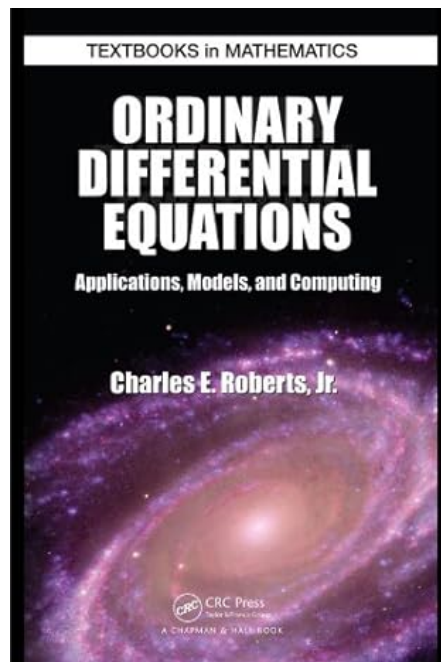


A Solution Manual For

**Ordinary Differential Equations by
Charles E. Roberts, Jr. CRC Press. 2010**



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May 16, 2024

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1.1 problem 15

Internal problem ID [12574]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 15.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _exact, _linear, _homogeneous]]`

$$x^2y'' + y'x - y = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 15

```
dsolve(x^2*diff(y(x),x$2)+x*diff(y(x),x)-y(x)=0,y(x), singsol=all)
```

$$y(x) = \frac{c_2x^2 + c_1}{x}$$

✓ Solution by Mathematica

Time used: 0.017 (sec). Leaf size: 16

```
DSolve[x^2*y''[x]+x*y'[x]-y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{c_1}{x} + c_2x$$

1.2 problem 16

Internal problem ID [12575]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 16.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y'x - y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 7

```
dsolve(x*diff(y(x),x)-y(x)=0,y(x), singsol=all)
```

$$y(x) = c_1x$$

✓ Solution by Mathematica

Time used: 0.036 (sec). Leaf size: 14

```
DSolve[x*y'[x]-y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1x$$

$$y(x) \rightarrow 0$$

1.3 problem 17

Internal problem ID [12576]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 17.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _exact, _linear, _homogeneous]]`

$$2x^2y'' + 3y'x - y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

```
dsolve(2*x^2*diff(y(x),x$2)+3*x*diff(y(x),x)-y(x)=0,y(x), singsol=all)
```

$$y(x) = \frac{c_2x^{\frac{3}{2}} + c_1}{x}$$

✓ Solution by Mathematica

Time used: 0.019 (sec). Leaf size: 20

```
DSolve[2*x^2*y''[x]+3*x*y'[x]-y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{c_2x^{3/2} + c_1}{x}$$

1.4 problem 18

Internal problem ID [12577]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 18.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - 3y' + 2y = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 15

```
dsolve(diff(y(x),x$2)-3*diff(y(x),x)+2*y(x)=0,y(x), singsol=all)
```

$$y(x) = c_1 e^x + c_2 e^{2x}$$

✓ Solution by Mathematica

Time used: 0.02 (sec). Leaf size: 18

```
DSolve[y''[x]-3*y'[x]+2*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^x(c_2 e^x + c_1)$$

1.5 problem 19

Internal problem ID [12578]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 19.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _exact, _linear, _homogeneous]]`

$$x^2 y'' - 2y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

```
dsolve(x^2*diff(y(x),x$2)-2*y(x)=0,y(x), singsol=all)
```

$$y(x) = \frac{c_2 x^3 + c_1}{x}$$

✓ Solution by Mathematica

Time used: 0.016 (sec). Leaf size: 18

```
DSolve[x^2*y''[x]-2*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{c_2 x^3 + c_1}{x}$$

1.6 problem 20

Internal problem ID [12579]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 20.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + \frac{1}{2y} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 23

```
dsolve(diff(y(x),x)+1/(2*y(x))=0,y(x), singsol=all)
```

$$y(x) = \sqrt{c_1 - x}$$
$$y(x) = -\sqrt{c_1 - x}$$

✓ Solution by Mathematica

Time used: 0.113 (sec). Leaf size: 35

```
DSolve[y'[x]+1/(2*y[x])==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\sqrt{-x + 2c_1}$$
$$y(x) \rightarrow \sqrt{-x + 2c_1}$$

1.7 problem 21

Internal problem ID [12580]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 21.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - \frac{y}{x} = 1$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 10

```
dsolve(diff(y(x),x)-y(x)/x=1,y(x), singsol=all)
```

$$y(x) = (\ln(x) + c_1)x$$

✓ Solution by Mathematica

Time used: 0.04 (sec). Leaf size: 12

```
DSolve[y'[x]-y[x]/x==1,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow x(\log(x) + c_1)$$

1.8 problem 22

Internal problem ID [12581]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 22.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - 2\sqrt{|y|} = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 27

```
dsolve(diff(y(x),x)-2*sqrt(abs(y(x)))=0,y(x), singsol=all)
```

$$x + \left(\begin{cases} \sqrt{-y(x)} & y(x) \leq 0 \\ -\sqrt{y(x)} & 0 < y(x) \end{cases} \right) + c_1 = 0$$

✓ Solution by Mathematica

Time used: 0.291 (sec). Leaf size: 31

```
DSolve[y'[x]-Sqrt[Abs[y[x]]]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \text{InverseFunction} \left[\int_1^{\#1} \frac{1}{\sqrt{|K[1]|}} dK[1] \& \right] [x + c_1]$$
$$y(x) \rightarrow 0$$

1.9 problem 23

Internal problem ID [12582]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 23.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [separable]

$$x^2y' + 2yx = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 9

```
dsolve(x^2*diff(y(x),x)+2*x*y(x)=0,y(x), singsol=all)
```

$$y(x) = \frac{c_1}{x^2}$$

✓ Solution by Mathematica

Time used: 0.064 (sec). Leaf size: 16

```
DSolve[x^2*y'[x]+2*x*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{c_1}{x^2}$$

$$y(x) \rightarrow 0$$

1.10 problem 24

Internal problem ID [12583]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 24.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y^2 = 1$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 8

```
dsolve(diff(y(x),x)-y(x)^2=1,y(x), singsol=all)
```

$$y(x) = \tan(c_1 + x)$$

✓ Solution by Mathematica

Time used: 0.213 (sec). Leaf size: 24

```
DSolve[y'[x]-y[x]^2==1,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \tan(x + c_1)$$

$$y(x) \rightarrow -i$$

$$y(x) \rightarrow i$$

1.11 problem 25

Internal problem ID [12584]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 25.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$2x^2y'' + y'x - y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 13

```
dsolve(2*x^2*diff(y(x),x$2)+x*diff(y(x),x)-y(x)=0,y(x), singsol=all)
```

$$y(x) = \frac{c_1}{\sqrt{x}} + c_2x$$

✓ Solution by Mathematica

Time used: 0.02 (sec). Leaf size: 18

```
DSolve[2*x^2*y''[x]+x*y'[x]-y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{c_1}{\sqrt{x}} + c_2x$$

1.12 problem 26

Internal problem ID [12585]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 26.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y'x = \sin(x)$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 8

```
dsolve(x*diff(y(x),x)-sin(x)=0,y(x), singsol=all)
```

$$y(x) = \text{Si}(x) + c_1$$

✓ Solution by Mathematica

Time used: 0.012 (sec). Leaf size: 10

```
DSolve[x*y'[x]-Sin[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \text{Si}(x) + c_1$$

1.13 problem 27

Internal problem ID [12586]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 27.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + 3y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 10

```
dsolve(diff(y(x),x)+3*y(x)=0,y(x), singsol=all)
```

$$y(x) = c_1 e^{-3x}$$

✓ Solution by Mathematica

Time used: 0.037 (sec). Leaf size: 18

```
DSolve[y'[x]+3*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1 e^{-3x}$$

$$y(x) \rightarrow 0$$

1.14 problem 28

Internal problem ID [12587]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 28.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - 3y' - 10y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

```
dsolve(diff(y(x),x$2)-3*diff(y(x),x)-10*y(x)=0,y(x), singsol=all)
```

$$y(x) = (c_1 e^{7x} + c_2) e^{-2x}$$

✓ Solution by Mathematica

Time used: 0.024 (sec). Leaf size: 22

```
DSolve[y''[x]-3*y'[x]-10*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{-2x}(c_2 e^{7x} + c_1)$$

1.15 problem 29

Internal problem ID [12588]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 29.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' + 2y' + y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 14

```
dsolve(diff(y(x),x$2)+2*diff(y(x),x)+y(x)=0,y(x), singsol=all)
```

$$y(x) = e^{-x}(c_2x + c_1)$$

✓ Solution by Mathematica

Time used: 0.024 (sec). Leaf size: 18

```
DSolve[y''[x]+2*y'[x]+y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{-x}(c_2x + c_1)$$

1.16 problem 30

Internal problem ID [12589]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 30.

ODE order: 3.

ODE degree: 1.

CAS Maple gives this as type `[[_3rd_order, _missing_x]]`

$$y''' - 7y'' + 12y' = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 18

```
dsolve(diff(y(x),x$3)-7*diff(y(x),x$2)+12*diff(y(x),x)=0,y(x), singsol=all)
```

$$y(x) = c_1 + c_2e^{3x} + c_3e^{4x}$$

✓ Solution by Mathematica

Time used: 0.054 (sec). Leaf size: 30

```
DSolve[y'''[x]-7*y''[x]+12*y'[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{3}c_1e^{3x} + \frac{1}{4}c_2e^{4x} + c_3$$

1.17 problem 31

Internal problem ID [12590]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 31.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$2y'x - y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 9

```
dsolve(2*x*diff(y(x),x)-y(x)=0,y(x), singsol=all)
```

$$y(x) = c_1\sqrt{x}$$

✓ Solution by Mathematica

Time used: 0.039 (sec). Leaf size: 18

```
DSolve[2*x*y'[x]-y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1\sqrt{x}$$

$$y(x) \rightarrow 0$$

1.18 problem 32

Internal problem ID [12591]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 32.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_y]]`

$$x^2 y'' - y' x = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 11

```
dsolve(x^2*diff(y(x),x$2)-x*diff(y(x),x)=0,y(x), singsol=all)
```

$$y(x) = c_1 x^2 + c_2$$

✓ Solution by Mathematica

Time used: 0.041 (sec). Leaf size: 17

```
DSolve[x^2*y''[x]-x*y'[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{c_1 x^2}{2} + c_2$$

1.19 problem 33

Internal problem ID [12592]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 33.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _exact, _linear, _homogeneous]]`

$$x^2y'' + 6y'x + 4y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

```
dsolve(x^2*diff(y(x),x$2)+6*x*diff(y(x),x)+4*y(x)=0,y(x), singsol=all)
```

$$y(x) = \frac{c_1x^3 + c_2}{x^4}$$

✓ Solution by Mathematica

Time used: 0.018 (sec). Leaf size: 18

```
DSolve[x^2*y''[x]+6*x*y'[x]+4*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{c_2x^3 + c_1}{x^4}$$

1.20 problem 34

Internal problem ID [12593]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 34.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$x^2 y'' - 5y'x + 9y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 14

```
dsolve(x^2*diff(y(x),x$2)-5*x*diff(y(x),x)+9*y(x)=0,y(x), singsol=all)
```

$$y(x) = x^3(c_1 + c_2 \ln(x))$$

✓ Solution by Mathematica

Time used: 0.029 (sec). Leaf size: 18

```
DSolve[x^2*y''[x]-5*x*y'[x]+9*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow x^3(3c_2 \log(x) + c_1)$$

1.21 problem 35

Internal problem ID [12594]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 35.

ODE order: 1.

ODE degree: 2.

CAS Maple gives this as type [_quadrature]

$$y'^2 - 4y = 0$$

✓ Solution by Maple

Time used: 0.11 (sec). Leaf size: 15

```
dsolve(diff(y(x),x)^2-4*y(x)=0,y(x), singsol=all)
```

$$y(x) = 0$$

$$y(x) = (x - c_1)^2$$

✓ Solution by Mathematica

Time used: 0.078 (sec). Leaf size: 38

```
DSolve[(y'[x])^2-4*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{4}(-2x + c_1)^2$$

$$y(x) \rightarrow \frac{1}{4}(2x + c_1)^2$$

$$y(x) \rightarrow 0$$

1.22 problem 36

Internal problem ID [12595]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 36.

ODE order: 1.

ODE degree: 2.

CAS Maple gives this as type `[[_homogeneous, 'class G']]`

$$y'^2 - 9yx = 0$$

✓ Solution by Maple

Time used: 0.109 (sec). Leaf size: 69

```
dsolve(diff(y(x),x)^2-9*x*y(x)=0,y(x), singsol=all)
```

$$\begin{aligned}y(x) &= 0 \\y(x) &= x^3 + 2\sqrt{c_1x}x + c_1 \\y(x) &= x^3 - 2\sqrt{c_1x}x + c_1 \\y(x) &= x^3 - 2\sqrt{c_1x}x + c_1 \\y(x) &= x^3 + 2\sqrt{c_1x}x + c_1\end{aligned}$$

✓ Solution by Mathematica

Time used: 0.087 (sec). Leaf size: 46

```
DSolve[(y'[x])^2-9*x*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$\begin{aligned}y(x) &\rightarrow \frac{1}{4}(-2x^{3/2} + c_1)^2 \\y(x) &\rightarrow \frac{1}{4}(2x^{3/2} + c_1)^2 \\y(x) &\rightarrow 0\end{aligned}$$

1.23 problem 37

Internal problem ID [12596]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises page 14

Problem number: 37.

ODE order: 1.

ODE degree: 2.

CAS Maple gives this as type [_quadrature]

$$y'^2 = x^6$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 21

```
dsolve(diff(y(x),x)^2=x^6,y(x), singsol=all)
```

$$y(x) = \frac{x^4}{4} + c_1$$
$$y(x) = -\frac{x^4}{4} + c_1$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 29

```
DSolve[(y'[x])^2==x^6,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{x^4}{4} + c_1$$
$$y(x) \rightarrow \frac{x^4}{4} + c_1$$

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2.1 problem 1

Internal problem ID [12597]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 1.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - 2yx = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 10

```
dsolve(diff(y(x),x)-2*x*y(x)=0,y(x), singsol=all)
```

$$y(x) = e^{x^2} c_1$$

✓ Solution by Mathematica

Time used: 0.04 (sec). Leaf size: 18

```
DSolve[y'[x]-2*x*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$\begin{aligned}y(x) &\rightarrow c_1 e^{x^2} \\ y(x) &\rightarrow 0\end{aligned}$$

2.2 problem 2

Internal problem ID [12598]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 2.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_linear, 'class A']]`

$$y' + y = x^2 + 2x - 1$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

```
dsolve(diff(y(x),x)+y(x)=x^2+2*x-1,y(x), singsol=all)
```

$$y(x) = x^2 - 1 + c_1 e^{-x}$$

✓ Solution by Mathematica

Time used: 0.088 (sec). Leaf size: 18

```
DSolve[y'[x]+y[x]==x^2+2*x-1,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow x^2 + c_1 e^{-x} - 1$$

2.3 problem 3

Internal problem ID [12599]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 3.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - y' - 6y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

```
dsolve(diff(y(x),x$2)-diff(y(x),x)-6*y(x)=0,y(x), singsol=all)
```

$$y(x) = (c_1 e^{5x} + c_2) e^{-2x}$$

✓ Solution by Mathematica

Time used: 0.022 (sec). Leaf size: 22

```
DSolve[y''[x]-y'[x]-6*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{-2x}(c_2 e^{5x} + c_1)$$

2.4 problem 4

Internal problem ID [12600]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 4.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - x\sqrt{y} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 16

```
dsolve(diff(y(x),x)=x*y(x)^(1/2),y(x), singsol=all)
```

$$\sqrt{y(x)} - \frac{x^2}{4} - c_1 = 0$$

✓ Solution by Mathematica

Time used: 0.2 (sec). Leaf size: 24

```
DSolve[y'[x]==x*y[x]^(1/2),y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{16}(x^2 + 2c_1)^2$$
$$y(x) \rightarrow 0$$

2.5 problem 5

Internal problem ID [12601]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 5.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - y = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 15

```
dsolve(diff(y(x),x$2)-y(x)=0,y(x), singsol=all)
```

$$y(x) = c_1 e^{-x} + c_2 e^x$$

✓ Solution by Mathematica

Time used: 0.021 (sec). Leaf size: 20

```
DSolve[y''[x]-y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1 e^x + c_2 e^{-x}$$

2.6 problem 6

Internal problem ID [12602]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 6.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - 3y^{\frac{2}{3}} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 14

```
dsolve(diff(y(x),x)=3*y(x)^(2/3),y(x), singsol=all)
```

$$y(x)^{\frac{1}{3}} - c_1 - x = 0$$

✓ Solution by Mathematica

Time used: 0.166 (sec). Leaf size: 22

```
DSolve[y'[x]==3*y[x]^(2/3),y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{27}(3x + c_1)^3$$
$$y(x) \rightarrow 0$$

2.7 problem 7

Internal problem ID [12603]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 7.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$x \ln(x) y' - (\ln(x) + 1) y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 9

```
dsolve((x*ln(x))*diff(y(x),x)-(1+ln(x))*y(x)=0,y(x), singsol=all)
```

$$y(x) = c_1 \ln(x) x$$

✓ Solution by Mathematica

Time used: 0.087 (sec). Leaf size: 16

```
DSolve[(x*Log[x])*y'[x]-(1+Log[x])*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1 x \log(x)$$

$$y(x) \rightarrow 0$$

2.8 problem 8 a(i)

Internal problem ID [12604]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 8 a(i).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - y' - 2y = 0$$

With initial conditions

$$[y(0) = 2, y'(0) = -5]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 17

```
dsolve([diff(y(x),x$2)-diff(y(x),x)-2*y(x)=0,y(0) = 2, D(y)(0) = -5],y(x), singsol=all)
```

$$y(x) = 3e^{-x} - e^{2x}$$

✓ Solution by Mathematica

Time used: 0.023 (sec). Leaf size: 19

```
DSolve[{y'[x]-y'[x]-2*y[x]==0,{y[0]==2,y'[0]==-5}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -e^{-x}(e^{3x} - 3)$$

2.9 problem 8 a(ii)

Internal problem ID [12605]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 8 a(ii).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - y' - 2y = 0$$

With initial conditions

$$[y(1) = 3, y'(1) = -1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 21

```
dsolve([diff(y(x),x$2)-diff(y(x),x)-2*y(x)=0,y(1) = 3, D(y)(1) = -1],y(x), singsol=all)
```

$$y(x) = \frac{7e^{1-x}}{3} + \frac{2e^{2x-2}}{3}$$

✓ Solution by Mathematica

Time used: 0.023 (sec). Leaf size: 28

```
DSolve[{y'[x]-y'[x]-2*y[x]==0,{y[1]==3,y'[1]==-1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{7e^{1-x}}{3} + \frac{2}{3}e^{2x-2}$$

2.10 problem 8 b(i)

Internal problem ID [12606]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 8 b(i).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - y' - 2y = 0$$

With initial conditions

$$[y(0) = 1, y(2) = 0]$$

✓ Solution by Maple

Time used: 0.11 (sec). Leaf size: 24

```
dsolve([diff(y(x),x$2)-diff(y(x),x)-2*y(x)=0,y(0) = 1, y(2) = 0],y(x), singsol=all)
```

$$y(x) = \frac{e^{6-x} - e^{2x}}{e^6 - 1}$$

✓ Solution by Mathematica

Time used: 0.022 (sec). Leaf size: 29

```
DSolve[{y'[x]-y'[x]-2*y[x]==0,{y[0]==1,y[2]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{e^{-x}(e^6 - e^{3x})}{e^6 - 1}$$

2.11 problem 8 b(ii)

Internal problem ID [12607]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 8 b(ii).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - y' - 2y = 0$$

With initial conditions

$$[y(0) = 0, y'(2) = 1]$$

✓ Solution by Maple

Time used: 0.094 (sec). Leaf size: 25

```
dsolve([diff(y(x),x$2)-diff(y(x),x)-2*y(x)=0,y(0) = 0, D(y)(2) = 1],y(x), singsol=all)
```

$$y(x) = \frac{e^{2-x}(e^{3x} - 1)}{2e^6 + 1}$$

✓ Solution by Mathematica

Time used: 0.025 (sec). Leaf size: 29

```
DSolve[{y'[x]-y'[x]-2*y[x]==0,{y[0]==0,y'[2]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{e^{2-x}(e^{3x} - 1)}{1 + 2e^6}$$

2.12 problem 9

Internal problem ID [12608]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 9.

ODE order: 3.

ODE degree: 1.

CAS Maple gives this as type `[[_3rd_order, _with_linear_symmetries]]`

$$x^3 y''' - 3x^2 y'' + 6y'x - 6y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 16

```
dsolve(x^3*diff(y(x),x$3)-3*x^2*diff(y(x),x$2)+6*x*diff(y(x),x)-6*y(x)=0,y(x), singsol=all)
```

$$y(x) = x(c_1 x^2 + c_3 x + c_2)$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 19

```
DSolve[x^3*y'''[x]-3*x^2*y''[x]+6*x*y'[x]-6*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow x(x(c_3 x + c_2) + c_1)$$

2.13 problem 10 (a)

Internal problem ID [12609]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 10 (a).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler], [_2nd_order, _linear, '_with_symmetry_[0,F`

$$x^2y'' - 4y'x + 6y = 0$$

With initial conditions

$$[y(1) = 0, y(2) = -4]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 13

```
dsolve([x^2*diff(y(x),x$2)-4*x*diff(y(x),x)+6*y(x)=0,y(1) = 0, y(2) = -4],y(x), singsol=all)
```

$$y(x) = -x^3 + x^2$$

✓ Solution by Mathematica

Time used: 0.017 (sec). Leaf size: 13

```
DSolve[{x^2*y''[x]-4*x*y'[x]+6*y[x]==0,{y[1]==0,y[2]==-4}},y[x],x,IncludeSingularSolutions -
```

$$y(x) \rightarrow -((x - 1)x^2)$$

2.14 problem 10 (b)

Internal problem ID [12610]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 10 (b).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler], [_2nd_order, _linear, '_with_symmetry_[0,F`

$$x^2 y'' - 4y'x + 6y = 0$$

With initial conditions

$$[y(2) = 4, y'(1) = 0]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 15

```
dsolve([x^2*diff(y(x),x$2)-4*x*diff(y(x),x)+6*y(x)=0,y(2) = 4, D(y)(1) = 0],y(x), singsol=al
```

$$y(x) = 2x^3 - 3x^2$$

✓ Solution by Mathematica

Time used: 0.019 (sec). Leaf size: 14

```
DSolve[{x^2*y'[x]-4*x*y'[x]+6*y[x]==0,{y'[1]==0,y[2]==4}},y[x],x,IncludeSingularSolutions -
```

$$y(x) \rightarrow x^2(2x - 3)$$

2.15 problem 10 (c)

Internal problem ID [12611]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 10 (c).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler], [_2nd_order, _linear, '_with_symmetry_[0,F`

$$x^2y'' - 4y'x + 6y = 0$$

With initial conditions

$$[y(1) = 1, y'(2) = -12]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

```
dsolve([x^2*diff(y(x),x$2)-4*x*diff(y(x),x)+6*y(x)=0,y(1) = 1, D(y)(2) = -12],y(x), singsol=
```

$$y(x) = -2x^3 + 3x^2$$

✓ Solution by Mathematica

Time used: 0.019 (sec). Leaf size: 14

```
DSolve[{x^2*y''[x]-4*x*y'[x]+6*y[x]==0,{y[1]==1,y'[2]==-12}},y[x],x,IncludeSingularSolutions
```

$$y(x) \rightarrow (3 - 2x)x^2$$

2.16 problem 10 (d)

Internal problem ID [12612]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 10 (d).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler], [_2nd_order, _linear, '_with_symmetry_[0,F`

$$x^2 y'' - 4y'x + 6y = 0$$

With initial conditions

$$[y'(1) = 3, y'(2) = 0]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 15

```
dsolve([x^2*diff(y(x),x$2)-4*x*diff(y(x),x)+6*y(x)=0,D(y)(1) = 3, D(y)(2) = 0],y(x), singsol
```

$$y(x) = -x^3 + 3x^2$$

✓ Solution by Mathematica

Time used: 0.017 (sec). Leaf size: 13

```
DSolve[{x^2*y'[x]-4*x*y'[x]+6*y[x]==0,{y'[1]==3,y'[2]==0}},y[x],x,IncludeSingularSolutions
```

$$y(x) \rightarrow -((x - 3)x^2)$$

2.17 problem 10 (e)

Internal problem ID [12613]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 10 (e).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler], [_2nd_order, _linear, '_with_symmetry_[0,F`

$$x^2y'' - 4y'x + 6y = 0$$

With initial conditions

$$[y(0) = 0, y(2) = 4]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 15

```
dsolve([x^2*diff(y(x),x$2)-4*x*diff(y(x),x)+6*y(x)=0,y(0) = 0, y(2) = 4],y(x), singsol=all)
```

$$y(x) = x^2(1 + c_1(x - 2))$$

✓ Solution by Mathematica

Time used: 0.029 (sec). Leaf size: 23

```
DSolve[{x^2*y''[x]-4*x*y'[x]+6*y[x]==0,{y[0]==0,y[2]==4}},y[x],x,IncludeSingularSolutions ->
```

$$y(x) \rightarrow \frac{1}{2}x^2(x - c_1x + 2c_1)$$

2.18 problem 10 (f)

Internal problem ID [12614]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 1. Introduction. Exercises 1.3, page 27

Problem number: 10 (f).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler], [_2nd_order, _linear, '_with_symmetry_[0,F`

$$x^2 y'' - 4y'x + 6y = 0$$

With initial conditions

$$[y(0) = 2, y'(2) = -1]$$

X Solution by Maple

