rightarrow e^{-2t}(c_2 \cosh(t) + c_1 \sinh(t))$$

19.15 problem 15

Internal problem ID [806]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.1, The Phase Plane: Linear Systems. page 505

Problem number: 15.

ODE order: 1. ODE degree: 1.

Solve

$$x_1'(t) = -x_1(t) - x_2(t) - 1$$

$$x_2'(t) = 2x_1(t) - x_2(t) + 5$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 61

$$dsolve([diff(x_{1}(t),t)=-1*x_{1}(t)-1*x_{2}(t)-1,diff(x_{2}(t),t)=2*x_{1}(t)-1*x_{2}(t)+5],[x_{1}(t)-1*x_{2}(t)+5]$$

$$x_1(t) = -2 - \frac{\sqrt{2} e^{-t} (c_1 \sin (t\sqrt{2}) - c_2 \cos (t\sqrt{2}))}{2}$$

$$x_2(t) = 1 + e^{-t} \left(c_2 \sin\left(t\sqrt{2}\right) + \cos\left(t\sqrt{2}\right) c_1 \right)$$

✓ Solution by Mathematica

Time used: 0.282 (sec). Leaf size: 85

DSolve[{x1'[t]==-1*x1[t]-1*x2[t]-1,x2'[t]==2*x1[t]-1*x2[t]+5},{x1[t],x2[t]},t,IncludeSingular

$$x1(t) \to -2 + \frac{1}{2}e^{-t} \left(2c_1 \cos\left(\sqrt{2}t\right) - \sqrt{2}c_2 \sin\left(\sqrt{2}t\right) \right)$$
$$x2(t) \to 1 + e^{-t} \left(c_2 \cos\left(\sqrt{2}t\right) + \sqrt{2}c_1 \sin\left(\sqrt{2}t\right) \right)$$

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20.1 problem 1

Internal problem ID [807]

 \mathbf{Book} : Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.2, Autonomous Systems and Stability. page 517

Problem number: 1.

ODE order: 1. ODE degree: 1.

Solve

$$x'(t) = -x(t)$$

$$y'(t) = -2y(t)$$

With initial conditions

$$[x(0) = 4, y(0) = 2]$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 20

dsolve([diff(x(t),t) = -x(t), diff(y(t),t) = -2*y(t), x(0) = 4, y(0) = 2],[x(t), y(t)], sings(x(t),t) = -x(t), diff(y(t),t) = -2*y(t), x(0) = 4, y(0) = 2],[x(t), y(t)], sings(x(t),t) = -x(t), diff(y(t),t) = -2*y(t), x(0) = 4, y(0) = 2],[x(t), y(t)], sings(x(t),t) = -x(t), diff(y(t),t) = -2*y(t), x(0) = 4, y(0) = 2],[x(t), y(t)], sings(x(t),t) = -x(t), diff(y(t),t) = -x(

$$x(t) = 4 \, \mathrm{e}^{-t}$$

$$y(t) = 2 e^{-2t}$$

✓ Solution by Mathematica

Time used: 0.038 (sec). Leaf size: 22

$$x(t) \to 4e^{-t}$$

$$y(t) \to 2e^{-2t}$$

20.2 problem 2 part 1

Internal problem ID [808]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.2, Autonomous Systems and Stability. page 517

Problem number: 2 part 1.

ODE order: 1.
ODE degree: 1.

Solve

$$x'(t) = -x(t)$$

$$y'(t) = 2y(t)$$

With initial conditions

$$[x(0) = 4, y(0) = 2]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 20

dsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 2],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 2],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 2],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 2],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 2],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 2],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 2],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = -x(t), x(0) = 4, y(0) = 2],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = -x(t), x(t), x

$$x(t) = 4 \, \mathrm{e}^{-t}$$

$$y(t) = 2e^{2t}$$

✓ Solution by Mathematica

Time used: 0.039 (sec). Leaf size: 22

DSolve[{x'[t]==-1*x[t]+0*y[t],y'[t]==0*x[t]+2*y[t]},{x[0]==4,y[0]==2},{x[t],y[t]},t,IncludeSi

$$x(t) \rightarrow 4e^{-t}$$

$$y(t) \to 2e^{2t}$$

20.3 problem 2 part 2

Internal problem ID [809]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.2, Autonomous Systems and Stability. page 517

Problem number: 2 part 2.

ODE order: 1.
ODE degree: 1.

Solve

$$x'(t) = -x(t)$$

$$y'(t) = 2y(t)$$

With initial conditions

$$[x(0) = 4, y(0) = 0]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 15

dsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 0],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 0],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 0],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 0],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 0],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 0],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = 2*y(t), x(0) = 4, y(0) = 0],[x(t), y(t)], singsolve([diff(x(t),t) = -x(t), diff(y(t),t) = -x(t), x(t), x(t) = -x(t), x(t), x(t), x(t) = -x(t), x(t), x(t), x(t), x(t), x(t) = -x(t), x(t), x(

$$x(t) = 4 \, \mathrm{e}^{-t}$$

$$y(t) = 0$$

✓ Solution by Mathematica

Time used: 0.041 (sec). Leaf size: 16

$$x(t) \to 4e^{-t}$$

$$y(t) \to 0$$

20.4 problem 3 part 1

Internal problem ID [810]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.2, Autonomous Systems and Stability. page 517

Problem number: 3 part 1.

ODE order: 1.
ODE degree: 1.

Solve

$$x'(t) = -y(t)$$

$$y'(t) = x(t)$$

With initial conditions

$$[x(0) = 4, y(0) = 0]$$

✓ Solution by Maple

Time used: 36.859 (sec). Leaf size: 16

dsolve([diff(x(t),t) = -y(t), diff(y(t),t) = x(t), x(0) = 4, y(0) = 0],[x(t), y(t)], singsol=

$$x(t) = 4\cos(t)$$

$$y(t) = 4\sin\left(t\right)$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 16

$$x(t) \to 4\cos(t)$$

$$y(t) \to 4\sin(t)$$

20.5 problem 3 part 2

Internal problem ID [811]

Book: Elementary differential equations and boundary value problems, 10th ed., Boyce and

DiPrima

Section: Chapter 9.2, Autonomous Systems and Stability. page 517

Problem number: 3 part 2.

ODE order: 1.
ODE degree: 1.

Solve

$$x'(t) = -y(t)$$

$$y'(t) = x(t)$$

With initial conditions

$$[x(0) = 0, y(0) = 4]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 16

dsolve([diff(x(t),t) = -y(t), diff(y(t),t) = x(t), x(0) = 0, y(0) = 4],[x(t), y(t)], singsol=

$$x(t) = -4\sin(t)$$

$$y(t) = 4\cos(t)$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 16

$$x(t) \rightarrow -4\sin(t)$$

$$y(t) \to 4\cos(t)$$