```
dsolve([x^2*diff(y(x),x$2)-4*x*diff(y(x),x)+6*y(x)=0,y(0) = 2, D(y)(2) = -1],y(x), singsol=a
```

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

```
DSolve[{x^2*y'[x]-4*x*y'[x]+6*y[x]==0,{y[0]==2,y'[2]==-1}},y[x],x,IncludeSingularSolutions
```

```
{}
```

3 Chapter 2. The Initial Value Problem. Exercises

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3.1 problem 1 (A)

Internal problem ID [12615]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 1 (A).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = 1 - x$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 12

```
dsolve(diff(y(x),x)=1-x,y(x), singsol=all)
```

$$y(x) = -\frac{1}{2}x^2 + x + c_1$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 16

```
DSolve[y'[x]==1-x,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{x^2}{2} + x + c_1$$

3.2 problem 1 (B)

Internal problem ID [12616]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 1 (B).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = x - 1$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 14

```
dsolve(diff(y(x),x)=x-1,y(x), singsol=all)
```

$$y(x) = \frac{1}{2}x^2 - x + c_1$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 18

```
DSolve[y'[x]==x-1,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{x^2}{2} - x + c_1$$

3.3 problem 2 (C)

Internal problem ID [12617]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 2 (C).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + y = 1$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 12

```
dsolve(diff(y(x),x)=1-y(x),y(x), singsol=all)
```

$$y(x) = c_1 e^{-x} + 1$$

✓ Solution by Mathematica

Time used: 0.035 (sec). Leaf size: 20

```
DSolve[y'[x]==1-y[x],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 1 + c_1 e^{-x}$$

$$y(x) \rightarrow 1$$

3.4 problem 2 (D)

Internal problem ID [12618]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 2 (D).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y = 1$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 10

```
dsolve(diff(y(x),x)=1+y(x),y(x), singsol=all)
```

$$y(x) = -1 + c_1 e^x$$

✓ Solution by Mathematica

Time used: 0.037 (sec). Leaf size: 18

```
DSolve[y'[x]==1+y[x],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -1 + c_1 e^x$$

$$y(x) \rightarrow -1$$

3.5 problem 3 (E)

Internal problem ID [12619]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 3 (E).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y^2 = -4$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 24

```
dsolve(diff(y(x),x)=y(x)^2-4,y(x), singsol=all)
```

$$y(x) = \frac{-2c_1e^{4x} - 2}{-1 + c_1e^{4x}}$$

✓ Solution by Mathematica

Time used: 1.066 (sec). Leaf size: 40

```
DSolve[y'[x]==y[x]^2-4,y[x],x,IncludeSingularSolutions -> True]
```

$$\begin{aligned}y(x) &\rightarrow \frac{2 - 2e^{4(x+c_1)}}{1 + e^{4(x+c_1)}} \\y(x) &\rightarrow -2 \\y(x) &\rightarrow 2\end{aligned}$$

3.6 problem 3 (F)

Internal problem ID [12620]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 3 (F).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + y^2 = 4$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 24

```
dsolve(diff(y(x),x)=4-y(x)^2,y(x), singsol=all)
```

$$y(x) = \frac{2c_1e^{4x} + 2}{-1 + c_1e^{4x}}$$

✓ Solution by Mathematica

Time used: 0.278 (sec). Leaf size: 45

```
DSolve[y'[x]==4-y[x]^2,y[x],x,IncludeSingularSolutions -> True]
```

$$\begin{aligned}y(x) &\rightarrow \frac{2(e^{4x} - e^{4c_1})}{e^{4x} + e^{4c_1}} \\y(x) &\rightarrow -2 \\y(x) &\rightarrow 2\end{aligned}$$

3.7 problem 4 (G)

Internal problem ID [12621]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 4 (G).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - yx = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 12

```
dsolve(diff(y(x),x)=x*y(x),y(x), singsol=all)
```

$$y(x) = c_1 e^{\frac{x^2}{2}}$$

✓ Solution by Mathematica

Time used: 0.039 (sec). Leaf size: 22

```
DSolve[y'[x]==x*y[x],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1 e^{\frac{x^2}{2}}$$

$$y(x) \rightarrow 0$$

3.8 problem 4 (H)

Internal problem ID [12622]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 4 (H).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' + yx = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 12

```
dsolve(diff(y(x),x)=-x*y(x),y(x), singsol=all)
```

$$y(x) = e^{-\frac{x^2}{2}} c_1$$

✓ Solution by Mathematica

Time used: 0.037 (sec). Leaf size: 22

```
DSolve[y'[x]==-x*y[x],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1 e^{-\frac{x^2}{2}}$$
$$y(x) \rightarrow 0$$

3.9 problem 5 (I)

Internal problem ID [12623]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 5 (I).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [Riccati]

$$y' + y^2 = x^2$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 44

```
dsolve(diff(y(x),x)=x^2-y(x)^2,y(x), singsol=all)
```

$$y(x) = \frac{x \left(\text{BesselI} \left(-\frac{3}{4}, \frac{x^2}{2} \right) c_1 - \text{BesselK} \left(\frac{3}{4}, \frac{x^2}{2} \right) \right)}{\text{BesselI} \left(\frac{1}{4}, \frac{x^2}{2} \right) c_1 + \text{BesselK} \left(\frac{1}{4}, \frac{x^2}{2} \right)}$$

✓ Solution by Mathematica

Time used: 0.184 (sec). Leaf size: 197

```
DSolve[y'[x]==x^2-y[x]^2,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{-ix^2 \left(2 \text{BesselJ} \left(-\frac{3}{4}, \frac{ix^2}{2} \right) + c_1 \left(\text{BesselJ} \left(-\frac{5}{4}, \frac{ix^2}{2} \right) - \text{BesselJ} \left(\frac{3}{4}, \frac{ix^2}{2} \right) \right) \right) - c_1 \text{BesselJ} \left(-\frac{1}{4}, \frac{ix^2}{2} \right)}{2x \left(\text{BesselJ} \left(\frac{1}{4}, \frac{ix^2}{2} \right) + c_1 \text{BesselJ} \left(-\frac{1}{4}, \frac{ix^2}{2} \right) \right)}$$
$$y(x) \rightarrow \frac{ix^2 \text{BesselJ} \left(-\frac{5}{4}, \frac{ix^2}{2} \right) - ix^2 \text{BesselJ} \left(\frac{3}{4}, \frac{ix^2}{2} \right) + \text{BesselJ} \left(-\frac{1}{4}, \frac{ix^2}{2} \right)}{2x \text{BesselJ} \left(-\frac{1}{4}, \frac{ix^2}{2} \right)}$$

3.10 problem 5 (J)

Internal problem ID [12624]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 5 (J).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [Riccati]

$$y' - y^2 = -x^2$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 45

```
dsolve(diff(y(x),x)=y(x)^2-x^2,y(x), singsol=all)
```

$$y(x) = -\frac{x \left(\text{BesselI} \left(-\frac{3}{4}, \frac{x^2}{2} \right) c_1 - \text{BesselK} \left(\frac{3}{4}, \frac{x^2}{2} \right) \right)}{\text{BesselI} \left(\frac{1}{4}, \frac{x^2}{2} \right) c_1 + \text{BesselK} \left(\frac{1}{4}, \frac{x^2}{2} \right)}$$

✓ Solution by Mathematica

Time used: 0.178 (sec). Leaf size: 196

```
DSolve[y'[x]==y[x]^2-x^2,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{ix^2 \left(2 \text{BesselJ} \left(-\frac{3}{4}, \frac{ix^2}{2} \right) + c_1 \left(\text{BesselJ} \left(-\frac{5}{4}, \frac{ix^2}{2} \right) - \text{BesselJ} \left(\frac{3}{4}, \frac{ix^2}{2} \right) \right) \right) + c_1 \text{BesselJ} \left(-\frac{1}{4}, \frac{ix^2}{2} \right)}{2x \left(\text{BesselJ} \left(\frac{1}{4}, \frac{ix^2}{2} \right) + c_1 \text{BesselJ} \left(-\frac{1}{4}, \frac{ix^2}{2} \right) \right)}$$

$$y(x) \rightarrow -\frac{ix^2 \text{BesselJ} \left(-\frac{5}{4}, \frac{ix^2}{2} \right) - ix^2 \text{BesselJ} \left(\frac{3}{4}, \frac{ix^2}{2} \right) + \text{BesselJ} \left(-\frac{1}{4}, \frac{ix^2}{2} \right)}{2x \text{BesselJ} \left(-\frac{1}{4}, \frac{ix^2}{2} \right)}$$

3.11 problem 6

Internal problem ID [12625]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 6.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_linear, 'class A']]`

$$y' - y = x$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 13

```
dsolve(diff(y(x),x)=x+y(x),y(x), singsol=all)
```

$$y(x) = -x - 1 + c_1 e^x$$

✓ Solution by Mathematica

Time used: 0.04 (sec). Leaf size: 16

```
DSolve[y'[x]==x+y[x],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -x + c_1 e^x - 1$$

3.12 problem 7

Internal problem ID [12626]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 7.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - yx = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 12

```
dsolve(diff(y(x),x)=x*y(x),y(x), singsol=all)
```

$$y(x) = c_1 e^{\frac{x^2}{2}}$$

✓ Solution by Mathematica

Time used: 0.038 (sec). Leaf size: 22

```
DSolve[y'[x]==x*y[x],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1 e^{\frac{x^2}{2}}$$

$$y(x) \rightarrow 0$$

3.13 problem 8

Internal problem ID [12627]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 8.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - \frac{x}{y} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 23

```
dsolve(diff(y(x),x)=x/y(x),y(x), singsol=all)
```

$$y(x) = \sqrt{x^2 + c_1}$$
$$y(x) = -\sqrt{x^2 + c_1}$$

✓ Solution by Mathematica

Time used: 0.127 (sec). Leaf size: 35

```
DSolve[y'[x]==x/y[x],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\sqrt{x^2 + 2c_1}$$
$$y(x) \rightarrow \sqrt{x^2 + 2c_1}$$

3.14 problem 9

Internal problem ID [12628]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 9.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - \frac{y}{x} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 7

```
dsolve(diff(y(x),x)=y(x)/x,y(x), singsol=all)
```

$$y(x) = c_1x$$

✓ Solution by Mathematica

Time used: 0.036 (sec). Leaf size: 14

```
DSolve[y'[x]==y[x]/x,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1x$$

$$y(x) \rightarrow 0$$

3.15 problem 10

Internal problem ID [12629]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 10.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y^2 = 1$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 8

```
dsolve(diff(y(x),x)=1+y(x)^2,y(x), singsol=all)
```

$$y(x) = \tan(c_1 + x)$$

✓ Solution by Mathematica

Time used: 0.145 (sec). Leaf size: 24

```
DSolve[y'[x]==1+y[x]^2,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \tan(x + c_1)$$

$$y(x) \rightarrow -i$$

$$y(x) \rightarrow i$$

3.16 problem 11

Internal problem ID [12630]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 11.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y^2 + 3y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

```
dsolve(diff(y(x),x)=y(x)^2-3*y(x),y(x), singsol=all)
```

$$y(x) = \frac{3}{1 + 3c_1 e^{3x}}$$

✓ Solution by Mathematica

Time used: 0.352 (sec). Leaf size: 29

```
DSolve[y'[x]==y[x]^2-3*y[x],y[x],x,IncludeSingularSolutions -> True]
```

$$\begin{aligned}y(x) &\rightarrow \frac{3}{1 + e^{3(x+c_1)}} \\y(x) &\rightarrow 0 \\y(x) &\rightarrow 3\end{aligned}$$

3.17 problem 12

Internal problem ID [12631]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 12.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [Abel]

$$y' - y^3 = x^3$$

X Solution by Maple

```
dsolve(diff(y(x),x)=x^3+y(x)^3,y(x), singsol=all)
```

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

```
DSolve[y'[x]==x^3+y[x]^3,y[x],x,IncludeSingularSolutions -> True]
```

Not solved

3.18 problem 13

Internal problem ID [12632]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 13.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - |y| = 0$$

✓ Solution by Maple

Time used: 0.125 (sec). Leaf size: 19

```
dsolve(diff(y(x),x)=abs(y(x)),y(x), singsol=all)
```

$$y(x) = \frac{e^{-x}}{c_1}$$
$$y(x) = c_1 e^x$$

✓ Solution by Mathematica

Time used: 0.229 (sec). Leaf size: 29

```
DSolve[y'[x]==Abs[y[x]],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \text{InverseFunction} \left[\int_1^{\#1} \frac{1}{|K[1]|} dK[1] \& \right] [x + c_1]$$
$$y(x) \rightarrow 0$$

3.19 problem 14

Internal problem ID [12633]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 14.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [separable]

$$y' - e^{-y+x} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 9

```
dsolve(diff(y(x),x)=exp(x-y(x)),y(x), singsol=all)
```

$$y(x) = \ln(e^x + c_1)$$

✓ Solution by Mathematica

Time used: 1.319 (sec). Leaf size: 12

```
DSolve[y'[x]==Exp[x-y[x]],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \log(e^x + c_1)$$

3.20 problem 15

Internal problem ID [12634]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 15.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_homogeneous, 'class C'], _dAlembert]`

$$y' - \ln(y + x) = 0$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 29

```
dsolve(diff(y(x),x)=ln(x+y(x)),y(x), singsol=all)
```

$$y(x) = e^{\text{RootOf}(c_1 e^{-x} e^{-\text{expIntegral}_1(-Z-1)} - x)}$$

✓ Solution by Mathematica

Time used: 0.207 (sec). Leaf size: 22

```
DSolve[y'[x]==Log[x+y[x]],y[x],x,IncludeSingularSolutions -> True]
```

$$\text{Solve}\left[\frac{\text{ExpIntegralEi}(\log(x + y(x)) + 1)}{e} - x = c_1, y(x)\right]$$

3.21 problem 16

Internal problem ID [12635]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 16.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_homogeneous, 'class A'], _rational, [_Abel, '2nd type', 'cl`

$$y' - \frac{2x - y}{3y + x} = 0$$

✓ Solution by Maple

Time used: 0.079 (sec). Leaf size: 53

```
dsolve(diff(y(x),x)=(2*x-y(x))/(x+3*y(x)),y(x), singsol=all)
```

$$y(x) = \frac{-c_1 x - \sqrt{7c_1^2 x^2 + 3}}{3c_1}$$
$$y(x) = \frac{-c_1 x + \sqrt{7c_1^2 x^2 + 3}}{3c_1}$$

✓ Solution by Mathematica

Time used: 0.812 (sec). Leaf size: 114

```
DSolve[y'[x]==(2*x-y[x])/(x+3*y[x]),y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{3} \left(-x - \sqrt{7x^2 + 3e^{2c_1}} \right)$$
$$y(x) \rightarrow \frac{1}{3} \left(-x + \sqrt{7x^2 + 3e^{2c_1}} \right)$$
$$y(x) \rightarrow \frac{1}{3} \left(-\sqrt{7}\sqrt{x^2} - x \right)$$
$$y(x) \rightarrow \frac{1}{3} \left(\sqrt{7}\sqrt{x^2} - x \right)$$

3.22 problem 17

Internal problem ID [12636]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.1, page 40

Problem number: 17.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [$y'_G(x,y)$]

$$y' - \frac{1}{\sqrt{15 - x^2 - y^2}} = 0$$

X Solution by Maple

```
dsolve(diff(y(x),x)=1/sqrt(15-x^2-y(x)^2),y(x), singsol=all)
```

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

```
DSolve[y'[x]==1/Sqrt[15-x^2-y[x]^2],y[x],x,IncludeSingularSolutions -> True]
```

Not solved

4 Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

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4.1 problem 1

Internal problem ID [12637]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 1.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_linear]

$$y' - \frac{3y}{(-5+x)(x+3)} = e^{-x}$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 34

```
dsolve(diff(y(x),x)=3*y(x)/( (x-5)*(x+3))+exp(-x),y(x), singsol=all)
```

$$y(x) = \frac{\left(\int \frac{e^{-x}(x+3)^{\frac{3}{8}}}{(x-5)^{\frac{3}{8}}} dx + c_1 \right) (x-5)^{\frac{3}{8}}}{(x+3)^{\frac{3}{8}}}$$

✓ Solution by Mathematica

Time used: 15.323 (sec). Leaf size: 57

```
DSolve[y'[x]==3*y[x]/( (x-5)*(x+3))+Exp[-x],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{(5-x)^{3/8} \left(\int_1^x \frac{e^{-K[1]}(K[1]+3)^{3/8}}{(5-K[1])^{3/8}} dK[1] + c_1 \right)}{(x+3)^{3/8}}$$

4.2 problem 2

Internal problem ID [12638]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 2.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_homogeneous, 'class A'], _rational, _dAlembert]`

$$y' - \frac{xy}{x^2 + y^2} = 0$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 16

```
dsolve(diff(y(x),x)=x*y(x)/(x^2+y(x)^2),y(x), singsol=all)
```

$$y(x) = \sqrt{\frac{1}{\text{LambertW}(c_1 x^2)}} x$$

✓ Solution by Mathematica

Time used: 11.187 (sec). Leaf size: 49

```
DSolve[y'[x]==x*y[x]/(x^2+y[x]^2),y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{x}{\sqrt{W(e^{-2c_1 x^2})}}$$

$$y(x) \rightarrow \frac{x}{\sqrt{W(e^{-2c_1 x^2})}}$$

$$y(x) \rightarrow 0$$

4.3 problem 3

Internal problem ID [12639]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 3.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{1}{yx} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 25

```
dsolve(diff(y(x),x)=1/(x*y(x)),y(x), singsol=all)
```

$$y(x) = \sqrt{2 \ln(x) + c_1}$$
$$y(x) = -\sqrt{2 \ln(x) + c_1}$$

✓ Solution by Mathematica

Time used: 0.1 (sec). Leaf size: 40

```
DSolve[y'[x]==1/(x*y[x]),y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\sqrt{2} \sqrt{\log(x) + c_1}$$
$$y(x) \rightarrow \sqrt{2} \sqrt{\log(x) + c_1}$$

4.4 problem 4

Internal problem ID [12640]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 4.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - \ln(y - 1) = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 16

```
dsolve(diff(y(x),x)=ln(y(x)-1),y(x), singsol=all)
```

$$y(x) = e^{\text{RootOf}(x + \exp(\text{Integral}_1(-_Z) + c_1))} + 1$$

✓ Solution by Mathematica

Time used: 0.29 (sec). Leaf size: 21

```
DSolve[y'[x]==Log[y[x]-1],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \text{InverseFunction}[\text{LogIntegral}(\#1 - 1)\&][x + c_1]$$
$$y(x) \rightarrow 2$$

4.5 problem 5

Internal problem ID [12641]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 5.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - \sqrt{(y+2)(y-1)} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 30

```
dsolve(diff(y(x),x)=sqrt((y(x)+2)*(y(x)-1)),y(x), singsol=all)
```

$$x + \ln(2) - \ln\left(1 + 2y(x) + 2\sqrt{(y(x)+2)(-1+y(x))}\right) + c_1 = 0$$

✓ Solution by Mathematica

Time used: 0.497 (sec). Leaf size: 41

```
DSolve[y'[x]==Sqrt[(y[x]+2)*(y[x]-1)],y[x],x,IncludeSingularSolutions->True]
```

$$\begin{aligned}y(x) &\rightarrow \frac{1}{4}(-e^{-x-c_1} - 9e^{x+c_1} - 2) \\y(x) &\rightarrow -2 \\y(x) &\rightarrow 1\end{aligned}$$

4.6 problem 6

Internal problem ID [12642]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 6.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_homogeneous, 'class A', _rational, [_Abel, '2nd type', 'cl`

$$y' - \frac{y}{y-x} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 31

```
dsolve(diff(y(x),x)=y(x)/(y(x)-x),y(x), singsol=all)
```

$$y(x) = x - \sqrt{x^2 - 2c_1}$$

$$y(x) = x + \sqrt{x^2 - 2c_1}$$

✓ Solution by Mathematica

Time used: 0.836 (sec). Leaf size: 80

```
DSolve[y'[x]==y[x]/(y[x]-x),y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow x - \sqrt{x^2 - e^{2c_1}}$$

$$y(x) \rightarrow x + \sqrt{x^2 - e^{2c_1}}$$

$$y(x) \rightarrow 0$$

$$y(x) \rightarrow x - \sqrt{x^2}$$

$$y(x) \rightarrow \sqrt{x^2} + x$$

4.7 problem 7

Internal problem ID [12643]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 7.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - \frac{x}{y^2} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 65

```
dsolve(diff(y(x),x)=x/y(x)^2,y(x), singsol=all)
```

$$y(x) = \frac{(12x^2 + 8c_1)^{\frac{1}{3}}}{2}$$
$$y(x) = -\frac{(12x^2 + 8c_1)^{\frac{1}{3}} (1 + i\sqrt{3})}{4}$$
$$y(x) = \frac{(12x^2 + 8c_1)^{\frac{1}{3}} (i\sqrt{3} - 1)}{4}$$

✓ Solution by Mathematica

Time used: 0.283 (sec). Leaf size: 79

```
DSolve[y'[x]==x/y[x]^2,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\sqrt[3]{-\frac{3}{2}\sqrt[3]{x^2 + 2c_1}}$$
$$y(x) \rightarrow \sqrt[3]{\frac{3}{2}\sqrt[3]{x^2 + 2c_1}}$$
$$y(x) \rightarrow (-1)^{2/3}\sqrt[3]{\frac{3}{2}\sqrt[3]{x^2 + 2c_1}}$$

4.8 problem 8

Internal problem ID [12644]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 8.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{\sqrt{y}}{x} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

```
dsolve(diff(y(x),x)=sqrt(y(x))/x,y(x), singsol=all)
```

$$\sqrt{y(x)} - \frac{\ln(x)}{2} - c_1 = 0$$

✓ Solution by Mathematica

Time used: 0.202 (sec). Leaf size: 21

```
DSolve[y'[x]==Sqrt[y[x]]/x,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{4}(\log(x) + c_1)^2$$
$$y(x) \rightarrow 0$$

4.9 problem 9

Internal problem ID [12645]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 9.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - \frac{xy}{1-y} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

```
dsolve(diff(y(x),x)=x*y(x)/(1-y(x)),y(x), singsol=all)
```

$$y(x) = -\text{LambertW}\left(-e^{\frac{x^2}{2}+c_1}\right)$$

✓ Solution by Mathematica

Time used: 3.96 (sec). Leaf size: 29

```
DSolve[y'[x]==x*y[x]/(1-y[x]),y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -W\left(-e^{\frac{x^2}{2}-c_1}\right)$$

$$y(x) \rightarrow 0$$

4.10 problem 10

Internal problem ID [12646]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 10.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_homogeneous, 'class G']]`

$$y' - (yx)^{\frac{1}{3}} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 87

```
dsolve(diff(y(x),x)=(x*y(x))^(1/3),y(x), singsol=all)
```

$$\frac{\left((-4x^5c_1 + 32y(x)^2c_1x + 2x)(y(x)x)^{\frac{2}{3}} + (x^3 + 4(y(x)x)^{\frac{1}{3}}y(x))(x^4c_1 - 8c_1y(x)^2 + 1) \right) x}{(x^4 - 8y(x)^2) \left(-2(y(x)x)^{\frac{2}{3}} + x^2 \right)^2} = 0$$

✓ Solution by Mathematica

Time used: 4.979 (sec). Leaf size: 35

```
DSolve[y'[x]==(x*y[x])^(1/3),y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{(3x^{4/3} + 4c_1)^{3/2}}{6\sqrt{6}}$$
$$y(x) \rightarrow 0$$

4.11 problem 11

Internal problem ID [12647]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 11.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_homogeneous, 'class C'], _dAlembert]`

$$y' - \sqrt{\frac{y-4}{x}} = 0$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 38

```
dsolve(diff(y(x),x)=sqrt( (y(x)-4)/x ),y(x), singsol=all)
```

$$-\ln\left(\frac{-y(x)+4+x}{x}\right) + 2 \operatorname{arctanh}\left(\sqrt{\frac{y(x)-4}{x}}\right) - \ln(x) - c_1 = 0$$

✓ Solution by Mathematica

Time used: 0.294 (sec). Leaf size: 29

```
DSolve[y'[x]==Sqrt[(y[x]-4)/x],y[x],x,IncludeSingularSolutions->True]
```

$$y(x) \rightarrow x + c_1\sqrt{x} + 4 + \frac{c_1^2}{4}$$
$$y(x) \rightarrow 4$$

4.12 problem 12

Internal problem ID [12648]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 12.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_homogeneous, 'class G', _rational, _Bernoulli]`

$$y' + \frac{y}{x} - y^{\frac{1}{4}} = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 17

```
dsolve(diff(y(x),x)=-y(x)/x+y(x)^(1/4),y(x), singsol=all)
```

$$y(x)^{\frac{3}{4}} - \frac{3x}{7} - \frac{c_1}{x^{\frac{3}{4}}} = 0$$

✓ Solution by Mathematica

Time used: 9.843 (sec). Leaf size: 31

```
DSolve[y'[x]==-y[x]/x+y[x]^(1/4),y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{(3x + \frac{7c_1}{x^{3/4}})^{4/3}}{7\sqrt[3]{7}}$$

4.13 problem 13

Internal problem ID [12649]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 13.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - 4y = -5$$

With initial conditions

$$[y(1) = 4]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 14

```
dsolve([diff(y(x),x)=4*y(x)-5,y(1) = 4],y(x), singsol=all)
```

$$y(x) = \frac{5}{4} + \frac{11 e^{-4+4x}}{4}$$

✓ Solution by Mathematica

Time used: 0.043 (sec). Leaf size: 20

```
DSolve[{y'[x]==4*y[x]-5,{y[1]==4}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{11}{4} e^{4x-4} + \frac{5}{4}$$

4.14 problem 14

Internal problem ID [12650]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 14.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + 3y = 1$$

With initial conditions

$$[y(-2) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 14

```
dsolve([diff(y(x),x)+3*y(x)=1,y(-2) = 1],y(x), singsol=all)
```

$$y(x) = \frac{1}{3} + \frac{2e^{-6-3x}}{3}$$

✓ Solution by Mathematica

Time used: 0.04 (sec). Leaf size: 20

```
DSolve[{y'[x]+3*y[x]==1,{y[-2]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{2}{3}e^{-3(x+2)} + \frac{1}{3}$$

4.15 problem 15

Internal problem ID [12651]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 15.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - ay = b$$

With initial conditions

$$[y(c) = d]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 27

```
dsolve([diff(y(x),x)=a*y(x)+b,y(c) = d],y(x), singsol=all)
```

$$y(x) = \frac{(ad + b)e^{-a(c-x)} - b}{a}$$

✓ Solution by Mathematica

Time used: 0.06 (sec). Leaf size: 39

```
DSolve[{y'[x]==a*y[x]+b,{y[c]==d}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{e^{-ac}(b(e^{ax} - e^{ac}) + ade^{ax})}{a}$$

4.16 problem 16

Internal problem ID [12652]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 16.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = x^2 + e^x - \sin(x)$$

With initial conditions

$$[y(2) = -1]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 23

```
dsolve([diff(y(x),x)=x^2+exp(x)-sin(x),y(2) = -1],y(x), singsol=all)
```

$$y(x) = \frac{x^3}{3} + \cos(x) + e^x - \frac{11}{3} - \cos(2) - e^2$$

✓ Solution by Mathematica

Time used: 0.023 (sec). Leaf size: 30

```
DSolve[{y'[x]==x^2+Exp[x]-Sin[x]},{y[2]==-1}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{x^3}{3} + e^x + \cos(x) - e^2 - \frac{11}{3} - \cos(2)$$

4.17 problem 17

Internal problem ID [12653]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 17.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - yx = \frac{1}{x^2 + 1}$$

With initial conditions

$$[y(-5) = 0]$$

✓ Solution by Maple

Time used: 0.046 (sec). Leaf size: 31

```
dsolve([diff(y(x),x)=x*y(x)+1/(1+x^2),y(-5) = 0],y(x), singsol=all)
```

$$y(x) = \left(\int_{-5}^x \frac{e^{-\frac{z^2}{2}}}{-z^2 + 1} d_{-}z \right) e^{\frac{x^2}{2}}$$

✓ Solution by Mathematica

Time used: 0.478 (sec). Leaf size: 41

```
DSolve[{y'[x]==x*y[x]+1/(1+x^2)},{y[-5]==0}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{\frac{x^2}{2}} \int_{-5}^x \frac{e^{-\frac{1}{2}K[1]^2}}{K[1]^2 + 1} dK[1]$$

4.18 problem 18

Internal problem ID [12654]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 18.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - \frac{y}{x} = \cos(x)$$

With initial conditions

$$[y(-1) = 0]$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 17

```
dsolve([diff(y(x),x)=y(x)/x+cos(x),y(-1) = 0],y(x), singsol=all)
```

$$y(x) = (\text{Ci}(x) - \text{Ci}(1) - i\pi) x$$

✓ Solution by Mathematica

Time used: 0.058 (sec). Leaf size: 14

```
DSolve[{y'[x]==y[x]/x+Cos[x],{y[-1]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow x(\text{CosIntegral}(x) - \text{CosIntegral}(-1))$$

4.19 problem 19

Internal problem ID [12655]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 19.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_linear]

$$y' - \frac{y}{x} = \tan(x)$$

With initial conditions

$$[y(\pi) = 0]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 18

```
dsolve([diff(y(x),x)=y(x)/x+tan(x),y(Pi) = 0],y(x), singsol=all)
```

$$y(x) = \left(\int_{\pi}^x \frac{\tan(z)}{z} dz \right) x$$

✓ Solution by Mathematica

Time used: 1.98 (sec). Leaf size: 22

```
DSolve[{y'[x]==y[x]/x+Tan[x],{y[Pi]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow x \int_{\pi}^x \frac{\tan(K[1])}{K[1]} dK[1]$$

4.20 problem 20

Internal problem ID [12656]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 20.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - \frac{y}{-x^2 + 4} = \sqrt{x}$$

With initial conditions

$$[y(3) = 4]$$

✓ Solution by Maple

Time used: 0.062 (sec). Leaf size: 41

```
dsolve([diff(y(x),x)=y(x)/(4-x^2)+sqrt(x),y(3) = 4],y(x), singsol=all)
```

$$y(x) = \frac{\left(4 \cdot 5^{\frac{3}{4}} + 5 \left(\int_3^x \frac{\sqrt{-z1} (-z1-2)^{\frac{1}{4}}}{(2+z1)^{\frac{1}{4}}} d_z1 \right)\right) (x+2)^{\frac{1}{4}}}{5 (x-2)^{\frac{1}{4}}}$$

✓ Solution by Mathematica

Time used: 2.843 (sec). Leaf size: 202

```
DSolve[{y'[x]==y[x]/(4-x^2)+Sqrt[x],{y[3]==4}],y[x],x,IncludeSingularSolutions -> True]
```

$y(x)$

$\rightarrow \left(\frac{1}{45} + \frac{i}{45}\right) \sqrt[4]{x+2} \left((10-10i)x^{3/2} \text{AppellF1}\left(\frac{3}{2}, \frac{3}{4}, \frac{1}{4}, \frac{5}{2}, \frac{x}{2}, -\frac{x}{2}\right) - (30-30i)\sqrt{x} \text{AppellF1}\left(\frac{1}{2}, \frac{3}{4}, \frac{1}{4}, \frac{3}{2}, \frac{x}{2}, -\frac{x}{2}\right)\right)$

4.21 problem 21

Internal problem ID [12657]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 21.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - \frac{y}{-x^2 + 4} = \sqrt{x}$$

With initial conditions

$$[y(1) = -3]$$

✓ Solution by Maple

Time used: 0.063 (sec). Leaf size: 44

```
dsolve([diff(y(x),x)=y(x)/(4-x^2)+sqrt(x),y(1) = -3],y(x), singsol=all)
```

$$y(x) = -\frac{(x+2)^{\frac{1}{4}} \left(-2 \left(\int_1^x \frac{\sqrt{-z1} (-z1-2)^{\frac{1}{4}}}{(2+z1)^{\frac{1}{4}}} d_z1 \right) + (1+i) \sqrt{2} 3^{\frac{3}{4}} \right)}{2(x-2)^{\frac{1}{4}}}$$

✓ Solution by Mathematica

Time used: 0.145 (sec). Leaf size: 158

```
DSolve[{y'[x]==y[x]/(4-x^2)+Sqrt[x],{y[1]==-3}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{\sqrt[4]{x+2} (4x^{3/2} \text{AppellF1}\left(\frac{3}{2}, \frac{3}{4}, \frac{1}{4}, \frac{5}{2}, \frac{x}{2}, -\frac{x}{2}\right) - 12\sqrt{x} \text{AppellF1}\left(\frac{1}{2}, \frac{3}{4}, \frac{1}{4}, \frac{3}{2}, \frac{x}{2}, -\frac{x}{2}\right) - 4 \text{AppellF1}\left(\frac{3}{2}, \frac{3}{4}, \frac{1}{4}, \frac{5}{2}, \frac{x}{2}, -\frac{x}{2}\right))}{9\sqrt[4]{2-x}}$$

4.22 problem 22

Internal problem ID [12658]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 22.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - y \cot(x) = \csc(x)$$

With initial conditions

$$\left[y\left(\frac{\pi}{2}\right) = 1 \right]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 11

```
dsolve([diff(y(x),x)=cot(x)*y(x)+csc(x),y(1/2*Pi) = 1],y(x), singsol=all)
```

$$y(x) = -\cos(x) + \sin(x)$$

✓ Solution by Mathematica

Time used: 0.082 (sec). Leaf size: 12

```
DSolve[{y'[x]==Cot[x]*y[x]+Csc[x],{y[Pi/2]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \sin(x) - \cos(x)$$

4.23 problem 23

Internal problem ID [12659]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 23.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' + x\sqrt{1-y^2} = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 5

```
dsolve([diff(y(x),x)=-x*sqrt(1-y(x)^2),y(0) = 1],y(x), singsol=all)
```

$$y(x) = 1$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 6

```
DSolve[{y'[x]==-x*Sqrt[1-y[x]^2],{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 1$$

4.24 problem 24

Internal problem ID [12660]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.2, page 53

Problem number: 24.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_1st_order, _with_linear_symmetries], _Clairaut]`

$$y' - \frac{\sqrt{x^2 + 4y}}{2} = -\frac{x}{2}$$

With initial conditions

$$[y(6) = -9]$$

✓ Solution by Maple

Time used: 1.328 (sec). Leaf size: 17

```
dsolve([diff(y(x),x)=(-x+sqrt(x^2+4*y(x)))/2,y(6) = -9],y(x), singsol=all)
```

$$y(x) = 9 - 3x$$
$$y(x) = -\frac{x^2}{4}$$

✓ Solution by Mathematica

Time used: 0.987 (sec). Leaf size: 10

```
DSolve[{y'[x]==(-x+Sqrt[x^2+4*y[x]])/2,{y[6]==-9}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 9 - 3x$$

5 Chapter 2. The Initial Value Problem. Exercises

2.3.1, page 57

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5.1 problem 1

Internal problem ID [12661]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.1, page 57

Problem number: 1.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = 3x + 1$$

With initial conditions

$$[y(1) = 2]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 12

```
dsolve([diff(y(x),x)=3*x+1,y(1) = 2],y(x), singsol=all)
```

$$y(x) = \frac{3}{2}x^2 + x - \frac{1}{2}$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 17

```
DSolve[{y'[x]==3*x+1,{y[1]==2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{3x^2}{2} + x - \frac{1}{2}$$

5.2 problem 2

Internal problem ID [12662]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.1, page 57

Problem number: 2.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = x + \frac{1}{x}$$

With initial conditions

$$[y(1) = 2]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 13

```
dsolve([diff(y(x),x)=x+1/x,y(1) = 2],y(x), singsol=all)
```

$$y(x) = \frac{x^2}{2} + \ln(x) + \frac{3}{2}$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 18

```
DSolve[{y'[x]==x+1/x,{y[1]==2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{2}(x^2 + 2\log(x) + 3)$$

5.3 problem 3

Internal problem ID [12663]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.1, page 57

Problem number: 3.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = 2 \sin(x)$$

With initial conditions

$$[y(\pi) = 1]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 10

```
dsolve([diff(y(x),x)=2*sin(x),y(Pi) = 1],y(x), singsol=all)
```

$$y(x) = -2 \cos(x) - 1$$

✓ Solution by Mathematica

Time used: 0.009 (sec). Leaf size: 11

```
DSolve[{y'[x]==2*Sin[x],{y[Pi]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -2 \cos(x) - 1$$

5.4 problem 4

Internal problem ID [12664]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.1, page 57

Problem number: 4.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = x \sin(x)$$

With initial conditions

$$\left[y\left(\frac{\pi}{2}\right) = 1 \right]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 12

```
dsolve([diff(y(x),x)=x*sin(x),y(1/2*Pi) = 1],y(x), singsol=all)
```

$$y(x) = \sin(x) - \cos(x)x$$

✓ Solution by Mathematica

Time used: 0.011 (sec). Leaf size: 13

```
DSolve[{y'[x]==x*Sin[x],{y[Pi/2]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \sin(x) - x \cos(x)$$

5.5 problem 5

Internal problem ID [12665]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.1, page 57

Problem number: 5.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = \frac{1}{x-1}$$

With initial conditions

$$[y(2) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 10

```
dsolve([diff(y(x),x)=1/(x-1),y(2) = 1],y(x), singsol=all)
```

$$y(x) = \ln(-1 + x) + 1$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 11

```
DSolve[{y'[x]==1/(x-1)},{y[2]==1}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \log(x - 1) + 1$$

5.6 problem 6

Internal problem ID [12666]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.1, page 57

Problem number: 6.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = \frac{1}{x-1}$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 14

```
dsolve([diff(y(x),x)=1/(x-1),y(0) = 1],y(x), singsol=all)
```

$$y(x) = \ln(-1 + x) + 1 - i\pi$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 16

```
DSolve[{y'[x]==1/(x-1)},{y[0]==1}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \log(x - 1) - i\pi + 1$$

5.7 problem 7

Internal problem ID [12667]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.1, page 57

Problem number: 7.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = \frac{1}{x^2 - 1}$$

With initial conditions

$$[y(2) = 1]$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 16

```
dsolve([diff(y(x),x)=1/(x^2-1),y(2) = 1],y(x), singsol=all)
```

$$y(x) = -\operatorname{arctanh}(x) + 1 + \operatorname{arctanh}\left(\frac{1}{2}\right) - \frac{i\pi}{2}$$

✓ Solution by Mathematica

Time used: 0.008 (sec). Leaf size: 28

```
DSolve[{y'[x]==1/(x^2-1)},{y[2]==1}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{2}(\log(3 - 3x) - \log(x + 1) - i\pi + 2)$$

5.8 problem 8

Internal problem ID [12668]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.1, page 57

Problem number: 8.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = \frac{1}{x^2 - 1}$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 10

```
dsolve([diff(y(x),x)=1/(x^2-1),y(0) = 1],y(x), singsol=all)
```

$$y(x) = -\operatorname{arctanh}(x) + 1$$

✓ Solution by Mathematica

Time used: 0.008 (sec). Leaf size: 23

```
DSolve[{y'[x]==1/(x^2-1)},{y[0]==1}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{2}(\log(1-x) - \log(x+1) + 2)$$

5.9 problem 9

Internal problem ID [12669]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.1, page 57

Problem number: 9.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = \tan(x)$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 9

```
dsolve([diff(y(x),x)=tan(x),y(0) = 0],y(x), singsol=all)
```

$$y(x) = -\ln(\cos(x))$$

✓ Solution by Mathematica

Time used: 0.009 (sec). Leaf size: 10

```
DSolve[{y'[x]==Tan[x],{y[0]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\log(\cos(x))$$

5.10 problem 10

Internal problem ID [12670]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.1, page 57

Problem number: 10.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = \tan(x)$$

With initial conditions

$$[y(\pi) = 0]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 14

```
dsolve([diff(y(x),x)=tan(x),y(Pi) = 0],y(x), singsol=all)
```

$$y(x) = -\ln(\cos(x)) + i\pi$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 16

```
DSolve[{y'[x]==Tan[x],{y[Pi]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\log(\cos(x)) + i\pi$$

6 Chapter 2. The Initial Value Problem. Exercises

2.3.2, page 63

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6.1 problem 1

Internal problem ID [12671]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 1.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - 3y = 0$$

With initial conditions

$$[y(0) = -1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 10

```
dsolve([diff(y(x),x)=3*y(x),y(0) = -1],y(x), singsol=all)
```

$$y(x) = -e^{3x}$$

✓ Solution by Mathematica

Time used: 0.039 (sec). Leaf size: 12

```
DSolve[{y'[x]==3*y[x],{y[0]==-1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -e^{3x}$$

6.2 problem 2

Internal problem ID [12672]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 2.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + y = 1$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 5

```
dsolve([diff(y(x),x)=-y(x)+1,y(0) = 1],y(x), singsol=all)
```

$$y(x) = 1$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 6

```
DSolve[{y'[x]==-y[x]+1,{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 1$$

6.3 problem 3

Internal problem ID [12673]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 3.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + y = 1$$

With initial conditions

$$[y(0) = 2]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 10

```
dsolve([diff(y(x),x)=-y(x)+1,y(0) = 2],y(x), singsol=all)
```

$$y(x) = e^{-x} + 1$$

✓ Solution by Mathematica

Time used: 0.04 (sec). Leaf size: 12

```
DSolve[{y'[x]==-y[x]+1,{y[0]==2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{-x} + 1$$

6.4 problem 4

Internal problem ID [12674]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 4.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - x e^{-x^2+y} = 0$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 0.062 (sec). Leaf size: 19

```
dsolve([diff(y(x),x)=x*exp(y(x)-x^2),y(0) = 0],y(x), singsol=all)
```

$$y(x) = \ln(2) - \ln(1 + e^{x^2}) + x^2$$

✓ Solution by Mathematica

Time used: 2.198 (sec). Leaf size: 21

```
DSolve[{y'[x]==x*Exp[y[x]-x^2],{y[0]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\log\left(\frac{1}{2}(e^{-x^2} + 1)\right)$$

6.5 problem 5

Internal problem ID [12675]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 5.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{y}{x} = 0$$

With initial conditions

$$[y(-1) = 2]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 7

```
dsolve([diff(y(x),x)=y(x)/x,y(-1) = 2],y(x), singsol=all)
```

$$y(x) = -2x$$

✓ Solution by Mathematica

Time used: 0.036 (sec). Leaf size: 8

```
DSolve[{y'[x]==y[x]/x,{y[-1]==2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -2x$$

6.6 problem 6

Internal problem ID [12676]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 6.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [separable]

$$y' - \frac{2x}{y} = 0$$

With initial conditions

$$[y(0) = 2]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 13

```
dsolve([diff(y(x),x)=2*x/y(x),y(0) = 2],y(x), singsol=all)
```

$$y(x) = \sqrt{2x^2 + 4}$$

✓ Solution by Mathematica

Time used: 0.121 (sec). Leaf size: 20

```
DSolve[{y'[x]==2*x/y[x],{y[0]==2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \sqrt{2}\sqrt{x^2 + 2}$$

6.7 problem 7

Internal problem ID [12677]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 7.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + 2y - y^2 = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 14

```
dsolve([diff(y(x),x)=-2*y(x)+y(x)^2,y(0) = 1],y(x), singsol=all)
```

$$y(x) = \frac{2}{e^{2x} + 1}$$

✓ Solution by Mathematica

Time used: 0.013 (sec). Leaf size: 16

```
DSolve[{y'[x]==-2*y[x]+y[x]^2,{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{2}{e^{2x} + 1}$$

6.8 problem 8

Internal problem ID [12678]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 8.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - yx = x$$

With initial conditions

$$[y(1) = 2]$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 17

```
dsolve([diff(y(x),x)=x*y(x)+x,y(1) = 2],y(x), singsol=all)
```

$$y(x) = -1 + 3e^{\frac{(-1+x)(1+x)}{2}}$$

✓ Solution by Mathematica

Time used: 0.099 (sec). Leaf size: 20

```
DSolve[{y'[x]==x*y[x]+x,{y[1]==2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 3e^{\frac{1}{2}(x^2-1)} - 1$$

6.9 problem 9

Internal problem ID [12679]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 9.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$x e^y + y' = 0$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 0.063 (sec). Leaf size: 15

```
dsolve([x*exp(y(x))+diff(y(x),x)=0,y(0) = 0],y(x), singsol=all)
```

$$y(x) = \ln(2) - \ln(x^2 + 2)$$

✓ Solution by Mathematica

Time used: 0.476 (sec). Leaf size: 16

```
DSolve[{x*Exp[y[x]]+y'[x]==0,{y[0]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \log(2) - \log(x^2 + 2)$$

6.10 problem 10

Internal problem ID [12680]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 10.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y - x^2 y' = 0$$

With initial conditions

$$[y(1) = 1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 13

```
dsolve([y(x)-x^2*diff(y(x),x)=0,y(1) = 1],y(x), singsol=all)
```

$$y(x) = e^{\frac{-1+x}{x}}$$

✓ Solution by Mathematica

Time used: 0.04 (sec). Leaf size: 14

```
DSolve[{y[x]-x^2*y'[x]==0,{y[1]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{1-\frac{1}{x}}$$

6.11 problem 11

Internal problem ID [12681]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 11.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$2yy' = 1$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 19

```
dsolve(2*y(x)*diff(y(x),x)=1,y(x), singsol=all)
```

$$y(x) = \sqrt{c_1 + x}$$
$$y(x) = -\sqrt{c_1 + x}$$

✓ Solution by Mathematica

Time used: 0.019 (sec). Leaf size: 31

```
DSolve[2*y[x]*y'[x]==1,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\sqrt{x + 2c_1}$$
$$y(x) \rightarrow \sqrt{x + 2c_1}$$

6.12 problem 12

Internal problem ID [12682]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 12.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$2xyy' + y^2 = -1$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 34

```
dsolve(2*x*y(x)*diff(y(x),x)+y(x)^2=-1,y(x), singsol=all)
```

$$y(x) = \frac{\sqrt{x(c_1 - x)}}{x}$$
$$y(x) = -\frac{\sqrt{x(c_1 - x)}}{x}$$

✓ Solution by Mathematica

Time used: 0.471 (sec). Leaf size: 98

```
DSolve[2*x*y[x]*y'[x]+y[x]^2== -1,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{\sqrt{-x + e^{2c_1}}}{\sqrt{x}}$$
$$y(x) \rightarrow \frac{\sqrt{-x + e^{2c_1}}}{\sqrt{x}}$$
$$y(x) \rightarrow -i$$
$$y(x) \rightarrow i$$
$$y(x) \rightarrow \frac{\sqrt{-x}}{\sqrt{x}}$$
$$y(x) \rightarrow \frac{\sqrt{x}}{\sqrt{-x}}$$

6.13 problem 13

Internal problem ID [12683]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 13.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - \frac{1 - yx}{x^2} = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 12

```
dsolve(diff(y(x),x)=(1-x*y(x))/x^2,y(x), singsol=all)
```

$$y(x) = \frac{\ln(x) + c_1}{x}$$

✓ Solution by Mathematica

Time used: 0.039 (sec). Leaf size: 14

```
DSolve[y'[x]==(1-x*y[x])/x^2,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{\log(x) + c_1}{x}$$

6.14 problem 14

Internal problem ID [12684]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 14.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_homogeneous, 'class A'], _rational, [_Abel, '2nd type', 'cl`

$$y' + \frac{y(2x + y)}{x(x + 2y)} = 0$$

✓ Solution by Maple

Time used: 0.062 (sec). Leaf size: 71

```
dsolve(diff(y(x),x)=-y(x)*(2*x+y(x))/(x*(2*y(x)+x)),y(x), singsol=all)
```

$$y(x) = \frac{-c_1^2 x^2 + \sqrt{c_1 x (c_1^3 x^3 + 4)}}{2c_1^2 x}$$
$$y(x) = \frac{-c_1^2 x^2 - \sqrt{c_1 x (c_1^3 x^3 + 4)}}{2c_1^2 x}$$

✓ Solution by Mathematica

Time used: 1.084 (sec). Leaf size: 118

```
DSolve[y'[x]==-y[x]*(2*x+y[x])/(x*(2*y[x]+x)),y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{2} \left(-x - \frac{\sqrt{x^3 + 4e^{c_1}}}{\sqrt{x}} \right)$$

$$y(x) \rightarrow \frac{1}{2} \left(-x + \frac{\sqrt{x^3 + 4e^{c_1}}}{\sqrt{x}} \right)$$

$$y(x) \rightarrow -\frac{x^{3/2} + \sqrt{x^3}}{2\sqrt{x}}$$

$$y(x) \rightarrow \frac{\sqrt{x^3}}{2\sqrt{x}} - \frac{x}{2}$$

6.15 problem 15

Internal problem ID [12685]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.2, page 63

Problem number: 15.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_homogeneous, 'class G', _rational, [_Abel, '2nd type', 'cl`

$$y' - \frac{y^2}{1 - yx} = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 17

```
dsolve(diff(y(x),x)=y(x)^2/(1-x*y(x)),y(x), singsol=all)
```

$$y(x) = -\frac{\text{LambertW}(-x e^{-c_1})}{x}$$

✓ Solution by Mathematica

Time used: 3.256 (sec). Leaf size: 25

```
DSolve[y'[x]==y[x]^2/(1-x*y[x]),y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{W(-e^{-c_1}x)}{x}$$
$$y(x) \rightarrow 0$$

7 Chapter 2. The Initial Value Problem. Exercises

2.3.3, page 71

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7.1 problem 1

Internal problem ID [12686]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 1.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - 4y = 1$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 12

```
dsolve([diff(y(x),x)=4*y(x)+1,y(0) = 1],y(x), singsol=all)
```

$$y(x) = -\frac{1}{4} + \frac{5e^{4x}}{4}$$

✓ Solution by Mathematica

Time used: 0.043 (sec). Leaf size: 18

```
DSolve[{y'[x]==4*y[x]+1,{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{4}(5e^{4x} - 1)$$

7.2 problem 2

Internal problem ID [12687]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 2.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - yx = 2$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 27

```
dsolve([diff(y(x),x)=x*y(x)+2,y(0) = 1],y(x), singsol=all)
```

$$y(x) = \left(\sqrt{\pi} \sqrt{2} \operatorname{erf}\left(\frac{x\sqrt{2}}{2}\right) + 1 \right) e^{\frac{x^2}{2}}$$

✓ Solution by Mathematica

Time used: 0.053 (sec). Leaf size: 33

```
DSolve[{y'[x]==x*y[x]+2,{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{\frac{x^2}{2}} \left(\sqrt{2\pi} \operatorname{erf}\left(\frac{x}{\sqrt{2}}\right) + 1 \right)$$

7.3 problem 3

Internal problem ID [12688]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 3.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - \frac{y}{x} = 0$$

With initial conditions

$$[y(-1) = 2]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 7

```
dsolve([diff(y(x),x)=y(x)/x,y(-1) = 2],y(x), singsol=all)
```

$$y(x) = -2x$$

✓ Solution by Mathematica

Time used: 0.038 (sec). Leaf size: 8

```
DSolve[{y'[x]==y[x]/x,{y[-1]==2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -2x$$

7.4 problem 4

Internal problem ID [12689]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 4.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - \frac{y}{x-1} = x^2$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 24

```
dsolve([diff(y(x),x)=y(x)/(x-1)+x^2,y(0) = 1],y(x), singsol=all)
```

$$y(x) = \left(\frac{x^2}{2} + x + \ln(-1+x) - 1 - i\pi \right) (-1+x)$$

✓ Solution by Mathematica

Time used: 0.06 (sec). Leaf size: 31

```
DSolve[{y'[x]==y[x]/(x-1)+x^2,{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{2}(x-1)(x^2 + 2x + 2\log(x-1) - 2i\pi - 2)$$

7.5 problem 5

Internal problem ID [12690]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 5.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - \frac{y}{x} = \sin(x^2)$$

With initial conditions

$$[y(-1) = -1]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 17

```
dsolve([diff(y(x),x)=y(x)/x+sin(x^2),y(-1) = -1],y(x), singsol=all)
```

$$y(x) = -\frac{(-\text{Si}(x^2) - 2 + \text{Si}(1))x}{2}$$

✓ Solution by Mathematica

Time used: 0.067 (sec). Leaf size: 20

```
DSolve[{y'[x]==y[x]/x+Sin[x^2],{y[-1]==-1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{2}x(\text{Si}(x^2) - \text{Si}(1) + 2)$$

7.6 problem 6

Internal problem ID [12691]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 6.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - \frac{2y}{x} = e^x$$

With initial conditions

$$\left[y(1) = \frac{1}{2} \right]$$

✓ Solution by Maple

Time used: 0.078 (sec). Leaf size: 29

```
dsolve([diff(y(x),x)=2*y(x)/x+exp(x),y(1) = 1/2],y(x), singsol=all)
```

$$y(x) = -\exp\text{Integral}_1(-x)x^2 + \exp\text{Integral}_1(-1)x^2 + \frac{(2xe + x - 2e^x)x}{2}$$

✓ Solution by Mathematica

Time used: 0.116 (sec). Leaf size: 31

```
DSolve[{y'[x]==2*y[x]/x+Exp[x],{y[1]==1/2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{2}x(2x \text{ExpIntegralEi}(x) - 2 \text{ExpIntegralEi}(1)x + 2ex + x - 2e^x)$$

7.7 problem 7

Internal problem ID [12692]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 7.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_linear`]

$$y' - y \cot(x) = \sin(x)$$

With initial conditions

$$\left[y\left(\frac{\pi}{2}\right) = 0 \right]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 12

```
dsolve([diff(y(x),x)=cot(x)*y(x)+sin(x),y(1/2*Pi) = 0],y(x), singsol=all)
```

$$y(x) = \left(-\frac{\pi}{2} + x\right) \sin(x)$$

✓ Solution by Mathematica

Time used: 0.088 (sec). Leaf size: 16

```
DSolve[{y'[x]==Cot[x]*y[x]+Sin[x],{y[Pi/2]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{1}{2}(\pi - 2x) \sin(x)$$

7.8 problem 12

Internal problem ID [12693]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 12.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$-yy' = -x$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 23

```
dsolve(x-y(x)*diff(y(x),x)=0,y(x), singsol=all)
```

$$y(x) = \sqrt{x^2 + c_1}$$
$$y(x) = -\sqrt{x^2 + c_1}$$

✓ Solution by Mathematica

Time used: 0.132 (sec). Leaf size: 35

```
DSolve[x-y[x]*y'[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\sqrt{x^2 + 2c_1}$$
$$y(x) \rightarrow \sqrt{x^2 + 2c_1}$$

7.9 problem 13

Internal problem ID [12694]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 13.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y - y'x = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 7

```
dsolve(y(x)-x*diff(y(x),x)=0,y(x), singsol=all)
```

$$y(x) = c_1x$$

✓ Solution by Mathematica

Time used: 0.037 (sec). Leaf size: 14

```
DSolve[y[x]-x*y'[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1x$$

$$y(x) \rightarrow 0$$

7.10 problem 14

Internal problem ID [12695]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 14.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y'x - y = -x^2$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 11

```
dsolve((x^2-y(x))+x*diff(y(x),x)=0,y(x), singsol=all)
```

$$y(x) = x(c_1 - x)$$

✓ Solution by Mathematica

Time used: 0.044 (sec). Leaf size: 13

```
DSolve[(x^2-y[x])+x*y'[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow x(-x + c_1)$$

7.11 problem 15

Internal problem ID [12696]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 15.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$xy(1 - y) - 2y' = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 16

```
dsolve(x*y(x)*(1-y(x))-2*diff(y(x),x)=0,y(x), singsol=all)
```

$$y(x) = \frac{1}{1 + e^{-\frac{x^2}{4}} c_1}$$

✓ Solution by Mathematica

Time used: 0.392 (sec). Leaf size: 41

```
DSolve[x*y[x]*(1-y[x])-2*y'[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$\begin{aligned}y(x) &\rightarrow \frac{e^{\frac{x^2}{4}}}{e^{\frac{x^2}{4}} + e^{c_1}} \\y(x) &\rightarrow 0 \\y(x) &\rightarrow 1\end{aligned}$$

7.12 problem 16

Internal problem ID [12697]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 16.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$x(1 - y^3) - 3y'y^2 = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 66

```
dsolve(x*(1-y(x)^3)-3*y(x)^2*diff(y(x),x)=0,y(x), singsol=all)
```

$$y(x) = \left(e^{-\frac{x^2}{2}} c_1 + 1\right)^{\frac{1}{3}}$$
$$y(x) = -\frac{\left(e^{-\frac{x^2}{2}} c_1 + 1\right)^{\frac{1}{3}} (1 + i\sqrt{3})}{2}$$
$$y(x) = \frac{\left(e^{-\frac{x^2}{2}} c_1 + 1\right)^{\frac{1}{3}} (i\sqrt{3} - 1)}{2}$$

✓ Solution by Mathematica

Time used: 2.121 (sec). Leaf size: 111

```
DSolve[x*(1-y[x]^3)-3*y[x]^2*y'[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \sqrt[3]{1 + e^{-\frac{x^2}{2} + 3c_1}}$$

$$y(x) \rightarrow -\sqrt[3]{-1} \sqrt[3]{1 + e^{-\frac{x^2}{2} + 3c_1}}$$

$$y(x) \rightarrow (-1)^{2/3} \sqrt[3]{1 + e^{-\frac{x^2}{2} + 3c_1}}$$

$$y(x) \rightarrow 1$$

$$y(x) \rightarrow -\sqrt[3]{-1}$$

$$y(x) \rightarrow (-1)^{2/3}$$

7.13 problem 17

Internal problem ID [12698]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.3.3, page 71

Problem number: 17.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$(2x - 1)y + x(x + 1)y' = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 12

```
dsolve(y(x)*(2*x-1)+x*(x+1)*diff(y(x),x)=0,y(x), singsol=all)
```

$$y(x) = \frac{c_1 x}{(1 + x)^3}$$

✓ Solution by Mathematica

Time used: 0.055 (sec). Leaf size: 19

```
DSolve[y[x]*(2*x-1)+x*(x+1)*y'[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{c_1 x}{(x + 1)^3}$$
$$y(x) \rightarrow 0$$

8 Chapter 2. The Initial Value Problem. Exercises

2.4.4, page 115

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8.1 problem 1

Internal problem ID [12699]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 1.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = \frac{1}{x-1}$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 14

```
dsolve([diff(y(x),x)=1/(x-1),y(0) = 1],y(x), singsol=all)
```

$$y(x) = \ln(-1 + x) + 1 - i\pi$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 16

```
DSolve[{y'[x]==1/(x-1)},{y[0]==1}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \log(x - 1) - i\pi + 1$$

8.2 problem 2

Internal problem ID [12700]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 2.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_linear, 'class A']]`

$$y' - y = x$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 11

```
dsolve([diff(y(x),x)=y(x)+x,y(0) = 0],y(x), singsol=all)
```

$$y(x) = -x - 1 + e^x$$

✓ Solution by Mathematica

Time used: 0.042 (sec). Leaf size: 13

```
DSolve[{y'[x]==y[x]+x,{y[0]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -x + e^x - 1$$

8.3 problem 3 (a)

Internal problem ID [12701]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 3 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - \frac{y}{x} = 0$$

With initial conditions

$$[y(-1) = 1]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 7

```
dsolve([diff(y(x),x)=y(x)/x,y(-1) = 1],y(x), singsol=all)
```

$$y(x) = -x$$

✓ Solution by Mathematica

Time used: 0.036 (sec). Leaf size: 8

```
DSolve[{y'[x]==y[x]/x,{y[-1]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -x$$

8.4 problem 3 (b)

Internal problem ID [12702]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 3 (b).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - \frac{y}{x} = 0$$

With initial conditions

$$[y(-1) = -1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 5

```
dsolve([diff(y(x),x)=y(x)/x,y(-1) = -1],y(x), singsol=all)
```

$$y(x) = x$$

✓ Solution by Mathematica

Time used: 0.035 (sec). Leaf size: 6

```
DSolve[{y'[x]==y[x]/x,{y[-1]==-1}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow x$$

8.5 problem 4 (a)

Internal problem ID [12703]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 4 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - \frac{y}{-x^2 + 1} = \sqrt{x}$$

With initial conditions

$$\left[y\left(\frac{1}{2}\right) = 1 \right]$$

✓ Solution by Maple

Time used: 1.969 (sec). Leaf size: 141

```
dsolve([diff(y(x),x)=y(x)/(1-x^2)+sqrt(x),y(1/2) = 1],y(x), singsol=all)
```

$$y(x) = \frac{\left(12i\sqrt{2} \operatorname{EllipticE}\left(\frac{\sqrt{6}}{2}, \frac{\sqrt{2}}{2}\right) - \sqrt{3}\sqrt{2} - 8i \operatorname{EllipticF}\left(\frac{\sqrt{3}}{2}, \sqrt{2}\right) + 2\sqrt{3}\right)(1+x)}{6\sqrt{-x^2+1}} + \frac{-2\sqrt{1+x}\sqrt{2-2x}\sqrt{-x} \operatorname{EllipticF}\left(\sqrt{1+x}, \frac{\sqrt{2}}{2}\right) + 6\sqrt{1+x}\sqrt{2-2x}\sqrt{-x} \operatorname{EllipticE}\left(\sqrt{1+x}, \frac{\sqrt{2}}{2}\right)}{\sqrt{x}(3x-3)}$$

✓ Solution by Mathematica

Time used: 1.562 (sec). Leaf size: 215

```
DSolve[{y'[x]==y[x]/(1-x^2)+Sqrt[x],{y[1/2]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{4\sqrt{1-x^2}x^2 \operatorname{Hypergeometric2F1}\left(\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, x^2\right) - 4\sqrt{1-x^2}x \operatorname{Hypergeometric2F1}\left(\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, x^2\right) - \sqrt{2} \operatorname{Hypergeometric2F1}\left(\frac{1}{2}, \frac{1}{2}, \frac{3}{2}, x^2\right)}{6\sqrt{-x^2+1}}$$

8.6 problem 4 (b)

Internal problem ID [12704]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 4 (b).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - \frac{y}{-x^2 + 1} = \sqrt{x}$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 98

```
dsolve(diff(y(x),x)=y(x)/(1-x^2)+sqrt(x),y(x), singsol=all)
```

$$y(x) = \frac{(1+x)c_1}{\sqrt{-x^2+1}} + \frac{-2\sqrt{1+x}\sqrt{2-2x}\sqrt{-x} \operatorname{EllipticF}\left(\sqrt{1+x}, \frac{\sqrt{2}}{2}\right) + 6\sqrt{1+x}\sqrt{2-2x}\sqrt{-x} \operatorname{EllipticE}\left(\sqrt{1+x}, \frac{\sqrt{2}}{2}\right)}{\sqrt{x}(3x-3)}$$

✓ Solution by Mathematica

Time used: 1.157 (sec). Leaf size: 100

```
DSolve[y'[x]==y[x]/(1-x^2)+Sqrt[x],y[x],x,IncludeSingularSolutions->True]
```

$$y(x) \rightarrow \frac{2x\left(-\sqrt{1-x^2} \operatorname{Hypergeometric2F1}\left(\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, x^2\right) + \sqrt{1-x^2} \operatorname{Hypergeometric2F1}\left(\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, x^2\right) + x^2 - 1\right)}{\sqrt{-((x-1)x)}} + 3c_1\sqrt{x+1}$$

$$3\sqrt{1-x}$$

8.7 problem 4 (c)

Internal problem ID [12705]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 4 (c).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [linear]

$$y' - \frac{y}{-x^2 + 1} = \sqrt{x}$$

With initial conditions

$$[y(2) = 1]$$

✓ Solution by Maple

Time used: 0.922 (sec). Leaf size: 136

```
dsolve([diff(y(x),x)=y(x)/(1-x^2)+sqrt(x),y(2) = 1],y(x), singsol=all)
```

$$y(x) = -\frac{i(1+x) \left(-1 + \frac{2(\sqrt{3} \operatorname{EllipticF}(\sqrt{3}, \frac{\sqrt{2}}{2}) - 3\sqrt{3} \operatorname{EllipticE}(\sqrt{3}, \frac{\sqrt{2}}{2}) + 3)\sqrt{2}}{3} \right) \sqrt{3}}{3\sqrt{-x^2 + 1}} + \frac{-2\sqrt{1+x}\sqrt{2-2x}\sqrt{-x} \operatorname{EllipticF}\left(\sqrt{1+x}, \frac{\sqrt{2}}{2}\right) + 6\sqrt{1+x}\sqrt{2-2x}\sqrt{-x} \operatorname{EllipticE}\left(\sqrt{1+x}, \frac{\sqrt{2}}{2}\right)}{\sqrt{x}(3x-3)}$$

✓ Solution by Mathematica

Time used: 0.121 (sec). Leaf size: 215

```
DSolve[{y'[x]==y[x]/(1-x^2)+Sqrt[x],{y[2]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{2\sqrt{1-x^2}x^2 \operatorname{Hypergeometric2F1}\left(\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, x^2\right) - 2\sqrt{1-x^2}x \operatorname{Hypergeometric2F1}\left(\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, x^2\right) - 4\sqrt{2} \operatorname{Hyp}}{\dots}$$

8.8 problem 5 (a)

Internal problem ID [12706]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 5 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y^2 = 0$$

With initial conditions

$$[y(-1) = 1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 9

```
dsolve([diff(y(x),x)=y(x)^2,y(-1) = 1],y(x), singsol=all)
```

$$y(x) = -\frac{1}{x}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 10

```
DSolve[{y'[x]==y[x]^2,{y[-1]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{1}{x}$$

8.9 problem 5 (b)

Internal problem ID [12707]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 5 (b).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y^2 = 0$$

With initial conditions

$$[y(-1) = 0]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 5

```
dsolve([diff(y(x),x)=y(x)^2,y(-1) = 0],y(x), singsol=all)
```

$$y(x) = 0$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 6

```
DSolve[{y'[x]==y[x]^2,{y[-1]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 0$$

8.10 problem 5 (c)

Internal problem ID [12708]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 5 (c).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y^2 = 0$$

With initial conditions

$$\left[y(1) = \frac{1}{2} \right]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 11

```
dsolve([diff(y(x),x)=y(x)^2,y(1) = 1/2],y(x), singsol=all)
```

$$y(x) = -\frac{1}{-3+x}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 12

```
DSolve[{y'[x]==y[x]^2,{y[1]==1/2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{3-x}$$

8.11 problem 6 (a)

Internal problem ID [12709]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 6 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y^3 = 0$$

With initial conditions

$$[y(-1) = 1]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 11

```
dsolve([diff(y(x),x)=y(x)^3,y(-1) = 1],y(x), singsol=all)
```

$$y(x) = \frac{1}{\sqrt{-2x - 1}}$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 14

```
DSolve[{y'[x]==y[x]^3,{y[-1]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{\sqrt{-2x - 1}}$$

8.12 problem 6 (b)

Internal problem ID [12710]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 6 (b).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y^3 = 0$$

With initial conditions

$$[y(-1) = 0]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 5

```
dsolve([diff(y(x),x)=y(x)^3,y(-1) = 0],y(x), singsol=all)
```

$$y(x) = 0$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 6

```
DSolve[{y'[x]==y[x]^3,{y[-1]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 0$$

8.13 problem 6 (c)

Internal problem ID [12711]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 6 (c).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y^3 = 0$$

With initial conditions

$$[y(-1) = -1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 13

```
dsolve([diff(y(x),x)=y(x)^3,y(-1) = -1],y(x), singsol=all)
```

$$y(x) = -\frac{1}{\sqrt{-2x-1}}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 16

```
DSolve[{y'[x]==y[x]^3,{y[-1]==-1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{1}{\sqrt{-2x-1}}$$

8.14 problem 7 (a)

Internal problem ID [12712]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 7 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' + \frac{3x^2}{2y} = 0$$

With initial conditions

$$[y(-1) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 12

```
dsolve([diff(y(x),x)=-3*x^2/(2*y(x)),y(-1) = 1],y(x), singsol=all)
```

$$y(x) = (-x)^{\frac{3}{2}}$$

✓ Solution by Mathematica

Time used: 0.144 (sec). Leaf size: 14

```
DSolve[{y'[x]==-3*x^2/(2*y[x]),{y[-1]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \sqrt{-x^3}$$

8.15 problem 7 (b)

Internal problem ID [12713]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 7 (b).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' + \frac{3x^2}{2y} = 0$$

With initial conditions

$$\left[y(-1) = \frac{1}{2} \right]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 15

```
dsolve([diff(y(x),x)=-3*x^2/(2*y(x)),y(-1) = 1/2],y(x), singsol=all)
```

$$y(x) = \frac{\sqrt{-4x^3 - 3}}{2}$$

✓ Solution by Mathematica

Time used: 0.07 (sec). Leaf size: 20

```
DSolve[{y'[x]==-3*x^2/(2*y[x]),{y[-1]==1/2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{2}\sqrt{-4x^3 - 3}$$

8.16 problem 7 (c)

Internal problem ID [12714]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 7 (c).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' + \frac{3x^2}{2y} = 0$$

With initial conditions

$$[y(-1) = 0]$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 27

```
dsolve([diff(y(x),x)=-3*x^2/(2*y(x)),y(-1) = 0],y(x), singsol=all)
```

$$y(x) = \sqrt{-x^3 - 1}$$
$$y(x) = -\sqrt{-x^3 - 1}$$

✓ Solution by Mathematica

Time used: 0.069 (sec). Leaf size: 33

```
DSolve[{y'[x]==-3*x^2/(2*y[x]),{y[-1]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\sqrt{-x^3 - 1}$$
$$y(x) \rightarrow \sqrt{-x^3 - 1}$$

8.17 problem 7 (d)

Internal problem ID [12715]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 7 (d).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' + \frac{3x^2}{2y} = 0$$

With initial conditions

$$[y(-1) = -1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 11

```
dsolve([diff(y(x),x)=-3*x^2/(2*y(x)),y(-1) = -1],y(x), singsol=all)
```

$$y(x) = -(-x)^{\frac{3}{2}}$$

✓ Solution by Mathematica

Time used: 0.07 (sec). Leaf size: 16

```
DSolve[{y'[x]==-3*x^2/(2*y[x]),{y[-1]==-1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\sqrt{-x^3}$$

8.18 problem 8 (a)

Internal problem ID [12716]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 8 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{\sqrt{y}}{x} = 0$$

With initial conditions

$$[y(-1) = 1]$$

✓ Solution by Maple

Time used: 0.078 (sec). Leaf size: 29

```
dsolve([diff(y(x),x)=sqrt(y(x))/x,y(-1) = 1],y(x), singsol=all)
```

$$y(x) = -\frac{i\pi \ln(x)}{2} - i\pi - \frac{\pi^2}{4} + \frac{\ln(x)^2}{4} + \ln(x) + 1$$

✓ Solution by Mathematica

Time used: 0.235 (sec). Leaf size: 43

```
DSolve[{y'[x]==Sqrt[y[x]]/x,{y[-1]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{1}{4}(i \log(x) + \pi - 2i)^2$$
$$y(x) \rightarrow -\frac{1}{4}(i \log(x) + \pi + 2i)^2$$

8.19 problem 8 (b)

Internal problem ID [12717]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 8 (b).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - \frac{\sqrt{y}}{x} = 0$$

With initial conditions

$$[y(-1) = 0]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 5

```
dsolve([diff(y(x),x)=sqrt(y(x))/x,y(-1) = 0],y(x), singsol=all)
```

$$y(x) = 0$$

✓ Solution by Mathematica

Time used: 0.157 (sec). Leaf size: 24

```
DSolve[{y'[x]==Sqrt[y[x]]/x,{y[-1]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 0$$
$$y(x) \rightarrow -\frac{1}{4}(\pi + i \log(x))^2$$

8.20 problem 8 (c)

Internal problem ID [12718]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 8 (c).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{\sqrt{y}}{x} = 0$$

With initial conditions

$$[y(-1) = -1]$$

✓ Solution by Maple

Time used: 0.093 (sec). Leaf size: 28

```
dsolve([diff(y(x),x)=sqrt(y(x))/x,y(-1) = -1],y(x), singsol=all)
```

$$y(x) = \frac{\ln(x)^2}{4} + \frac{i(2 - \pi) \ln(x)}{2} - \frac{(-2 + \pi)^2}{4}$$

✓ Solution by Mathematica

Time used: 0.151 (sec). Leaf size: 39

```
DSolve[{y'[x]==Sqrt[y[x]]/x,{y[-1]==-1}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{1}{4}(i \log(x) + \pi + 2)^2$$
$$y(x) \rightarrow -\frac{1}{4}(i \log(x) + \pi - 2)^2$$

8.21 problem 8 (d)

Internal problem ID [12719]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 8 (d).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_separable]

$$y' - \frac{\sqrt{y}}{x} = 0$$

With initial conditions

$$[y(1) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 12

```
dsolve([diff(y(x),x)=sqrt(y(x))/x,y(1) = 1],y(x), singsol=all)
```

$$y(x) = \frac{(\ln(x) + 2)^2}{4}$$

✓ Solution by Mathematica

Time used: 0.151 (sec). Leaf size: 29

```
DSolve[{y'[x]==Sqrt[y[x]]/x,{y[1]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{4}(\log(x) - 2)^2$$
$$y(x) \rightarrow \frac{1}{4}(\log(x) + 2)^2$$

8.22 problem 9 (a)

Internal problem ID [12720]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 9 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - 3xy^{\frac{1}{3}} = 0$$

With initial conditions

$$\left[y(-1) = \frac{3}{2} \right]$$

✓ Solution by Maple

Time used: 0.64 (sec). Leaf size: 23

```
dsolve([diff(y(x),x)=3*x*y(x)^(1/3),y(-1) = 3/2],y(x), singsol=all)
```

$$y(x) = \frac{\sqrt{2 \cdot 3^{\frac{2}{3}} 2^{\frac{1}{3}} + 4x^2} - 4 \left(3^{\frac{2}{3}} 2^{\frac{1}{3}} + 2x^2 - 2 \right)}{4}$$

✓ Solution by Mathematica

Time used: 0.374 (sec). Leaf size: 36

```
DSolve[{y'[x]==3*x*y[x]^(1/3),{y[-1]==3/2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{\left(2x^2 + \sqrt[3]{2} 3^{2/3} - 2 \right)^{3/2}}{2\sqrt{2}}$$

8.23 problem 9 (b)

Internal problem ID [12721]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 9 (b).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - 3xy^{\frac{1}{3}} = 0$$

With initial conditions

$$[y(-1) = 1]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 9

```
dsolve([diff(y(x),x)=3*x*y(x)^(1/3),y(-1) = 1],y(x), singsol=all)
```

$$y(x) = -x^3$$

✓ Solution by Mathematica

Time used: 0.214 (sec). Leaf size: 12

```
DSolve[{y'[x]==3*x*y[x]^(1/3)},{y[-1]==1}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow (x^2)^{3/2}$$

8.24 problem 9 (c)

Internal problem ID [12722]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 9 (c).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - 3xy^{\frac{1}{3}} = 0$$

With initial conditions

$$\left[y(-1) = \frac{1}{2} \right]$$

✓ Solution by Maple

Time used: 0.266 (sec). Leaf size: 20

```
dsolve([diff(y(x),x)=3*x*y(x)^(1/3),y(-1) = 1/2],y(x), singsol=all)
```

$$y(x) = \frac{\sqrt{4x^2 + 22^{\frac{1}{3}} - 4} \left(2x^2 + 2^{\frac{1}{3}} - 2 \right)}{4}$$

✓ Solution by Mathematica

Time used: 0.175 (sec). Leaf size: 30

```
DSolve[{y'[x]==3*x*y[x]^(1/3),{y[-1]==1/2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{\left(2x^2 + \sqrt[3]{2} - 2 \right)^{3/2}}{2\sqrt{2}}$$

8.25 problem 9 (d)

Internal problem ID [12723]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 9 (d).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - 3xy^{\frac{1}{3}} = 0$$

With initial conditions

$$[y(-1) = 0]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 5

```
dsolve([diff(y(x),x)=3*x*y(x)^(1/3),y(-1) = 0],y(x), singsol=all)
```

$$y(x) = 0$$

✓ Solution by Mathematica

Time used: 0.159 (sec). Leaf size: 19

```
DSolve[{y'[x]==3*x*y[x]^(1/3),{y[-1]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 0$$

$$y(x) \rightarrow (x^2 - 1)^{3/2}$$

8.26 problem 9 (e)

Internal problem ID [12724]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 9 (e).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - 3xy^{\frac{1}{3}} = 0$$

With initial conditions

$$[y(-1) = -1]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 7

```
dsolve([diff(y(x),x)=3*x*y(x)^(1/3),y(-1) = -1],y(x), singsol=all)
```

$$y(x) = x^3$$

✓ Solution by Mathematica

Time used: 0.175 (sec). Leaf size: 67

```
DSolve[{y'[x]==3*x*y[x]^(1/3),{y[-1]==-1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{(2x^2 - i\sqrt{3} - 3)^{3/2}}{2\sqrt{2}}$$
$$y(x) \rightarrow \frac{(2x^2 + i\sqrt{3} - 3)^{3/2}}{2\sqrt{2}}$$

8.27 problem 10 (a)

Internal problem ID [12725]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 10 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - \sqrt{(y+2)(y-1)} = 0$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 1.031 (sec). Leaf size: 34

```
dsolve([diff(y(x),x)=sqrt((y(x)+2)*(y(x)-1)),y(0) = 0],y(x), singsol=all)
```

$$y(x) = \frac{ie^x\sqrt{2}}{2} - \frac{i\sqrt{2}e^{-x}}{2} + \frac{e^x}{4} - \frac{1}{2} + \frac{e^{-x}}{4}$$

✓ Solution by Mathematica

Time used: 0.053 (sec). Leaf size: 45

```
DSolve[{y'[x]==Sqrt[(y[x]+2)*(y[x]-1)],{y[0]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{4}e^{-x}(e^x - 1) \left((1 + 2i\sqrt{2})e^x - 1 + 2i\sqrt{2} \right)$$

8.28 problem 10 (b)

Internal problem ID [12726]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 10 (b).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - \sqrt{(y+2)(y-1)} = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 5

```
dsolve([diff(y(x),x)=sqrt((y(x)+2)*(y(x)-1)),y(0) = 1],y(x), singsol=all)
```

$$y(x) = 1$$

✓ Solution by Mathematica

Time used: 0.022 (sec). Leaf size: 23

```
DSolve[{y'[x]==Sqrt[(y[x]+2)*(y[x]-1)],{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{4}(3e^{-x} + 3e^x - 2)$$

8.29 problem 10 (c)

Internal problem ID [12727]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 10 (c).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - \sqrt{(y+2)(y-1)} = 0$$

With initial conditions

$$[y(0) = -3]$$

✓ Solution by Maple

Time used: 0.234 (sec). Leaf size: 16

```
dsolve([diff(y(x),x)=sqrt((y(x)+2)*(y(x)-1)),y(0) = -3],y(x), singsol=all)
```

$$y(x) = -\frac{e^x}{4} - \frac{1}{2} - \frac{9e^{-x}}{4}$$

✓ Solution by Mathematica

Time used: 0.021 (sec). Leaf size: 23

```
DSolve[{y'[x]==Sqrt[(y[x]+2)*(y[x]-1)],{y[0]==-3}},y[x],x,IncludeSingularSolutions -> True
```

$$y(x) \rightarrow \frac{1}{4}(-9e^{-x} - e^x - 2)$$

8.30 problem 11 (a)

Internal problem ID [12728]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 11 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_homogeneous, 'class A', _rational, [_Abel, '2nd type', 'cl`

$$y' - \frac{y}{y-x} = 0$$

With initial conditions

$$[y(1) = 2]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 7

```
dsolve([diff(y(x),x)=y(x)/(y(x)-x),y(1) = 2],y(x), singsol=all)
```

$$y(x) = 2x$$

✓ Solution by Mathematica

Time used: 0.838 (sec). Leaf size: 14

```
DSolve[{y'[x]==y[x]/(y[x]-x),{y[1]==2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \sqrt{x^2} + x$$

8.31 problem 11 (b)

Internal problem ID [12729]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 11 (b).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_homogeneous, 'class A', _rational, [_Abel, '2nd type', 'cl`

$$y' - \frac{y}{y-x} = 0$$

With initial conditions

$$[y(1) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 27

```
dsolve([diff(y(x),x)=y(x)/(y(x)-x),y(1) = 1],y(x), singsol=all)
```

$$y(x) = x - \sqrt{x^2 - 1}$$

$$y(x) = x + \sqrt{x^2 - 1}$$

✓ Solution by Mathematica

Time used: 0.129 (sec). Leaf size: 33

```
DSolve[{y'[x]==y[x]/(y[x]-x)},{y[1]==1}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow x - \sqrt{x^2 - 1}$$

$$y(x) \rightarrow \sqrt{x^2 - 1} + x$$

8.32 problem 11 (c)

Internal problem ID [12730]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 11 (c).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_homogeneous, 'class A', _rational, [_Abel, '2nd type', 'cl`

$$y' - \frac{y}{y-x} = 0$$

With initial conditions

$$[y(1) = 0]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 5

```
dsolve([diff(y(x),x)=y(x)/(y(x)-x),y(1) = 0],y(x), singsol=all)
```

$$y(x) = 0$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 6

```
DSolve[{y'[x]==y[x]/(y[x]-x),{y[1]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 0$$

8.33 problem 11 (d)

Internal problem ID [12731]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 11 (d).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_homogeneous, 'class A', _rational, [_Abel, '2nd type', 'cl`

$$y' - \frac{y}{y-x} = 0$$

With initial conditions

$$[y(1) = -1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 15

```
dsolve([diff(y(x),x)=y(x)/(y(x)-x),y(1) = -1],y(x), singsol=all)
```

$$y(x) = x - \sqrt{x^2 + 3}$$

✓ Solution by Mathematica

Time used: 0.127 (sec). Leaf size: 18

```
DSolve[{y'[x]==y[x]/(y[x]-x)},{y[1]==-1}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow x - \sqrt{x^2 + 3}$$

8.34 problem 12 (a)

Internal problem ID [12732]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 12 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_homogeneous, 'class A', _rational, _dAlembert]`

$$y' - \frac{xy}{x^2 + y^2} = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 1.75 (sec). Leaf size: 11

```
dsolve([diff(y(x),x)=x*y(x)/(x^2+y(x)^2),y(0) = 1],y(x), singsol=all)
```

$$y(x) = \sqrt{\frac{x^2}{\text{LambertW}(x^2)}}$$

✓ Solution by Mathematica

Time used: 10.851 (sec). Leaf size: 15

```
DSolve[{y'[x]==x*y[x]/(x^2+y[x]^2),{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{x}{\sqrt{W(x^2)}}$$

8.35 problem 12 (b)

Internal problem ID [12733]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 12 (b).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_homogeneous, 'class A', _rational, _dAlembert]`

$$y' - \frac{xy}{x^2 + y^2} = 0$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 5

```
dsolve([diff(y(x),x)=x*y(x)/(x^2+y(x)^2),y(0) = 0],y(x), singsol=all)
```

$$y(x) = 0$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 6

```
DSolve[{y'[x]==x*y[x]/(x^2+y[x]^2),{y[0]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 0$$

8.36 problem 12 (c)

Internal problem ID [12734]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 12 (c).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_homogeneous, 'class A', _rational, _dAlembert]`

$$y' - \frac{xy}{x^2 + y^2} = 0$$

With initial conditions

$$[y(0) = -1]$$

✓ Solution by Maple

Time used: 0.875 (sec). Leaf size: 13

```
dsolve([diff(y(x),x)=x*y(x)/(x^2+y(x)^2),y(0) = -1],y(x), singsol=all)
```

$$y(x) = -\sqrt{\frac{x^2}{\text{LambertW}(x^2)}}$$

✓ Solution by Mathematica

Time used: 0.443 (sec). Leaf size: 16

```
DSolve[{y'[x]==x*y[x]/(x^2+y[x]^2),{y[0]==-1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{x}{\sqrt{W(x^2)}}$$

8.37 problem 13 (a)

Internal problem ID [12735]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 13 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - x\sqrt{1-y^2} = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 5

```
dsolve([diff(y(x),x)=x*sqrt(1-y(x)^2),y(0) = 1],y(x), singsol=all)
```

$$y(x) = 1$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 6

```
DSolve[{y'[x]==x*Sqrt[1-y[x]^2],{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 1$$

8.38 problem 13 (b)

Internal problem ID [12736]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 13 (b).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - x\sqrt{1-y^2} = 0$$

With initial conditions

$$\left[y(0) = \frac{9}{10} \right]$$

✓ Solution by Maple

Time used: 0.062 (sec). Leaf size: 13

```
dsolve([diff(y(x),x)=x*sqrt(1-y(x)^2),y(0) = 9/10],y(x), singsol=all)
```

$$y(x) = \sin\left(\frac{x^2}{2} + \arcsin\left(\frac{9}{10}\right)\right)$$

✓ Solution by Mathematica

Time used: 0.368 (sec). Leaf size: 43

```
DSolve[{y'[x]==x*Sqrt[1-y[x]^2],{y[0]==9/10}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \cos\left(\frac{1}{2}\left(4\arctan\left(\frac{1}{\sqrt{19}}\right) + x^2\right)\right)$$
$$y(x) \rightarrow \cos\left(\frac{1}{2}\left(x^2 - 4\arctan\left(\frac{1}{\sqrt{19}}\right)\right)\right)$$

8.39 problem 13 (c)

Internal problem ID [12737]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 13 (c).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - x\sqrt{1-y^2} = 0$$

With initial conditions

$$\left[y(0) = \frac{1}{2} \right]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 14

```
dsolve([diff(y(x),x)=x*sqrt(1-y(x)^2),y(0) = 1/2],y(x), singsol=all)
```

$$y(x) = \sin\left(\frac{x^2}{2} + \frac{\pi}{6}\right)$$

✓ Solution by Mathematica

Time used: 0.215 (sec). Leaf size: 33

```
DSolve[{y'[x]==x*Sqrt[1-y[x]^2},{y[0]==1/2}],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \sin\left(\frac{1}{6}(\pi - 3x^2)\right)$$

$$y(x) \rightarrow \sin\left(\frac{1}{6}(3x^2 + \pi)\right)$$

8.40 problem 13 (d)

Internal problem ID [12738]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 13 (d).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [`_separable`]

$$y' - x\sqrt{1-y^2} = 0$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 10

```
dsolve([diff(y(x),x)=x*sqrt(1-y(x)^2),y(0) = 0],y(x), singsol=all)
```

$$y(x) = \sin\left(\frac{x^2}{2}\right)$$

✓ Solution by Mathematica

Time used: 0.21 (sec). Leaf size: 27

```
DSolve[{y'[x]==x*Sqrt[1-y[x]^2],{y[0]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\sin\left(\frac{x^2}{2}\right)$$

$$y(x) \rightarrow \sin\left(\frac{x^2}{2}\right)$$

8.41 problem 14 (a)

Internal problem ID [12739]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 14 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_1st_order, _with_linear_symmetries], _Clairaut]`

$$y' - \frac{\sqrt{x^2 + 4y}}{2} = -\frac{x}{2}$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.359 (sec). Leaf size: 15

```
dsolve([diff(y(x),x)=(-x+sqrt(x^2+4*y(x)))/2,y(0) = 1],y(x), singsol=all)
```

$$y(x) = 1 - x$$

$$y(x) = 1 + x$$

✓ Solution by Mathematica

Time used: 0.443 (sec). Leaf size: 17

```
DSolve[{y'[x]==(-x+Sqrt[x^2+4*y[x]])/2,{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 1 - x$$

$$y(x) \rightarrow x + 1$$

8.42 problem 14 (b)

Internal problem ID [12740]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 14 (b).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_1st_order, _with_linear_symmetries], _Clairaut]`

$$y' - \frac{\sqrt{x^2 + 4y}}{2} = -\frac{x}{2}$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 13

```
dsolve([diff(y(x),x)=(-x+sqrt(x^2+4*y(x)))/2,y(0) = 0],y(x), singsol=all)
```

$$y(x) = 0$$
$$y(x) = -\frac{x^2}{4}$$

✓ Solution by Mathematica

Time used: 0.287 (sec). Leaf size: 6

```
DSolve[{y'[x]==(-x+Sqrt[x^2+4*y[x]])/2,{y[0]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 0$$

8.43 problem 14 (c)

Internal problem ID [12741]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 14 (c).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_1st_order, _with_linear_symmetries], _Clairaut]`

$$y' - \frac{\sqrt{x^2 + 4y}}{2} = -\frac{x}{2}$$

With initial conditions

$$[y(0) = -1]$$

✓ Solution by Maple

Time used: 0.25 (sec). Leaf size: 19

```
dsolve([diff(y(x),x)=(-x+sqrt(x^2+4*y(x)))/2,y(0) = -1],y(x), singsol=all)
```

$$y(x) = -ix - 1$$

$$y(x) = ix - 1$$

✓ Solution by Mathematica

Time used: 0.293 (sec). Leaf size: 23

```
DSolve[{y'[x]==(-x+Sqrt[x^2+4*y[x]])/2,{y[0]==-1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -1 - ix$$

$$y(x) \rightarrow -1 + ix$$

8.44 problem 14 (d)

Internal problem ID [12742]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 14 (d).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_1st_order, _with_linear_symmetries], _Clairaut]`

$$y' - \frac{\sqrt{x^2 + 4y}}{2} = -\frac{x}{2}$$

With initial conditions

$$\left[y(1) = -\frac{1}{5} \right]$$

✓ Solution by Maple

Time used: 0.969 (sec). Leaf size: 69

```
dsolve([diff(y(x),x)=(-x+sqrt(x^2+4*y(x)))/2,y(1) = -1/5],y(x), singsol=all)
```

$$y(x) = \frac{(-1+x)\sqrt{5}}{10} - \frac{x}{2} + \frac{3}{10}$$

$$y(x) = \frac{(\sqrt{5}-5)(-5+\sqrt{5}+10x)}{100}$$

$$y(x) = -\frac{2^{\frac{1}{3}}(50+20\sqrt{5})^{\frac{1}{3}}\left(2^{\frac{1}{3}}x - \frac{(50+20\sqrt{5})^{\frac{1}{3}}}{5}\right)}{10}$$

✓ Solution by Mathematica

Time used: 0.301 (sec). Leaf size: 51

```
DSolve[{y'[x]==(-x+Sqrt[x^2+4*y[x]])/2,{y[1]==-2/10}},y[x],x,IncludeSingularSolutions -> True
```

$$y(x) \rightarrow \frac{1}{100} (5 + \sqrt{5}) (-10x + \sqrt{5} + 5)$$

$$y(x) \rightarrow \frac{1}{100} (\sqrt{5} - 5) (10x + \sqrt{5} - 5)$$

8.45 problem 14 (e)

Internal problem ID [12743]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 2. The Initial Value Problem. Exercises 2.4.4, page 115

Problem number: 14 (e).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_1st_order, _with_linear_symmetries], _Clairaut]`

$$y' - \frac{\sqrt{x^2 + 4y}}{2} = -\frac{x}{2}$$

With initial conditions

$$\left[y(1) = -\frac{1}{4} \right]$$

✓ Solution by Maple

Time used: 8.516 (sec). Leaf size: 17

```
dsolve([diff(y(x),x)=(-x+sqrt(x^2+4*y(x)))/2,y(1) = -1/4],y(x), singsol=all)
```

$$y(x) = -\frac{x^2}{4}$$
$$y(x) = \frac{1}{4} - \frac{x}{2}$$

✓ Solution by Mathematica

Time used: 0.282 (sec). Leaf size: 14

```
DSolve[{y'[x]==(-x+Sqrt[x^2+4*y[x]])/2,{y[1]==-1/4}},y[x],x,IncludeSingularSolutions -> True
```

$$y(x) \rightarrow \frac{1}{4}(1 - 2x)$$

9 Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

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9.1 problem 1

Internal problem ID [12744]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 1.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$3y'' - 2y' + 4y = x$$

With initial conditions

$$[y(-1) = 2, y'(-1) = 3]$$

✓ Solution by Maple

Time used: 0.266 (sec). Leaf size: 85

```
dsolve([3*dif(y(x),x$2)-2*dif(y(x),x)+4*y(x)=x,y(-1) = 2, D(y)(-1) = 3],y(x), singsol=all)
```

$$y(x) = \frac{\left(\left(49 \sin\left(\frac{\sqrt{11}}{3}\right) \sqrt{11} + 187 \cos\left(\frac{\sqrt{11}}{3}\right) \right) \cos\left(\frac{\sqrt{11}x}{3}\right) + 49 \sin\left(\frac{\sqrt{11}x}{3}\right) \left(\cos\left(\frac{\sqrt{11}}{3}\right) \sqrt{11} - \frac{187 \sin\left(\frac{\sqrt{11}}{3}\right)}{49} \right) \right) e^{\frac{x+1}{3}}}{88} + \frac{x}{4} + \frac{1}{8}$$

✓ Solution by Mathematica

Time used: 0.054 (sec). Leaf size: 67

```
DSolve[{3*y'[x]-2*y'[x]+4*y[x]==x,{y[-1]==2,y'[-1]==3}},y[x],x,IncludeSingularSolutions ->
```

$$y(x) \rightarrow \frac{1}{88} \left(22x + 49\sqrt{11}e^{\frac{x+1}{3}} \sin\left(\frac{1}{3}\sqrt{11}(x+1)\right) + 187e^{\frac{x+1}{3}} \cos\left(\frac{1}{3}\sqrt{11}(x+1)\right) + 11 \right)$$

9.2 problem 2

Internal problem ID [12745]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 2.

ODE order: 3.

ODE degree: 1.

CAS Maple gives this as type `[[_3rd_order, _missing_y]]`

$$xy''' + y'x = 4$$

With initial conditions

$$[y(1) = 0, y'(1) = 1, y''(1) = -1]$$

✓ Solution by Maple

Time used: 0.171 (sec). Leaf size: 49

```
dsolve([x*dif(y(x),x$3)+x*dif(y(x),x)=4,y(1) = 0, D(y)(1) = 1, (D@@2)(y)(1) = -1],y(x), si
```

$$y(x) = (4 \operatorname{Ci}(1) - 4 \operatorname{Ci}(x) + \cos(1) - \sin(1)) \cos(x) \\ + (4 \operatorname{Si}(1) - 4 \operatorname{Si}(x) + \cos(1) + \sin(1)) \sin(x) + 4 \ln(x) - 1$$

✓ Solution by Mathematica

Time used: 0.184 (sec). Leaf size: 85

```
DSolve[{x*y'''[x]+x*y'[x]==4,{y[1]==0,y'[1]==1,y''[1]==-1}},y[x],x,IncludeSingularSolutions
```

$$y(x) \rightarrow -4 \operatorname{CosIntegral}(x) \cos(x) + 4 \operatorname{CosIntegral}(1) \cos(x) - 2 \operatorname{sinc}(1) \cos(2-x) \\ - 6 \operatorname{sinc}(1) \cos(x) + 8 \operatorname{sinc}(1) \cos(1) - 4 \operatorname{Si}(x) \sin(x) + 4 \operatorname{Si}(1) \sin(x) + 4 \log(x) \\ + \sin(1-x) + \sin(3-x) + 3 \sin(x+1) + \cos(1-x) - 1 - 4 \sin(2)$$

9.3 problem 3

Internal problem ID [12746]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 3.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_y]]`

$$x(x-3)y'' + 3y' = x^2$$

With initial conditions

$$[y(1) = 0, y'(1) = 1]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 11

```
dsolve([x*(x-3)*diff(y(x),x$2)+3*diff(y(x),x)=x^2,y(1) = 0, D(y)(1) = 1],y(x), singsol=all)
```

$$y(x) = -\frac{1}{2} + \frac{x^2}{2}$$

✓ Solution by Mathematica

Time used: 0.08 (sec). Leaf size: 14

```
DSolve[{x*(x-3)*y''[x]+3*y'[x]==x^2,{y[1]==0,y'[1]==1}},y[x],x,IncludeSingularSolutions -> T
```

$$y(x) \rightarrow \frac{1}{2}(x^2 - 1)$$

9.4 problem 4

Internal problem ID [12747]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 4.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_y]]`

$$x(x-3)y'' + 3y' = x^2$$

With initial conditions

$$[y(5) = 0, y'(5) = 1]$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 24

```
dsolve([x*(x-3)*diff(y(x),x$2)+3*diff(y(x),x)=x^2,y(5) = 0, D(y)(5) = 1],y(x), singsol=all)
```

$$y(x) = \frac{x^2}{2} - \frac{8x}{5} - \frac{24 \ln(-3+x)}{5} + \frac{24 \ln(2)}{5} - \frac{9}{2}$$

✓ Solution by Mathematica

Time used: 0.069 (sec). Leaf size: 29

```
DSolve[{x*(x-3)*y''[x]+3*y'[x]==x^2,{y[5]==0,y'[5]==1}},y[x],x,IncludeSingularSolutions -> T
```

$$y(x) \rightarrow \frac{1}{10}(5x^2 - 16x - 48 \log(x-3) - 45 + 48 \log(2))$$

9.5 problem 5

Internal problem ID [12748]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 5.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\sqrt{1-x}y'' - 4y = \sin(x)$$

With initial conditions

$$[y(-2) = 3, y'(-2) = -1]$$

✓ Solution by Maple

Time used: 0.843 (sec). Leaf size: 185

```
dsolve([sqrt(1-x)*diff(y(x),x$2)-4*y(x)=sin(x),y(-2) = 3, D(y)(-2) = -1],y(x), singsol=all)
```

$$y(x) = 4 \left((1-x)^{\frac{3}{2}} \right)^{\frac{2}{3}} \left(\int_{-2}^x \frac{\text{BesselI}\left(\frac{2}{3}, \frac{8\sqrt{(-z1+1)^{\frac{3}{2}}}}{3}\right) \sqrt{-z1+1} \sin(-z1)}{\left((-z1+1)^{\frac{3}{2}}\right)^{\frac{1}{3}}} dz1 \right) \sqrt{3} + 6 \cdot 3^{\frac{3}{4}} \text{BesselI}\left(-\frac{1}{3}, \frac{8 \cdot 3^{\frac{3}{4}}}{3}\right)$$

✗ Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

```
DSolve[{Sqrt[1-x]*y'[x]-4*y[x]==Sin[x],{y[-2]==3,y'[-2]==-1}},y[x],x,IncludeSingularSolutio
```

Not solved

9.6 problem 6

Internal problem ID [12749]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 6.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$(x^2 - 4) y'' + y \ln(x) = x e^x$$

With initial conditions

$$[y(1) = 1, y'(1) = 2]$$

X Solution by Maple

```
dsolve([(x^2-4)*diff(y(x),x$2)+ln(x)*y(x)=x*exp(x),y(1) = 1, D(y)(1) = 2],y(x), singsol=all)
```

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

```
DSolve[{(x^2-4)*y'[x]+Log[x]*y[x]==x*Exp[x],{y[1]==1,y'[1]==2}},y[x],x,IncludeSingularSolut
```

Not solved

9.7 problem 7

Internal problem ID [12750]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 7.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

```
dsolve(diff(y(x),x$2)-y(x)=0,y(x), singsol=all)
```

$$y(x) = c_1 e^{-x} + c_2 e^x$$

✓ Solution by Mathematica

Time used: 0.02 (sec). Leaf size: 20

```
DSolve[y''[x]-y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1 e^x + c_2 e^{-x}$$

9.8 problem 8

Internal problem ID [12751]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 8.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' + y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 13

```
dsolve(diff(y(x),x$2)+y(x)=0,y(x), singsol=all)
```

$$y(x) = c_1 \sin(x) + c_2 \cos(x)$$

✓ Solution by Mathematica

Time used: 0.019 (sec). Leaf size: 16

```
DSolve[y''[x]+y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1 \cos(x) + c_2 \sin(x)$$

9.9 problem 9

Internal problem ID [12752]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 9.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type [[_Emden, _Fowler]]

$$y''x^2 + 2y'x - 2y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

```
dsolve(x^2*diff(y(x),x$2)+2*x*diff(y(x),x)-2*y(x)=0,y(x), singsol=all)
```

$$y(x) = \frac{c_1x^3 + c_2}{x^2}$$

✓ Solution by Mathematica

Time used: 0.018 (sec). Leaf size: 16

```
DSolve[x^2*y''[x]+2*x*y'[x]-2*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{c_1}{x^2} + c_2x$$

9.10 problem 10

Internal problem ID [12753]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 10.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x], _Liouville, [_2nd_order, _reducible]`

$$2yy'' - y'^2 = 0$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 17

```
dsolve(2*y(x)*diff(y(x),x$2)-diff(y(x),x)^2=0,y(x), singsol=all)
```

$$y(x) = 0$$
$$y(x) = \frac{(c_1x + c_2)^2}{4}$$

✓ Solution by Mathematica

Time used: 0.028 (sec). Leaf size: 29

```
DSolve[2*y[x]*y'[x]-(y'[x])^2==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{(c_1x + 2c_2)^2}{4c_2}$$
$$y(x) \rightarrow \text{Indeterminate}$$

9.11 problem 13

Internal problem ID [12754]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 13.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - y = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 15

```
dsolve([diff(y(x),x$2)-y(x)=0,y(0) = 0, D(y)(0) = 1],y(x), singsol=all)
```

$$y(x) = -\frac{e^{-x}}{2} + \frac{e^x}{2}$$

✓ Solution by Mathematica

Time used: 0.02 (sec). Leaf size: 21

```
DSolve[{y'[x]-y[x]==0,{y[0]==0,y'[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{2}e^{-x}(e^{2x} - 1)$$

9.12 problem 14

Internal problem ID [12755]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 14.

ODE order: 3.

ODE degree: 1.

CAS Maple gives this as type `[[_3rd_order, _missing_x]]`

$$y''' + y' = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = 0, y''(0) = -1]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 6

```
dsolve([diff(y(x),x$3)+diff(y(x),x)=0,y(0) = 1, D(y)(0) = 0, (D@@2)(y)(0) = -1],y(x), singso
```

$$y(x) = \cos(x)$$

✓ Solution by Mathematica

Time used: 0.031 (sec). Leaf size: 7

```
DSolve[{y'''[x]+y'[x]==0,{y[0]==1,y'[0]==0,y''[0]==-1}},y[x],x,IncludeSingularSolutions -> T
```

$$y(x) \rightarrow \cos(x)$$

9.13 problem 15

Internal problem ID [12756]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 15.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$y''x^2 - y'x + y = 0$$

With initial conditions

$$[y(1) = 2, y'(1) = -1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 12

```
dsolve([x^2*diff(y(x),x$2)-x*diff(y(x),x)+y(x)=0,y(1) = 2, D(y)(1) = -1],y(x), singsol=all)
```

$$y(x) = x(2 - 3 \ln(x))$$

✓ Solution by Mathematica

Time used: 0.028 (sec). Leaf size: 13

```
DSolve[{x^2*y'[x]-x*y'[x]+y[x]==0,{y[1]==2,y'[1]==-1}},y[x],x,IncludeSingularSolutions -> T
```

$$y(x) \rightarrow x(2 - 3 \log(x))$$

9.14 problem 16

Internal problem ID [12757]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 16.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - 4y = 31$$

With initial conditions

$$[y(0) = -9, y'(0) = 6]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 18

```
dsolve([diff(y(x),x$2)-4*y(x)=31,y(0) = -9, D(y)(0) = 6],y(x), singsol=all)
```

$$y(x) = \frac{7e^{2x}}{8} - \frac{17e^{-2x}}{8} - \frac{31}{4}$$

✓ Solution by Mathematica

Time used: 0.023 (sec). Leaf size: 25

```
DSolve[{y'[x]-4*y[x]==31,{y[0]==-9,y'[0]==6}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{8}(-17e^{-2x} + 7e^{2x} - 62)$$

9.15 problem 17

Internal problem ID [12758]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 17.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$y'' + 9y = 27x + 18$$

With initial conditions

$$[y(0) = 23, y'(0) = 21]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 21

```
dsolve([diff(y(x),x$2)+9*y(x)=27*x+18,y(0) = 23, D(y)(0) = 21],y(x), singsol=all)
```

$$y(x) = 6 \sin(3x) + 21 \cos(3x) + 3x + 2$$

✓ Solution by Mathematica

Time used: 0.027 (sec). Leaf size: 22

```
DSolve[{y'[x]+9*y[x]==27*x+18,{y[0]==23,y'[0]==21}},y[x],x,IncludeSingularSolutions -> True
```

$$y(x) \rightarrow 3x + 6 \sin(3x) + 21 \cos(3x) + 2$$

9.16 problem 18

Internal problem ID [12759]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.1, page 186

Problem number: 18.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$y''x^2 + y'x - 4y = -3x - \frac{3}{x}$$

With initial conditions

$$[y(1) = 3, y'(1) = -6]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 19

```
dsolve([x^2*diff(y(x),x$2)+x*diff(y(x),x)-4*y(x)=-3*x-3/x,y(1) = 3, D(y)(1) = -6],y(x),sing
```

$$y(x) = \frac{-x^4 + x^3 + x + 2}{x^2}$$

✓ Solution by Mathematica

Time used: 0.03 (sec). Leaf size: 20

```
DSolve[{x^2*y''[x]+x*y'[x]-4*y[x]==-3*x-3/x,{y[1]==3,y'[1]==-6}},y[x],x,IncludeSingularSolut
```

$$y(x) \rightarrow \frac{-x^4 + x^3 + x + 2}{x^2}$$

10 Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

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10.1 problem 1

Internal problem ID [12760]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 1.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$4y'' + 4y' - 3y = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 17

```
dsolve(4*diff(y(x),x$2)+4*diff(y(x),x)-3*y(x)=0,y(x), singsol=all)
```

$$y(x) = (e^{2x}c_1 + c_2) e^{-\frac{3x}{2}}$$

✓ Solution by Mathematica

Time used: 0.023 (sec). Leaf size: 24

```
DSolve[4*y'[x]+4*y'[x]-3*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{-3x/2}(c_2e^{2x} + c_1)$$

10.2 problem 2

Internal problem ID [12761]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 2.

ODE order: 3.

ODE degree: 1.

CAS Maple gives this as type `[[_3rd_order, _missing_x]]`

$$y''' - 4y'' + 6y' - 4y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 23

```
dsolve(diff(y(x),x$3)-4*diff(y(x),x$2)+6*diff(y(x),x)-4*y(x)=0,y(x), singsol=all)
```

$$y(x) = e^{2x}c_1 + c_2e^x \sin(x) + c_3 \cos(x) e^x$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 26

```
DSolve[y'''[x]-4*y''[x]+6*y'[x]-4*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^x(c_3e^x + c_2 \cos(x) + c_1 \sin(x))$$

10.3 problem 3

Internal problem ID [12762]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 3.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_x]]`

$$y'''' - 16y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 29

```
dsolve(diff(y(x),x$4)-16*y(x)=0,y(x), singsol=all)
```

$$y(x) = e^{2x}c_1 + e^{-2x}c_2 + c_3 \sin(2x) + c_4 \cos(2x)$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 36

```
DSolve[y''''[x]-16*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1 e^{2x} + c_3 e^{-2x} + c_2 \cos(2x) + c_4 \sin(2x)$$

10.4 problem 4

Internal problem ID [12763]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 4.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_x]]`

$$y'''' + 16y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 65

```
dsolve(diff(y(x),x$4)+16*y(x)=0,y(x), singsol=all)
```

$$y(x) = -c_1 e^{-x\sqrt{2}} \sin(x\sqrt{2}) - c_2 e^{x\sqrt{2}} \sin(x\sqrt{2}) + c_3 e^{-x\sqrt{2}} \cos(x\sqrt{2}) + c_4 e^{x\sqrt{2}} \cos(x\sqrt{2})$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 67

```
DSolve[y''''[x]+16*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{-\sqrt{2}x} \left((c_1 e^{2\sqrt{2}x} + c_2) \cos(\sqrt{2}x) + (c_4 e^{2\sqrt{2}x} + c_3) \sin(\sqrt{2}x) \right)$$

10.5 problem 5

Internal problem ID [12764]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 5.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_x]]`

$$y'''' - 4y'''' + 8y'' - 8y' + 4y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 24

```
dsolve(diff(y(x),x$4)-4*diff(y(x),x$3)+8*diff(y(x),x$2)-8*diff(y(x),x)+4*y(x)=0,y(x), singso
```

$$y(x) = ((c_4x + c_2) \cos(x) + \sin(x) (c_3x + c_1)) e^x$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 30

```
DSolve[y''''[x]-4*y''''[x]+8*y''[x]-8*y'[x]+4*y[x]==0,y[x],x,IncludeSingularSolutions -> True
```

$$y(x) \rightarrow e^x((c_4x + c_3) \cos(x) + (c_2x + c_1) \sin(x))$$

10.6 problem 6

Internal problem ID [12765]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 6.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_x]]`

$$y'''' - 8y' = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 36

```
dsolve(diff(y(x),x$4)-8*diff(y(x),x)=0,y(x), singsol=all)
```

$$y(x) = c_1 + c_2 e^{2x} + c_3 e^{-x} \sin(\sqrt{3}x) + c_4 e^{-x} \cos(\sqrt{3}x)$$

✓ Solution by Mathematica

Time used: 0.658 (sec). Leaf size: 70

```
DSolve[y''''[x]-8*y'[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{4} e^{-x} \left(2c_1 e^{3x} - (c_2 + \sqrt{3}c_3) \cos(\sqrt{3}x) + (\sqrt{3}c_2 - c_3) \sin(\sqrt{3}x) \right) + c_4$$

10.7 problem 7

Internal problem ID [12766]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 7.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_x]]`

$$36y'''' - 12y''' - 11y'' + 2y' + y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 24

```
dsolve(36*diff(y(x),x$4)-12*diff(y(x),x$3)-11*diff(y(x),x$2)+2*diff(y(x),x)+y(x)=0,y(x), sin
```

$$y(x) = \left((c_4x + c_3) e^{\frac{5x}{6}} + c_2x + c_1 \right) e^{-\frac{x}{3}}$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 41

```
DSolve[36*y''''[x]-12*y'''[x]-11*y''[x]+2*y'[x]+y[x]==0,y[x],x,IncludeSingularSolutions -> T
```

$$y(x) \rightarrow e^{-x/3} \left(c_3 e^{5x/6} + x(c_4 e^{5x/6} + c_2) + c_1 \right)$$

10.8 problem 8

Internal problem ID [12767]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 8.

ODE order: 5.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_x]]`

$$y^{(5)} - 3y'''' + 3y''' - 3y'' + 2y' = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 24

```
dsolve(diff(y(x),x$5)-3*diff(y(x),x$4)+3*diff(y(x),x$3)-3*diff(y(x),x$2)+2*diff(y(x),x)=0,y(x)
```

$$y(x) = c_1 + c_2 e^x + c_3 e^{2x} + c_4 \sin(x) + c_5 \cos(x)$$

✓ Solution by Mathematica

Time used: 0.043 (sec). Leaf size: 36

```
DSolve[y'''''[x]-3*y''''[x]+3*y'''[x]-3*y''[x]+2*y'[x]==0,y[x],x,IncludeSingularSolutions ->
```

$$y(x) \rightarrow c_3 e^x + \frac{1}{2} c_4 e^{2x} - c_2 \cos(x) + c_1 \sin(x) + c_5$$

10.9 problem 9

Internal problem ID [12768]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 9.

ODE order: 5.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_x]]`

$$y^{(5)} - y'''' + y''' + 35y'' + 16y' - 52y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 40

```
dsolve(diff(y(x),x$5)-diff(y(x),x$4)+diff(y(x),x$3)+35*diff(y(x),x$2)+16*diff(y(x),x)-52*y(x),x))
```

$$y(x) = (c_4 e^{4x} \sin(3x) + c_5 e^{4x} \cos(3x) + c_1 e^{3x} + c_3 x + c_2) e^{-2x}$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 50

```
DSolve[y'''''[x]-y''''[x]+y'''[x]+35*y''[x]+16*y'[x]-52*y[x]==0,y[x],x,IncludeSingularSolutions->True]
```

$$y(x) \rightarrow e^{-2x} (c_4 x + c_5 e^{3x} + c_2 e^{4x} \cos(3x) + c_1 e^{4x} \sin(3x) + c_3)$$

10.10 problem 10

Internal problem ID [12769]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 10.

ODE order: 8.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_x]]`

$$y^{(8)} + 8y'''' + 16y = 0$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 47

```
dsolve(diff(y(x),x$8)+8*diff(y(x),x$4)+16*y(x)=0,y(x), singsol=all)
```

$$y(x) = ((c_4x + c_2) \cos(x) + \sin(x) (c_3x + c_1)) e^{-x} + e^x((c_8x + c_6) \cos(x) + \sin(x) (c_7x + c_5))$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 66

```
DSolve[D[y[x] ,{x,8}]+8*y''''[x]+16*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{-x}((c_4x + c_7e^{2x} + c_8e^{2x}x + c_3) \cos(x) + (c_2x + c_5e^{2x} + c_6e^{2x}x + c_1) \sin(x))$$

10.11 problem 11

Internal problem ID [12770]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 11.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' + \alpha y = 0$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 21

```
dsolve(diff(y(x),x$2)+alpha*y(x)=0,y(x), singsol=all)
```

$$y(x) = c_1 \sin(\sqrt{\alpha} x) + c_2 \cos(\sqrt{\alpha} x)$$

✓ Solution by Mathematica

Time used: 0.025 (sec). Leaf size: 28

```
DSolve[y''[x]+a*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1 \cos(\sqrt{ax}) + c_2 \sin(\sqrt{ax})$$

10.12 problem 17

Internal problem ID [12771]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 17.

ODE order: 3.

ODE degree: 1.

CAS Maple gives this as type `[[_3rd_order, _missing_x]]`

$$y''' + (-3 - 4i)y'' + (-4 + 12i)y' + 12y = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 22

```
dsolve(diff(y(x),x$3)-(3+4*I)*diff(y(x),x$2)-(4-12*I)*diff(y(x),x)+12*y(x)=0,y(x), singsol=a
```

$$y(x) = (c_3x + c_2)e^{2ix} + c_1e^{3x}$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 29

```
DSolve[y'''[x]-(3+4*I)*y''[x]-(4-12*I)*y'[x]+12*y[x]==0,y[x],x,IncludeSingularSolutions -> T
```

$$y(x) \rightarrow e^{2ix}(c_2x + c_1) + c_3e^{3x}$$

10.13 problem 18

Internal problem ID [12772]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 18.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_x]]`

$$y'''' + (-3 - i)y''' + (4 + 3i)y'' = 0$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 25

```
dsolve(diff(y(x),x$4)-(3+I)*diff(y(x),x$3)+(4+3*I)*diff(y(x),x$2)=0,y(x), singsol=all)
```

$$y(x) = c_1 e^{(1+2i)x} + c_2 e^{(2-i)x} + c_3 + c_4 x$$

✓ Solution by Mathematica

Time used: 0.156 (sec). Leaf size: 46

```
DSolve[y''''[x]-(3+I)*y'''[x]+(4+3*I)*y''[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \left(-\frac{3}{25} - \frac{4i}{25}\right) c_1 e^{(1+2i)x} + \left(\frac{3}{25} + \frac{4i}{25}\right) c_2 e^{(2-i)x} + c_4 x + c_3$$

10.14 problem 19

Internal problem ID [12773]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.3, page 210

Problem number: 19.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - iy = 0$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 9

```
dsolve([diff(y(x),x)-I*y(x)=0,y(0) = 1],y(x), singsol=all)
```

$$y(x) = e^{ix}$$

✓ Solution by Mathematica

Time used: 0.039 (sec). Leaf size: 12

```
DSolve[{y'[x]-I*y[x]==0,{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{ix}$$

11 Chapter 4. N-th Order Linear Differential Equations. Exercises 4.4, page 218

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11.1 problem 1

Internal problem ID [12774]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.4, page 218

Problem number: 1.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _linear, _nonhomogeneous]]`

$$y'''' - 6y''' + 13y'' - 12y' + 4y = 2e^x - 4e^{2x}$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 37

```
dsolve(diff(y(x),x$4)-6*diff(y(x),x$3)+13*diff(y(x),x$2)-12*diff(y(x),x)+4*y(x)=2*exp(x)-4*exp(2*x),y(x))
```

$$y(x) = (-2x^2 + (c_4 + 8)x + c_2 - 12)e^{2x} + (x^2 + (c_3 + 4)x + c_1 + 6)e^x$$

✓ Solution by Mathematica

Time used: 0.187 (sec). Leaf size: 41

```
DSolve[y''''[x]-6*y'''[x]+13*y''[x]-12*y'[x]+4*y[x]==2*Exp[x]-4*Exp[2*x],y[x],x,IncludeSingularSolutions->True]
```

$$y(x) \rightarrow e^x(x^2 + e^x(-2x^2 + (8 + c_4)x - 12 + c_3) + (4 + c_2)x + 6 + c_1)$$

11.2 problem 2

Internal problem ID [12775]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.4, page 218

Problem number: 2.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_y]]`

$$y'''' + 4y'' = 24x^2 - 6x + 14 + 32 \cos(2x)$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 48

```
dsolve(diff(y(x),x$4)+4*diff(y(x),x$2)=24*x^2-6*x+14+32*cos(2*x),y(x), singsol=all)
```

$$y(x) = \frac{(-c_1 - 10) \cos(2x)}{4} + \frac{(-8x - c_2) \sin(2x)}{4} + \frac{x^4}{2} - \frac{x^3}{4} + \frac{x^2}{4} + c_3x + c_4$$

✓ Solution by Mathematica

Time used: 1.052 (sec). Leaf size: 54

```
DSolve[y''''[x]+4*y''[x]==24*x^2-6*x+14+32*Cos[2*x],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{4}(2x^4 - x^3 + x^2 + 4c_4x - (12 + c_1) \cos(2x) - (8x + c_2) \sin(2x) + 4c_3)$$

11.3 problem 3

Internal problem ID [12776]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.4, page 218

Problem number: 3.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _linear, _nonhomogeneous]]`

$$y'''' + 2y'' + y = 3 + \cos(2x)$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 28

```
dsolve(diff(y(x),x$4)+2*diff(y(x),x$2)+y(x)=3+cos(2*x),y(x), singsol=all)
```

$$y(x) = 3 + \frac{\cos(2x)}{9} + (c_4x + c_1) \cos(x) + (c_3x + c_2) \sin(x)$$

✓ Solution by Mathematica

Time used: 0.199 (sec). Leaf size: 36

```
DSolve[y''''[x]+2*y''[x]+y[x]==3+Cos[2*x],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{9} \cos(2x) + (c_2x + c_1) \cos(x) + c_3 \sin(x) + c_4x \sin(x) + 3$$

11.4 problem 4

Internal problem ID [12777]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.4, page 218

Problem number: 4.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_y]]`

$$y'''' - 3y''' + 3y'' - y' = 6x - 20 - 120x^2e^x$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 56

```
dsolve(diff(y(x),x$4)-3*diff(y(x),x$3)+3*diff(y(x),x$2)-diff(y(x),x)=6*x-20-120*x^2*exp(x),y
```

$$y(x) = (-2x^5 + 10x^4 - 40x^3 + (c_3 + 120)x^2 + (c_2 - 2c_3 - 240)x + c_1 - c_2 + 2c_3 + 240)e^x - 3x^2 + 2x + c_4$$

✓ Solution by Mathematica

Time used: 0.569 (sec). Leaf size: 65

```
DSolve[y''''[x]-3*y'''[x]+3*y''[x]-y'[x]==6*x-20-120*x^2*Exp[x],y[x],x,IncludeSingularSoluti
```

$$y(x) \rightarrow -3x^2 + e^x(-2x^5 + 10x^4 - 40x^3 + (120 + c_3)x^2 + (-240 + c_2 - 2c_3)x + 240 + c_1 - c_2 + 2c_3) + 2x + c_4$$

11.5 problem 5

Internal problem ID [12778]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.4, page 218

Problem number: 5.

ODE order: 3.

ODE degree: 1.

CAS Maple gives this as type `[[_3rd_order, _linear, _nonhomogeneous]]`

$$y''' - 6y'' + 21y' - 26y = 36e^{2x} \sin(3x)$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 41

```
dsolve(diff(y(x),x$3)-6*diff(y(x),x$2)+21*diff(y(x),x)-26*y(x)=36*exp(2*x)*sin(3*x),y(x), si
```

$$y(x) = \frac{e^{2x}(3c_3 \sin(3x) - 6x \sin(3x) + 3c_2 \cos(3x) - 2 \cos(3x) + 3c_1)}{3}$$

✓ Solution by Mathematica

Time used: 0.103 (sec). Leaf size: 34

```
DSolve[y'''[x]-6*y''[x]+21*y'[x]-26*y[x]==36*Exp[2*x]*Sin[3*x],y[x],x,IncludeSingularSolutio
```

$$y(x) \rightarrow e^{2x}((-1 + c_2) \cos(3x) + (-2x + c_1) \sin(3x) + c_3)$$

11.6 problem 6

Internal problem ID [12779]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.4, page 218

Problem number: 6.

ODE order: 3.

ODE degree: 1.

CAS Maple gives this as type `[[_3rd_order, _linear, _nonhomogeneous]]`

$$y''' + y'' - y' - y = (2x^2 + 4x + 8) \cos(x) + (6x^2 + 8x + 12) \sin(x)$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 43

```
dsolve(diff(y(x),x$3)+diff(y(x),x$2)-diff(y(x),x)-y(x)=(2*x^2+4*x+8)*cos(x)+(6*x^2+8*x+12)*sin(x),y(x),x,IncludeS
```

$$y(x) = (c_3x + c_2) e^{-x} + (x^2 - 6x - 2) \cos(x) + (-2x^2 - 4x + 1) \sin(x) + c_1 e^x$$

✓ Solution by Mathematica

Time used: 0.027 (sec). Leaf size: 55

```
DSolve[y''''[x]+y'''[x]-y''[x]-y'[x]-y[x]==(2*x^2+4*x+8)*Cos[x]+(6*x^2+8*x+12)*Sin[x],y[x],x,IncludeS
```

$$y(x) \rightarrow (x^2 - 6x - 2) \cos(x) + e^{-x} (-e^x (2x^2 + 4x - 1) \sin(x) + c_2x + c_3e^{2x} + c_1)$$

11.7 problem 7

Internal problem ID [12780]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.4, page 218

Problem number: 7.

ODE order: 6.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _linear, _nonhomogeneous]]`

$$y^{(6)} - 12y^{(5)} + 63y^{(4)} - 18y^{(3)} + 315y'' - 300y' + 125y = e^x(48 \cos(x) + 96 \sin(x))$$

✓ Solution by Maple

Time used: 0.062 (sec). Leaf size: 5468

```
dsolve(diff(y(x), x$6)-12*diff(y(x), x$5)+63*diff(y(x), x$4)-18*diff(y(x), x$3)+315*diff(y(x), x$2)-300*diff(y(x), x$1)+125*y(x), x$0)=exp(x)*(48*cos(x)+96*sin(x)), y(x))
```

Expression too large to display

✓ Solution by Mathematica

Time used: 0.024 (sec). Leaf size: 292

```
DSolve[y''''''[x]-12*y''''''[x]+63*y''''''[x]-18*y''''''[x]+315*y''''[x]-300*y''[x]+125*y[x]==Exp[x]*(48*Cos[x]+96*Sin[x]), y[x]]
```

$$\begin{aligned} y(x) \rightarrow & c_3 \exp(x \text{Root}[\#1^6 - 12\#1^5 + 63\#1^4 - 18\#1^3 + 315\#1^2 - 300\#1 + 125\&, 3]) \\ & + c_4 \exp(x \text{Root}[\#1^6 - 12\#1^5 + 63\#1^4 - 18\#1^3 + 315\#1^2 - 300\#1 + 125\&, 4]) \\ & + c_1 \exp(x \text{Root}[\#1^6 - 12\#1^5 + 63\#1^4 - 18\#1^3 + 315\#1^2 - 300\#1 + 125\&, 1]) \\ & + c_2 \exp(x \text{Root}[\#1^6 - 12\#1^5 + 63\#1^4 - 18\#1^3 + 315\#1^2 - 300\#1 + 125\&, 2]) \\ & + c_5 \exp(x \text{Root}[\#1^6 - 12\#1^5 + 63\#1^4 - 18\#1^3 + 315\#1^2 - 300\#1 + 125\&, 5]) \\ & + c_6 \exp(x \text{Root}[\#1^6 - 12\#1^5 + 63\#1^4 - 18\#1^3 + 315\#1^2 - 300\#1 + 125\&, 6]) \\ & - \frac{48e^x(352 \sin(x) + 1011 \cos(x))}{229205} \end{aligned}$$

12 Chapter 4. N-th Order Linear Differential Equations. Exercises 4.5, page 221

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12.1 problem 1

Internal problem ID [12781]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.5, page 221

Problem number: 1.

ODE order: 3.

ODE degree: 1.

CAS Maple gives this as type `[[_3rd_order, _missing_x]]`

$$y''' - 3y'' - 4y' + 12y = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = 5, y''(0) = -1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 23

```
dsolve([diff(y(x),x$3)-3*diff(y(x),x$2)-4*diff(y(x),x)+12*y(x)=0,y(0) = 1, D(y)(0) = 5, D@@
```

$$y(x) = (-e^{5x} + 3e^{4x} - 1)e^{-2x}$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 26

```
DSolve[{y'''[x]-3*y''[x]-4*y'[x]+12*y[x]==0,{y[0]==1,y'[0]==5,y''[0]==-1}},y[x],x,IncludeSin
```

$$y(x) \rightarrow -e^{-2x}(-3e^{4x} + e^{5x} + 1)$$

12.2 problem 2

Internal problem ID [12782]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.5, page 221

Problem number: 2.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_x]]`

$$y'''' - 2y''' + 2y' - y = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = -1, y''(0) = -3, y'''(0) = 3]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 27

```
dsolve([diff(y(x),x$4)-2*diff(y(x),x$3)+2*diff(y(x),x)-y(x)=0,y(0) = 1, D(y)(0) = -1, (D@@2)
```

$$y(x) = -e^{-x} + (2x^2 - 4x + 2)e^x$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 25

```
DSolve[{y''''[x]-2*y'''[x]+2*y'[x]-y[x]==0,{y[0]==1,y'[0]==-1,y''[0]==-3,y'''[0]==3}},y[x],x
```

$$y(x) \rightarrow e^{-x}(2e^{2x}(x-1)^2 - 1)$$

12.3 problem 3

Internal problem ID [12783]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.5, page 221

Problem number: 3.

ODE order: 3.

ODE degree: 1.

CAS Maple gives this as type `[[_3rd_order, _with_linear_symmetries]]`

$$y''' - y'' + y' - y = 2e^x$$

With initial conditions

$$[y(0) = 1, y'(0) = 3, y''(0) = -3]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 19

```
dsolve([diff(y(x),x$3)-diff(y(x),x$2)+diff(y(x),x)-y(x)=2*exp(x),y(0) = 1, D(y)(0) = 3, D@@
```

$$y(x) = (x - 2)e^x + 3 \cos(x) + 4 \sin(x)$$

✓ Solution by Mathematica

Time used: 0.018 (sec). Leaf size: 21

```
DSolve[{y'''[x]-y''[x]+y'[x]-y[x]==2*Exp[x],{y[0]==1,y'[0]==3,y''[0]==-3}},y[x],x,IncludeSin
```

$$y(x) \rightarrow e^x(x - 2) + 4 \sin(x) + 3 \cos(x)$$

12.4 problem 4

Internal problem ID [12784]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 4. N-th Order Linear Differential Equations. Exercises 4.5, page 221

Problem number: 4.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _with_linear_symmetries]]`

$$y'''' + 2y'' + y = 4 + 3x$$

With initial conditions

$$[y(0) = 0, y'(0) = 0, y''(0) = 1, y'''(0) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 26

```
dsolve([diff(y(x),x$4)+2*diff(y(x),x$2)+y(x)=3*x+4,y(0) = 0, D(y)(0) = 0, (D@@2)(y)(0) = 1,
```

$$y(x) = 4 + (x - 4) \cos(x) + \frac{(-3x - 8) \sin(x)}{2} + 3x$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 27

```
DSolve[{y''''[x]+2*y''[x]+y[x]==3*x+4,{y[0]==0,y'[0]==0,y''[0]==1,y'''[0]==1}},y[x],x,Includ
```

$$y(x) \rightarrow 3x - \frac{1}{2}(3x + 8) \sin(x) + (x - 4) \cos(x) + 4$$

13 Chapter 5. The Laplace Transform Method.

Exercises 5.2, page 248

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13.1 problem 1

Internal problem ID [12785]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 1.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - y = 0$$

✓ Solution by Maple

Time used: 4.609 (sec). Leaf size: 9

```
dsolve(diff(y(x),x)-y(x)=0,y(x), singsol=all)
```

$$y(x) = e^x y(0)$$

✓ Solution by Mathematica

Time used: 0.033 (sec). Leaf size: 16

```
DSolve[y'[x]-y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow c_1 e^x$$

$$y(x) \rightarrow 0$$

13.2 problem 2

Internal problem ID [12786]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 2.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - 2y' + 5y = 0$$

✓ Solution by Maple

Time used: 5.516 (sec). Leaf size: 29

```
dsolve(diff(y(x),x$2)-2*diff(y(x),x)+5*y(x)=0,y(x), singsol=all)
```

$$y(x) = \frac{e^x(2y(0) \cos(2x) + \sin(2x)(D(y)(0) - y(0)))}{2}$$

✓ Solution by Mathematica

Time used: 0.024 (sec). Leaf size: 24

```
DSolve[y''[x]-2*y'[x]+5*y[x]==0,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^x(c_2 \cos(2x) + c_1 \sin(2x))$$

13.3 problem 3

Internal problem ID [12787]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 3.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' + 2y = 4$$

✓ Solution by Maple

Time used: 5.422 (sec). Leaf size: 15

```
dsolve(diff(y(x),x)+2*y(x)=4,y(x), singsol=all)
```

$$y(x) = (y(0) - 2)e^{-2x} + 2$$

✓ Solution by Mathematica

Time used: 0.039 (sec). Leaf size: 20

```
DSolve[y'[x]+2*y[x]==4,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 2 + c_1 e^{-2x}$$

$$y(x) \rightarrow 2$$

13.4 problem 4

Internal problem ID [12788]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 4.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' - 9y = 2 \sin(3x)$$

✓ Solution by Maple

Time used: 5.781 (sec). Leaf size: 30

```
dsolve(diff(y(x),x$2)-9*y(x)=2*sin(3*x),y(x), singsol=all)
```

$$y(x) = -\frac{\sin(3x)}{9} + y(0) \cosh(3x) + \frac{\sinh(3x)(1 + 3D(y)(0))}{9}$$

✓ Solution by Mathematica

Time used: 0.032 (sec). Leaf size: 30

```
DSolve[y''[x]-9*y[x]==2*Sin[3*x],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{1}{9} \sin(3x) + c_1 e^{3x} + c_2 e^{-3x}$$

13.5 problem 5

Internal problem ID [12789]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 5.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + 9y = 2 \sin(3x)$$

✓ Solution by Maple

Time used: 5.437 (sec). Leaf size: 29

```
dsolve(diff(y(x),x$2)+9*y(x)=2*sin(3*x),y(x), singsol=all)
```

$$y(x) = -\frac{\cos(3x)(x - 3y(0))}{3} + \frac{\sin(3x)(1 + 3D(y)(0))}{9}$$

✓ Solution by Mathematica

Time used: 0.051 (sec). Leaf size: 33

```
DSolve[y''[x]+9*y[x]==2*Sin[3*x],y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \left(-\frac{x}{3} + c_1\right) \cos(3x) + \frac{1}{18}(1 + 18c_2) \sin(3x)$$

13.6 problem 6

Internal problem ID [12790]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 6.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + y' - 2y = x e^x - 3x^2$$

✓ Solution by Maple

Time used: 5.812 (sec). Leaf size: 52

```
dsolve(diff(y(x),x$2)+diff(y(x),x)-2*y(x)=x*exp(x)-3*x^2,y(x), singsol=all)
```

$$y(x) = \frac{9}{4} + \frac{3x}{2} + \frac{3x^2}{2} + \frac{e^x(9x^2 + 18D(y)(0) + 36y(0) - 6x - 106)}{54} + \frac{(36y(0) - 36D(y)(0) - 31)e^{-2x}}{108}$$

✓ Solution by Mathematica

Time used: 0.313 (sec). Leaf size: 49

```
DSolve[y''[x]+y'[x]-2*y[x]==x*Exp[x]-3*x^2,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{3}{4}(2x^2 + 2x + 3) + \frac{1}{54}e^x(9x^2 - 6x + 2 + 54c_2) + c_1e^{-2x}$$

13.7 problem 7

Internal problem ID [12791]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 7.

ODE order: 4.

ODE degree: 1.

CAS Maple gives this as type `[[_high_order, _missing_y]]`

$$y'''' - 2y''' + y'' = x e^x - 3x^2$$

✓ Solution by Maple

Time used: 5.985 (sec). Leaf size: 79

```
dsolve(diff(y(x),x$4)-2*diff(y(x),x$3)+diff(y(x),x$2)=x*exp(x)-3*x^2,y(x), singsol=all)
```

$$y(x) = -26 - \frac{x^4}{4} - 9x^2 - 2x^3 + y(0) + \frac{e^x(x^3 + 6xD^{(3)}(y)(0) - 6xD^{(2)}(y)(0) - 6x^2 - 12D^{(3)}(y)(0) + 18D^{(2)}(y)(0) - 18x + 156)}{6} - D^{(2)}(y)(0)(3 + 2x) + D^{(3)}(y)(0)(x + 2) + x(-23 + D(y)(0))$$

✓ Solution by Mathematica

Time used: 0.812 (sec). Leaf size: 59

```
DSolve[y''''[x]-2*y'''[x]+y''[x]==x*Exp[x]-3*x^2,y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow -\frac{x^4}{4} - 2x^3 - 9x^2 + e^x \left(\frac{x^3}{6} - x^2 + (3 + c_2)x - 4 + c_1 - 2c_2 \right) + c_4x + c_3$$

13.8 problem 8

Internal problem ID [12792]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 8.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' = e^x$$

With initial conditions

$$[y(0) = -1]$$

✓ Solution by Maple

Time used: 5.328 (sec). Leaf size: 8

```
dsolve([diff(y(x),x)=exp(x),y(0) = -1],y(x), singsol=all)
```

$$y(x) = e^x - 2$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 10

```
DSolve[{y'[x]==Exp[x],{y[0]==-1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^x - 2$$

13.9 problem 9

Internal problem ID [12793]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 9.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_linear, 'class A']]`

$$y' - y = 2e^x$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 5.094 (sec). Leaf size: 12

```
dsolve([diff(y(x),x)-y(x)=2*exp(x),y(0) = 1],y(x), singsol=all)
```

$$y(x) = (2x + 1)e^x$$

✓ Solution by Mathematica

Time used: 0.067 (sec). Leaf size: 14

```
DSolve[{y'[x]-y[x]==2*Exp[x],{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^x(2x + 1)$$

13.10 problem 10

Internal problem ID [12794]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 10.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$y'' - 9y = x + 2$$

With initial conditions

$$[y(0) = -1, y'(0) = 1]$$

✓ Solution by Maple

Time used: 5.391 (sec). Leaf size: 21

```
dsolve([diff(y(x),x$2)-9*y(x)=x+2,y(0) = -1, D(y)(0) = 1],y(x), singsol=all)
```

$$y(x) = -\frac{x}{9} - \frac{7 \cosh(3x)}{9} + \frac{10 \sinh(3x)}{27} - \frac{2}{9}$$

✓ Solution by Mathematica

Time used: 0.026 (sec). Leaf size: 33

```
DSolve[{y'[x]-9*y[x]==x+2,{y[0]==-1,y'[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{54} e^{-3x} (-6e^{3x}(x+2) - 11e^{6x} - 31)$$

13.11 problem 11

Internal problem ID [12795]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 11.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$y'' + 9y = x + 2$$

With initial conditions

$$[y(0) = -1, y'(0) = 1]$$

✓ Solution by Maple

Time used: 5.313 (sec). Leaf size: 21

```
dsolve([diff(y(x),x$2)+9*y(x)=x+2,y(0) = -1, D(y)(0) = 1],y(x), singsol=all)
```

$$y(x) = \frac{x}{9} - \frac{11 \cos(3x)}{9} + \frac{8 \sin(3x)}{27} + \frac{2}{9}$$

✓ Solution by Mathematica

Time used: 0.025 (sec). Leaf size: 26

```
DSolve[{y'[x]+9*y[x]==x+2,{y[0]==-1,y'[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{1}{27}(3x + 8 \sin(3x) - 33 \cos(3x) + 6)$$

13.12 problem 12

Internal problem ID [12796]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 12.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' - y' + 6y = -2 \sin(3x)$$

With initial conditions

$$[y(0) = 0, y'(0) = -1]$$

✓ Solution by Maple

Time used: 6.438 (sec). Leaf size: 45

```
dsolve([diff(y(x),x$2)-diff(y(x),x)+6*y(x)=-2*sin(3*x),y(0) = 0, D(y)(0) = -1],y(x), singsol
```

$$y(x) = -\frac{13 e^{\frac{x}{2}} \sqrt{23} \sin\left(\frac{\sqrt{23}x}{2}\right)}{69} + \frac{e^{\frac{x}{2}} \cos\left(\frac{\sqrt{23}x}{2}\right)}{3} + \frac{\sin(3x)}{3} - \frac{\cos(3x)}{3}$$

✓ Solution by Mathematica

Time used: 0.057 (sec). Leaf size: 67

```
DSolve[{y'[x]-y'[x]+6*y[x]==-2*Sin[3*x],{y[0]==0,y'[0]==-1}},y[x],x,IncludeSingularSolution
```

$$y(x) \rightarrow \frac{1}{69} \left(23 \sin(3x) - 13\sqrt{23}e^{x/2} \sin\left(\frac{\sqrt{23}x}{2}\right) - 23 \cos(3x) + 23e^{x/2} \cos\left(\frac{\sqrt{23}x}{2}\right) \right)$$

13.13 problem 13

Internal problem ID [12797]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 13.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$y'' - 2y' + 2y = -x^2 + 1$$

With initial conditions

$$[y(0) = 1, y'(0) = 0]$$

✓ Solution by Maple

Time used: 5.0 (sec). Leaf size: 18

```
dsolve([diff(y(x),x$2)-2*diff(y(x),x)+2*y(x)=1-x^2,y(0) = 1, D(y)(0) = 0],y(x), singsol=all)
```

$$y(x) = -x - \frac{x^2}{2} + \cos(x) e^x$$

✓ Solution by Mathematica

Time used: 0.026 (sec). Leaf size: 20

```
DSolve[{y'[x]-2*y'[x]+2*y[x]==1-x^2,{y[0]==1,y'[0]==0}},y[x],x,IncludeSingularSolutions ->
```

$$y(x) \rightarrow e^x \cos(x) - \frac{1}{2}x(x + 2)$$

13.14 problem 14

Internal problem ID [12798]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.2, page 248

Problem number: 14.

ODE order: 3.

ODE degree: 1.

CAS Maple gives this as type `[[_3rd_order, _missing_y]]`

$$y''' + 3y'' + 2y' = x + \cos(x)$$

With initial conditions

$$[y(0) = 1, y'(0) = -1, y''(0) = 2]$$

✓ Solution by Maple

Time used: 5.36 (sec). Leaf size: 34

```
dsolve([diff(y(x),x$3)+3*diff(y(x),x$2)+2*diff(y(x),x)=x+cos(x),y(0) = 1, D(y)(0) = -1, D@@
```

$$y(x) = -\frac{3 \cos(x)}{10} + \frac{\sin(x)}{10} - \frac{e^{-x}}{2} - \frac{3x}{4} + \frac{x^2}{4} + \frac{17e^{-2x}}{40} + \frac{11}{8}$$

✓ Solution by Mathematica

Time used: 0.565 (sec). Leaf size: 41

```
DSolve[{y'''[x]+3*y''[x]+2*y'[x]==x+Cos[x],{y[0]==1,y'[0]==-1,y''[0]==2}},y[x],x,IncludeSing
```

$$y(x) \rightarrow \frac{1}{40}(10x^2 - 30x + 17e^{-2x} - 20e^{-x} + 4 \sin(x) - 12 \cos(x) + 55)$$

14 Chapter 5. The Laplace Transform Method.

Exercises 5.3, page 255

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14.1 problem 7

Internal problem ID [12799]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.3, page 255

Problem number: 7.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type [_quadrature]

$$y' - 2y = 6$$

With initial conditions

$$[y(0) = 2]$$

✓ Solution by Maple

Time used: 5.266 (sec). Leaf size: 15

```
dsolve([diff(y(x),x)-2*y(x)=6,y(0) = 2],y(x), singsol=all)
```

$$y(x) = 2e^x(\cosh(x) + 4\sinh(x))$$

✓ Solution by Mathematica

Time used: 0.041 (sec). Leaf size: 14

```
DSolve[{y'[x]-2*y[x]==6,{y[0]==2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 5e^{2x} - 3$$

14.2 problem 8

Internal problem ID [12800]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.3, page 255

Problem number: 8.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_linear, 'class A']`

$$y' + y = e^x$$

With initial conditions

$$\left[y(0) = \frac{5}{2} \right]$$

✓ Solution by Maple

Time used: 5.813 (sec). Leaf size: 13

```
dsolve([diff(y(x),x)+y(x)=exp(x),y(0) = 5/2],y(x), singsol=all)
```

$$y(x) = \frac{5 \cosh(x)}{2} - \frac{3 \sinh(x)}{2}$$

✓ Solution by Mathematica

Time used: 0.066 (sec). Leaf size: 20

```
DSolve[{y'[x]+y[x]==Exp[x],{y[0]==5/2}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow 2e^{-x} + \frac{e^x}{2}$$

14.3 problem 9

Internal problem ID [12801]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.3, page 255

Problem number: 9.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' + 9y = 1$$

With initial conditions

$$[y(0) = 0, y'(0) = 0]$$

✓ Solution by Maple

Time used: 4.921 (sec). Leaf size: 12

```
dsolve([diff(y(x),x$2)+9*y(x)=1,y(0) = 0, D(y)(0) = 0],y(x), singsol=all)
```

$$y(x) = -\frac{\cos(3x)}{9} + \frac{1}{9}$$

✓ Solution by Mathematica

Time used: 0.021 (sec). Leaf size: 17

```
DSolve[{y'[x]+9*y[x]==1,{y[0]==0,y'[0]==0}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow \frac{2}{9} \sin^2\left(\frac{3x}{2}\right)$$

14.4 problem 10

Internal problem ID [12802]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.3, page 255

Problem number: 10.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$y'' + 9y = 18e^{3x}$$

With initial conditions

$$[y(0) = -1, y'(0) = 6]$$

✓ Solution by Maple

Time used: 5.922 (sec). Leaf size: 19

```
dsolve([diff(y(x),x$2)+9*y(x)=18*exp(3*x),y(0) = -1, D(y)(0) = 6],y(x), singsol=all)
```

$$y(x) = -2 \cos(3x) + \sin(3x) + e^{3x}$$

✓ Solution by Mathematica

Time used: 0.029 (sec). Leaf size: 21

```
DSolve[{y''[x]+9*y[x]==18*Exp[3*x],{y[0]==-1,y'[0]==6}},y[x],x,IncludeSingularSolutions -> T
```

$$y(x) \rightarrow e^{3x} + \sin(3x) - 2 \cos(3x)$$

14.5 problem 11

Internal problem ID [12803]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.3, page 255

Problem number: 11.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$y'' - y' - 2y = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 3]$$

✓ Solution by Maple

Time used: 5.203 (sec). Leaf size: 15

```
dsolve([diff(y(x),x$2)-diff(y(x),x)-2*y(x)=0,y(0) = 0, D(y)(0) = 3],y(x), singsol=all)
```

$$y(x) = -e^{-x} + e^{2x}$$

✓ Solution by Mathematica

Time used: 0.022 (sec). Leaf size: 18

```
DSolve[{y'[x]-y'[x]-2*y[x]==0,{y[0]==0,y'[0]==3}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{-x}(e^{3x} - 1)$$

14.6 problem 12

Internal problem ID [12804]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.3, page 255

Problem number: 12.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$y'' - y' - 2y = x^2$$

With initial conditions

$$\left[y(0) = \frac{11}{4}, y'(0) = \frac{1}{2} \right]$$

✓ Solution by Maple

Time used: 5.016 (sec). Leaf size: 26

```
dsolve([diff(y(x),x$2)-diff(y(x),x)-2*y(x)=x^2,y(0) = 11/4, D(y)(0) = 1/2],y(x), singsol=all
```

$$y(x) = \frac{7e^{-x}}{3} + \frac{x}{2} - \frac{x^2}{2} + \frac{7e^{2x}}{6} - \frac{3}{4}$$

✓ Solution by Mathematica

Time used: 0.024 (sec). Leaf size: 33

```
DSolve[{y'[x]-y'[x]-2*y[x]==x^2,{y[0]==11/4,y'[0]==1/2}},y[x],x,IncludeSingularSolutions ->
```

$$y(x) \rightarrow \frac{1}{12}(-6x^2 + 6x + 28e^{-x} + 14e^{2x} - 9)$$

14.7 problem 13

Internal problem ID [12805]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.3, page 255

Problem number: 13.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' - 2y' + y = 2 \sin(x)$$

With initial conditions

$$[y(0) = -2, y'(0) = 0]$$

✓ Solution by Maple

Time used: 5.109 (sec). Leaf size: 14

```
dsolve([diff(y(x),x$2)-2*diff(y(x),x)+y(x)=2*sin(x),y(0) = -2, D(y)(0) = 0],y(x), singsol=al
```

$$y(x) = (3x - 3)e^x + \cos(x)$$

✓ Solution by Mathematica

Time used: 0.03 (sec). Leaf size: 16

```
DSolve[{y'[x]-2*y'[x]+y[x]==2*Sin[x],{y[0]==-2,y'[0]==0}},y[x],x,IncludeSingularSolutions -
```

$$y(x) \rightarrow 3e^x(x - 1) + \cos(x)$$

14.8 problem 14

Internal problem ID [12806]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.3, page 255

Problem number: 14.

ODE order: 3.

ODE degree: 1.

CAS Maple gives this as type `[[_3rd_order, _missing_x]]`

$$y''' - y'' + 4y' - 4y = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 5, y''(0) = 5]$$

✓ Solution by Maple

Time used: 5.813 (sec). Leaf size: 19

```
dsolve([diff(y(x),x$3)-diff(y(x),x$2)+4*diff(y(x),x)-4*y(x)=0,y(0) = 0, D(y)(0) = 5, (D@@2)(
```

$$y(x) = e^x - \cos(2x) + 2 \sin(2x)$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 21

```
DSolve[{y'''[x]-y''[x]+4*y'[x]-4*y[x]==0,{y[0]==0,y'[0]==5,y''[0]==5}},y[x],x,IncludeSingular
```

$$y(x) \rightarrow e^x + 2 \sin(2x) - \cos(2x)$$

15 Chapter 5. The Laplace Transform Method.

Exercises 5.4, page 265

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15.1 problem 4 (a)

Internal problem ID [12807]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.4, page 265

Problem number: 4 (a).

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_linear, 'class A']`

$$y' + 2y = \begin{cases} 2 & 0 \leq x < 1 \\ 1 & 1 \leq x \end{cases}$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 7.625 (sec). Leaf size: 22

```
dsolve([diff(y(x),x)+2*y(x)=piecewise(0<=x and x<1,2,1<=x,1),y(0) = 1],y(x), singsol=all)
```

$$y(x) = \begin{cases} 1 & x < 1 \\ \frac{1}{2} + \frac{e^{2-2x}}{2} & 1 \leq x \end{cases}$$

✓ Solution by Mathematica

Time used: 0.113 (sec). Leaf size: 37

```
DSolve[{y'[x]+2*y[x]==Piecewise[{ {2,0<=x<1},{1,1<=x}}],{y[0]==1}],y[x],x,IncludeSingularSol
```

$$y(x) \rightarrow \begin{cases} e^{-2x} & x \leq 0 \\ 1 & 0 < x \leq 1 \\ \frac{1}{2}(1 + e^{2-2x}) & \text{True} \end{cases}$$

15.2 problem 4 (b)

Internal problem ID [12808]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.4, page 265

Problem number: 4 (b).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' - y' - 2y = \begin{cases} 1 & 2 \leq x < 4 \\ 0 & \text{otherwise} \end{cases}$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

✓ Solution by Maple

Time used: 8.969 (sec). Leaf size: 136

```
dsolve([diff(y(x),x$2)-diff(y(x),x)-2*y(x)=piecewise(2<=x and x<4,1,true,0),y(0) = 0, D(y)(0) = 1])
```

$$y(x) = \frac{\left(\begin{array}{ll} -e^{-x} + e^{2x} & x < 2 \\ -\frac{1}{2} - e^{-2} + e^4 & x = 2 \\ -e^{-x} + e^{2x} - \frac{3}{2} + e^{2-x} + \frac{e^{2x-4}}{2} & x < 4 \\ \frac{(2e^{12} + e^8 - 2e^4 + 2e^2 - 2)e^{-4}}{2} & x = 4 \\ -e^{-x} + e^{2x} - e^{4-x} + e^{2-x} - \frac{e^{2x-8}}{2} + \frac{e^{2x-4}}{2} & 4 < x \end{array} \right)}{3}$$

✓ Solution by Mathematica

Time used: 0.068 (sec). Leaf size: 127

```
DSolve[{y'[x]-y'[x]-2*y[x]==Piecewise[{ {1,2<=x<4},{0,True}}],{y[0]==0,y'[0]==1}},y[x],x,In
```

$$y(x) \rightarrow \begin{cases} \frac{1}{3}e^{-x}(-1 + e^{3x}) & x \leq 2 \\ \frac{1}{6}e^{-x-4}(-2e^4 + 2e^6 + e^{3x} - 3e^{x+4} + 2e^{3x+4}) & 2 < x \leq 4 \\ \frac{1}{6}e^{-x-8}(-2e^8 + 2e^{10} - 2e^{12} - e^{3x} + e^{3x+4} + 2e^{3x+8}) & \text{True} \end{cases}$$

15.3 problem 4 (c)

Internal problem ID [12809]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.4, page 265

Problem number: 4 (c).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_y]]`

$$y'' - 2y' = \begin{cases} 0 & 0 \leq x < 1 \\ (x-1)^2 & 1 \leq x \end{cases}$$

With initial conditions

$$[y(0) = 1, y'(0) = 0]$$

✓ Solution by Maple

Time used: 9.25 (sec). Leaf size: 39

```
dsolve([diff(y(x),x$2)-2*diff(y(x),x)=piecewise(0<=x and x<1,0,1<=x,(x-1)^2),y(0) = 1, D(y)
```

$$y(x) = \begin{cases} 1 & x < 1 \\ \frac{7}{8} & x = 1 \\ \frac{25}{24} + \frac{e^{2x-2}}{8} + \frac{x^2}{4} - \frac{x^3}{6} - \frac{x}{4} & 1 < x \end{cases}$$

✓ Solution by Mathematica

Time used: 0.269 (sec). Leaf size: 40

```
DSolve[{y'[x]-2*y'[x]==Piecewise[{0,0<=x<1},{(x-1)^2,x>=1}],{y[0]==1,y'[0]==0}},y[x],x,D
```

$$y(x) \rightarrow \begin{cases} 1 & x \leq 1 \\ \frac{1}{24}(-4x^3 + 6x^2 - 6x + 3e^{2x-2} + 25) & \text{True} \end{cases}$$

15.4 problem 4 (d)

Internal problem ID [12810]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.4, page 265

Problem number: 4 (d).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' - 2y' + y = \begin{cases} 0 & 0 \leq x < 1 \\ x^2 - 2x + 3 & 1 \leq x \end{cases}$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

✓ Solution by Maple

Time used: 7.61 (sec). Leaf size: 43

```
dsolve([diff(y(x),x$2)-2*diff(y(x),x)+y(x)=piecewise(0<=x and x<1,0,1<=x,x^2-2*x+3),y(0) = 0
```

$$y(x) = \begin{cases} e^x x & x < 1 \\ e + 8 & x = 1 \\ e^x x + 5 + 4(-3 + x) e^{-1+x} + x^2 + 2x & 1 < x \end{cases}$$

✓ Solution by Mathematica

Time used: 0.044 (sec). Leaf size: 39

```
DSolve[{y'[x]-2*y'[x]+y[x]==Piecewise[{ {0,0<=x<1},{x^2-2*x+3,x>=1}},{y[0]==0,y'[0]==1}],y
```

$$y(x) \rightarrow \begin{cases} e^x x & x \leq 1 \\ x^2 + e^x x + 2x + 4e^{x-1}(x-3) + 5 & \text{True} \end{cases}$$

15.5 problem 4 (e)

Internal problem ID [12811]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.4, page 265

Problem number: 4 (e).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + 4y = \begin{cases} 0 & 0 \leq x < \pi \\ -\sin(3x) & \pi \leq x \end{cases}$$

With initial conditions

$$[y(0) = 1, y'(0) = 1]$$

✓ Solution by Maple

Time used: 8.188 (sec). Leaf size: 39

```
dsolve([diff(y(x),x$2)+4*y(x)=piecewise(0<=x and x<Pi,0,Pi<=x,sin(3*(x-Pi))),y(0) = 1, D(y)
```

$$y(x) = \cos(2x) + \begin{cases} \frac{\sin(2x)}{2} & x < \pi \\ \frac{4\sin(2x)}{5} + \frac{\sin(3x)}{5} & \pi \leq x \end{cases}$$

✓ Solution by Mathematica

Time used: 0.058 (sec). Leaf size: 42

```
DSolve[{y'[x]+4*y[x]==Piecewise[{0,0<=x<Pi},{Sin[3*(x-Pi)],x>=Pi}],{y[0]==1,y'[0]==1}},y
```

$$y(x) \rightarrow \begin{cases} \cos(2x) + \cos(x) \sin(x) & x \leq \pi \\ \frac{1}{5}(5 \cos(2x) + 4 \sin(2x) + \sin(3x)) & \text{True} \end{cases}$$

15.6 problem 4 (g)

Internal problem ID [12812]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.4, page 265

Problem number: 4 (g).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' - 4y = \begin{cases} x & 0 \leq x < 1 \\ 1 & 1 \leq x \end{cases}$$

With initial conditions

$$[y(0) = 0, y'(0) = 0]$$

✓ Solution by Maple

Time used: 8.235 (sec). Leaf size: 46

```
dsolve([diff(y(x),x$2)-4*y(x)=piecewise(0<=x and x<1,x,1<=x,1),y(0) = 0, D(y)(0) = 0],y(x),
```

$$y(x) = \frac{\begin{pmatrix} \begin{cases} \sinh(2x) - 2x & x < 1 \\ \sinh(2) - 4 & x = 1 \\ \sinh(2x) - \sinh(2x - 2) - 2 & 1 < x \end{cases} \end{pmatrix}}{8}$$

✓ Solution by Mathematica

Time used: 0.045 (sec). Leaf size: 36

```
DSolve[{y''[x]-4*y[x]==Piecewise[{ {x,0<=x<1},{x,x>=1}]}],{y[0]==0,y'[0]==0}],y[x],x,IncludeS
```

$$y(x) \rightarrow \begin{cases} 0 & x \leq 0 \\ \frac{1}{16}e^{-2x}(-4e^{2x}x + e^{4x} - 1) & \text{True} \end{cases}$$

15.7 problem 4 (h)

Internal problem ID [12813]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.4, page 265

Problem number: 4 (h).

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' - 4y' + 5y = \begin{cases} x & 0 \leq x < 1 \\ 1 & 1 \leq x \end{cases}$$

With initial conditions

$$[y(0) = 1, y'(0) = 0]$$

✓ Solution by Maple

Time used: 8.484 (sec). Leaf size: 87

```
dsolve([diff(y(x),x$2)-4*diff(y(x),x)+5*y(x)=piecewise(0<=x and x<1,x,1<=x,1),y(0) = 1, D(y
```

$y(x)$

$$= \frac{\begin{pmatrix} \begin{cases} 4 + 5x + e^{2x}(21 \cos(x) - 47 \sin(x)) & x < 1 \\ 10 + e^2(21 \cos(1) - 47 \sin(1)) & x = 1 \\ (4 \cos(-1 + x) - 3 \sin(-1 + x))e^{2x-2} + 5 + e^{2x}(21 \cos(x) - 47 \sin(x)) & 1 < x \end{cases} \end{pmatrix}}{25}$$

✓ Solution by Mathematica

Time used: 0.052 (sec). Leaf size: 51

```
DSolve[{y''[x]-4*y'[x]+5*y[x]==Piecewise[{ {x,0<=x<1},{1,x>=1}},{y[0]==1,y'[0]==0}],y[x],x,
```

$$y(x) \rightarrow \begin{cases} e^{2x}(\cos(x) - 2 \sin(x)) & x \leq 0 \\ \frac{1}{25}(5x + 21e^{2x} \cos(x) - 47e^{2x} \sin(x) + 4) & \text{True} \end{cases}$$

16 Chapter 5. The Laplace Transform Method.

Exercises 5.5, page 273

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16.1 problem 1

Internal problem ID [12814]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.5, page 273

Problem number: 1.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[_linear, 'class A']`

$$y' + 3y = \delta(x - 2)$$

With initial conditions

$$[y(0) = 1]$$

✓ Solution by Maple

Time used: 5.921 (sec). Leaf size: 20

```
dsolve([diff(y(x),x)+3*y(x)=Dirac(x-2),y(0) = 1],y(x), singsol=all)
```

$$y(x) = \text{Heaviside}(x - 2) e^{6-3x} + e^{-3x}$$

✓ Solution by Mathematica

Time used: 0.052 (sec). Leaf size: 21

```
DSolve[{y'[x]+3*y[x]==DiracDelta[x-2],{y[0]==1}},y[x],x,IncludeSingularSolutions -> True]
```

$$y(x) \rightarrow e^{-3x}(e^6 \theta(x - 2) + 1)$$

16.2 problem 2

Internal problem ID [12815]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.5, page 273

Problem number: 2.

ODE order: 1.

ODE degree: 1.

CAS Maple gives this as type `[[_linear, 'class A']]`

$$y' - 3y = \delta(x - 1) + 2 \operatorname{Heaviside}(x - 2)$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 6.234 (sec). Leaf size: 46

```
dsolve([diff(y(x),x)-3*y(x)=Dirac(x-1)+2*Heaviside(x-2),y(0) = 0],y(x), singsol=all)
```

$$y(x) = -\frac{2 \operatorname{Heaviside}(x - 2)}{3} + \frac{2 \operatorname{Heaviside}(x - 2) e^{-6+3x}}{3} + \operatorname{Heaviside}(-1 + x) e^{3x-3}$$

✓ Solution by Mathematica

Time used: 0.212 (sec). Leaf size: 44

```
DSolve[{y'[x]-3*y[x]==DiracDelta[x-1]+2*UnitStep[x-2],{y[0]==0}},y[x],x,IncludeSingularSolut
```

$$y(x) \rightarrow e^{3x-3} \theta(x - 1) + \frac{2(e^6 - e^{3x})(\theta(2 - x) - 1)}{3e^6}$$

16.3 problem 3

Internal problem ID [12816]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.5, page 273

Problem number: 3.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + 9y = \delta(x - \pi) + \delta(x - 3\pi)$$

With initial conditions

$$[y(0) = 0, y'(0) = 0]$$

✓ Solution by Maple

Time used: 6.469 (sec). Leaf size: 23

```
dsolve([diff(y(x),x$2)+9*y(x)=Dirac(x-Pi)+Dirac(x-3*Pi),y(0) = 0, D(y)(0) = 0],y(x), singsol
```

$$y(x) = -\frac{(\text{Heaviside}(x - 3\pi) + \text{Heaviside}(x - \pi)) \sin(3x)}{3}$$

✓ Solution by Mathematica

Time used: 0.085 (sec). Leaf size: 26

```
DSolve[{y''[x]+9*y[x]==DiracDelta[x-Pi]+DiracDelta[x-3*Pi],{y[0]==0,y'[0]==0}},y[x],x,Includ
```

$$y(x) \rightarrow -\frac{1}{3}(\theta(x - 3\pi) + \theta(x - \pi)) \sin(3x)$$

16.4 problem 4

Internal problem ID [12817]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.5, page 273

Problem number: 4.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' - 2y' + y = 2\delta(x - 1)$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

✓ Solution by Maple

Time used: 6.187 (sec). Leaf size: 28

```
dsolve([diff(y(x),x$2)-2*diff(y(x),x)+y(x)=2*Dirac(x-1),y(0) = 0, D(y)(0) = 1],y(x), singsol
```

$$y(x) = 2 \operatorname{Heaviside}(-1 + x) e^{-1+x}(-1 + x) + e^x x$$

✓ Solution by Mathematica

Time used: 0.039 (sec). Leaf size: 24

```
DSolve[{y''[x]-2*y'[x]+y[x]==2*DiracDelta[x-1],{y[0]==0,y'[0]==1}},y[x],x,IncludeSingularSol
```

$$y(x) \rightarrow e^{x-1}(2(x-1)\theta(x-1) + ex)$$

16.5 problem 5

Internal problem ID [12818]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.5, page 273

Problem number: 5.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' - 2y' + 5y = \cos(x) + 2\delta(x - \pi)$$

With initial conditions

$$[y(0) = 1, y'(0) = 0]$$

✓ Solution by Maple

Time used: 6.625 (sec). Leaf size: 50

```
dsolve([diff(y(x),x$2)-2*diff(y(x),x)+5*y(x)=cos(x)+2*Dirac(x-Pi),y(0) = 1, D(y)(0) = 0],y(x)
```

$$y(x) = \sin(2x) \operatorname{Heaviside}(x - \pi) e^{x-\pi} + \frac{4e^x \cos(2x)}{5} - \frac{7e^x \sin(2x)}{20} - \frac{\sin(x)}{10} + \frac{\cos(x)}{5}$$

✓ Solution by Mathematica

Time used: 0.506 (sec). Leaf size: 54

```
DSolve[{y'[x]-2*y'[x]+5*y[x]==Cos[x]+2*DiracDelta[x-Pi],{y[0]==1,y'[0]==0}},y[x],x,IncludeS
```

$$y(x) \rightarrow \frac{1}{10} (10e^{x-\pi} \theta(x - \pi) \sin(2x) - \sin(x) + 8e^x \cos(2x) + (2 - 7e^x \sin(x)) \cos(x))$$

16.6 problem 6

Internal problem ID [12819]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.5, page 273

Problem number: 6.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + 4y = \delta(x - \pi) \cos(x)$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

✓ Solution by Maple

Time used: 5.968 (sec). Leaf size: 16

```
dsolve([diff(y(x),x$2)+4*y(x)=cos(x)*Dirac(x-Pi),y(0) = 0, D(y)(0) = 1],y(x), singsol=all)
```

$$y(x) = -\frac{\sin(2x)(-1 + \text{Heaviside}(x - \pi))}{2}$$

✓ Solution by Mathematica

Time used: 0.06 (sec). Leaf size: 19

```
DSolve[{y''[x]+4*y[x]==Cos[x]*DiracDelta[x-Pi],{y[0]==0,y'[0]==1}},y[x],x,IncludeSingularSol
```

$$y(x) \rightarrow (\theta(x - \pi) - 1) \sin(x)(-\cos(x))$$

16.7 problem 7

Internal problem ID [12820]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 5. The Laplace Transform Method. Exercises 5.5, page 273

Problem number: 7.

ODE order: 2.

ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + ya^2 = \delta(x - \pi) f(x)$$

With initial conditions

$$[y(0) = 0, y'(0) = 0]$$

✓ Solution by Maple

Time used: 6.188 (sec). Leaf size: 24

```
dsolve([diff(y(x),x$2)+a^2*y(x)=Dirac(x-Pi)*f(x),y(0) = 0, D(y)(0) = 0],y(x), singsol=all)
```

$$y(x) = \frac{\text{Heaviside}(x - \pi) \sin(a(x - \pi)) f(\pi)}{a}$$

✓ Solution by Mathematica

Time used: 0.398 (sec). Leaf size: 26

```
DSolve[{y''[x]+a^2*y[x]==DiracDelta[x-Pi]*f[x],{y[0]==0,y'[0]==0}},y[x],x,IncludeSingularSol
```

$$y(x) \rightarrow -\frac{f(\pi)\theta(x - \pi) \sin(a(\pi - x))}{a}$$

17 Chapter 7. Systems of First-Order Differential Equations. Exercises page 329

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17.1 problem 1

Internal problem ID [12821]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 7. Systems of First-Order Differential Equations. Exercises page 329

Problem number: 1.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = 2y_1(x) - 3y_2(x)$$

$$y_2'(x) = y_1(x) - 2y_2(x)$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 31

```
dsolve([diff(y__1(x),x)=2*y__1(x)-3*y__2(x),diff(y__2(x),x)=y__1(x)-2*y__2(x)],singsol=all)
```

$$y_1(x) = c_1 e^x + c_2 e^{-x}$$

$$y_2(x) = \frac{c_1 e^x}{3} + c_2 e^{-x}$$

✓ Solution by Mathematica

Time used: 0.01 (sec). Leaf size: 72

```
DSolve[{y1'[x]==2*y1[x]-3*y2[x],y2'[x]==y1[x]-2*y2[x]},{y1[x],y2[x]},x,IncludeSingularSoluti
```

$$y_1(x) \rightarrow \frac{1}{2} e^{-x} (c_1 (3e^{2x} - 1) - 3c_2 (e^{2x} - 1))$$

$$y_2(x) \rightarrow \frac{1}{2} e^{-x} (c_1 (e^{2x} - 1) - c_2 (e^{2x} - 3))$$

17.2 problem 3

Internal problem ID [12822]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 7. Systems of First-Order Differential Equations. Exercises page 329

Problem number: 3.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = y_1(x) - 2y_2(x)$$

$$y_2'(x) = y_1(x) + 3y_2(x)$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 46

```
dsolve([diff(y__1(x),x)=y__1(x)-2*y__2(x),diff(y__2(x),x)=y__1(x)+3*y__2(x)],singsol=all)
```

$$y_1(x) = e^{2x}(\sin(x) c_1 + \cos(x) c_2)$$
$$y_2(x) = -\frac{e^{2x}(\sin(x) c_1 - \sin(x) c_2 + \cos(x) c_1 + \cos(x) c_2)}{2}$$

✓ Solution by Mathematica

Time used: 0.009 (sec). Leaf size: 51

```
DSolve[{y1'[x]==y1[x]-2*y2[x],y2'[x]==y1[x]+3*y2[x]},{y1[x],y2[x]},x,IncludeSingularSolution
```

$$y_1(x) \rightarrow e^{2x}(c_1 \cos(x) - (c_1 + 2c_2) \sin(x))$$
$$y_2(x) \rightarrow e^{2x}(c_2 \cos(x) + (c_1 + c_2) \sin(x))$$

17.3 problem 4

Internal problem ID [12823]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 7. Systems of First-Order Differential Equations. Exercises page 329

Problem number: 4.

ODE order: 1.

ODE degree: 1.

Solve

$$\begin{aligned}y_1'(x) &= y_1(x) + 2y_2(x) + x - 1 \\y_2'(x) &= 3y_1(x) + 2y_2(x) - 5x - 2\end{aligned}$$

With initial conditions

$$[y_1(0) = -2, y_2(0) = 3]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 18

```
dsolve([diff(y__1(x),x) = y__1(x)+2*y__2(x)+x-1, diff(y__2(x),x) = 3*y__1(x)+2*y__2(x)-5*x-2
```

$$\begin{aligned}y_1(x) &= -2 + 3x \\y_2(x) &= 3 - 2x\end{aligned}$$

✓ Solution by Mathematica

Time used: 0.316 (sec). Leaf size: 18

```
DSolve[{y1'[x]==y1[x]+2*y2[x]+x-1,y2'[x]==3*y1[x]+2*y2[x]-5*x-2},{y1[0]==-2,y2[0]==3},{y1[x]
```

$$\begin{aligned}y_1(x) &\rightarrow 3x - 2 \\y_2(x) &\rightarrow 3 - 2x\end{aligned}$$

17.4 problem 5

Internal problem ID [12824]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 7. Systems of First-Order Differential Equations. Exercises page 329

Problem number: 5.

ODE order: 1.

ODE degree: 1.

Solve

$$\begin{aligned}y_1'(x) &= \frac{2y_1(x)}{x} - \frac{y_2(x)}{x^2} - 3 + \frac{1}{x} - \frac{1}{x^2} \\y_2'(x) &= 2y_1(x) + 1 - 6x\end{aligned}$$

With initial conditions

$$[y_1(1) = -2, y_2(1) = -5]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 20

```
dsolve([diff(y__1(x),x) = 2*y__1(x)/x-y__2(x)/x^2-3+1/x-1/x^2, diff(y__2(x),x) = 2*y__1(x)+1-6*x], [y1(1)=-2, y2(1)=-5])
```

$$\begin{aligned}y_1(x) &= -2x \\y_2(x) &= -1 + x(-5x + 1)\end{aligned}$$

✓ Solution by Mathematica

Time used: 0.012 (sec). Leaf size: 19

```
DSolve[{y1'[x]==2*y1[x]/x-y2[x]/x^2-3+1/x-1/x^2,y2'[x]==2*y1[x]+1-6*x},{y1[1]==-2,y2[1]==-5}]
```

$$\begin{aligned}y_1(x) &\rightarrow -2x \\y_2(x) &\rightarrow -5x^2 + x - 1\end{aligned}$$

17.5 problem 6

Internal problem ID [12825]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 7. Systems of First-Order Differential Equations. Exercises page 329

Problem number: 6.

ODE order: 1.

ODE degree: 1.

Solve

$$\begin{aligned}y_1'(x) &= \frac{5y_1(x)}{x} + \frac{4y_2(x)}{x} - 2x \\y_2'(x) &= -\frac{6y_1(x)}{x} - \frac{5y_2(x)}{x} + 5x\end{aligned}$$

With initial conditions

$$[y_1(-1) = 3, y_2(-1) = -3]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 39

```
dsolve([diff(y__1(x),x) = 5*y__1(x)/x+4*y__2(x)/x-2*x, diff(y__2(x),x) = -6*y__1(x)/x-5*y__2(x)/x+5*x],{y1[-1]==3,y2[-1]==-3})
```

$$\begin{aligned}y_1(x) &= \frac{2x^3 + x^2 - 2}{x} \\y_2(x) &= -\frac{2x^3 + 2x^2 - 6}{2x}\end{aligned}$$

✓ Solution by Mathematica

Time used: 0.021 (sec). Leaf size: 33

```
DSolve[{y1'[x]==5*y1[x]/x+4*y2[x]/x-2*x,y2'[x]==-6*y1[x]/x-5*y2[x]/x+5*x},{y1[-1]==3,y2[-1]==-3}]
```

$$\begin{aligned}y_1(x) &\rightarrow 2x^2 + x - \frac{2}{x} \\y_2(x) &\rightarrow -\frac{x^3 + x^2 - 3}{x}\end{aligned}$$

17.6 problem 13 (a)

Internal problem ID [12826]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 7. Systems of First-Order Differential Equations. Exercises page 329

Problem number: 13 (a).

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = 3y_1(x) - 2y_2(x)$$

$$y_2'(x) = -y_1(x) + y_2(x)$$

With initial conditions

$$[y_1(0) = 1, y_2(0) = -1]$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 119

```
dsolve([diff(y__1(x),x) = 3*y__1(x)-2*y__2(x), diff(y__2(x),x) = -y__1(x)+y__2(x), y__1(0) =
```

$$y_1(x) = \left(\frac{1}{2} + \frac{\sqrt{3}}{2}\right) e^{(2+\sqrt{3})x} + \left(\frac{1}{2} - \frac{\sqrt{3}}{2}\right) e^{-(2+\sqrt{3})x}$$
$$y_2(x) = -\frac{\left(\frac{1}{2} + \frac{\sqrt{3}}{2}\right) e^{(2+\sqrt{3})x} \sqrt{3}}{2} + \frac{\left(\frac{1}{2} - \frac{\sqrt{3}}{2}\right) e^{-(2+\sqrt{3})x} \sqrt{3}}{2}$$
$$+ \frac{\left(\frac{1}{2} + \frac{\sqrt{3}}{2}\right) e^{(2+\sqrt{3})x}}{2} + \frac{\left(\frac{1}{2} - \frac{\sqrt{3}}{2}\right) e^{-(2+\sqrt{3})x}}{2}$$

✓ Solution by Mathematica

Time used: 0.023 (sec). Leaf size: 79

```
DSolve[{y1'[x]==3*y1[x]-2*y2[x],y2'[x]==-y1[x]+y2[x]},{y1[0]==1,y2[0]==-1},{y1[x],y2[x]},x,I
```

$$y_1(x) \rightarrow \frac{1}{2} e^{-((\sqrt{3}-2)x)} \left((1 + \sqrt{3}) e^{2\sqrt{3}x} + 1 - \sqrt{3} \right)$$

$$y_2(x) \rightarrow -\frac{1}{2} e^{-((\sqrt{3}-2)x)} \left(e^{2\sqrt{3}x} + 1 \right)$$

17.7 problem 13 (b(i))

Internal problem ID [12827]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 7. Systems of First-Order Differential Equations. Exercises page 329

Problem number: 13 (b(i)).

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = \sin(x) y_1(x) + \sqrt{x} y_2(x) + \ln(x)$$

$$y_2'(x) = \tan(x) y_1(x) - e^x y_2(x) + 1$$

With initial conditions

$$[y_1(1) = 1, y_2(1) = -1]$$

X Solution by Maple

```
dsolve([diff(y__1(x),x) = sin(x)*y__1(x)+x^(1/2)*y__2(x)+ln(x), diff(y__2(x),x) = tan(x)*y__
```

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

```
DSolve[{y1'[x]==Sin[x]*y1[x]+Sqrt[x]*y2[x]+Log[x],y2'[x]==Tan[x]*y1[x]-Exp[x]*y2[x]+1},{y1[1]=1,y2[1]=-1},x]
```

Not solved

17.8 problem 13 (b(ii))

Internal problem ID [12828]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 7. Systems of First-Order Differential Equations. Exercises page 329

Problem number: 13 (b(ii)).

ODE order: 1.

ODE degree: 1.

Solve

$$\begin{aligned}y_1'(x) &= \sin(x) y_1(x) + \sqrt{x} y_2(x) + \ln(x) \\y_2'(x) &= \tan(x) y_1(x) - e^x y_2(x) + 1\end{aligned}$$

With initial conditions

$$[y_1(2) = 1, y_2(2) = -1]$$

X Solution by Maple

```
dsolve([diff(y__1(x),x) = sin(x)*y__1(x)+x^(1/2)*y__2(x)+ln(x), diff(y__2(x),x) = tan(x)*y__
```

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

```
DSolve[{y1'[x]==Sin[x]*y1[x]+Sqrt[x]*y2[x]+Log[x],y2'[x]==Tan[x]*y1[x]-Exp[x]*y2[x]+1},{y1[2
```

Not solved

17.9 problem 13 (c(i))

Internal problem ID [12829]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 7. Systems of First-Order Differential Equations. Exercises page 329

Problem number: 13 (c(i)).

ODE order: 1.

ODE degree: 1.

Solve

$$\begin{aligned}y_1'(x) &= e^{-x}y_1(x) - \sqrt{x+1}y_2(x) + x^2 \\ y_2'(x) &= \frac{y_1(x)}{x^2 - 4x + 4}\end{aligned}$$

With initial conditions

$$[y_1(0) = 0, y_2(0) = 1]$$

X Solution by Maple

```
dsolve([diff(y__1(x),x) = exp(-x)*y__1(x)-(1+x)^(1/2)*y__2(x)+x^2, diff(y__2(x),x) = y__1(x)
```

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

```
DSolve[{y1'[x]==Exp[-x]*y1[x]-Sqrt[x+1]*y2[x]+x^2,y2'[x]==y1[x]/(x-2)^2},{y1[0]==0,y2[0]==1}
```

Not solved

17.10 problem 13 (c(ii))

Internal problem ID [12830]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 7. Systems of First-Order Differential Equations. Exercises page 329

Problem number: 13 (c(ii)).

ODE order: 1.

ODE degree: 1.

Solve

$$\begin{aligned}y_1'(x) &= e^{-x}y_1(x) - \sqrt{x+1}y_2(x) + x^2 \\y_2'(x) &= \frac{y_1(x)}{x^2 - 4x + 4}\end{aligned}$$

With initial conditions

$$[y_1(3) = 1, y_2(3) = 0]$$

X Solution by Maple

```
dsolve([diff(y__1(x),x) = exp(-x)*y__1(x)-(1+x)^(1/2)*y__2(x)+x^2, diff(y__2(x),x) = y__1(x)
```

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

```
DSolve[{y1'[x]==Exp[-x]*y1[x]-Sqrt[x+1]*y2[x]+x^2,y2'[x]==y1[x]/(x-2)^2},{y1[3]==1,y2[3]==0}
```

Not solved

18 Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

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18.1 problem 1

Internal problem ID [12839]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 1.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = 2y_1(x) - 3y_2(x) + 5e^x$$

$$y_2'(x) = y_1(x) + 4y_2(x) - 2e^{-x}$$

✓ Solution by Maple

Time used: 0.157 (sec). Leaf size: 112

```
dsolve([diff(y__1(x),x)=2*y__1(x)-3*y__2(x)+5*exp(x),diff(y__2(x),x)=y__1(x)+4*y__2(x)-2*exp
```

$$y_1(x) = e^{3x} \cos(\sqrt{2}x) c_2 + e^{3x} \sin(\sqrt{2}x) c_1 + \frac{e^{-x}}{3} - \frac{5e^x}{2}$$
$$y_2(x) = -\frac{e^{3x} \cos(\sqrt{2}x) c_2}{3} + \frac{e^{3x} \sqrt{2} \sin(\sqrt{2}x) c_2}{3}$$
$$-\frac{e^{3x} \sin(\sqrt{2}x) c_1}{3} - \frac{e^{3x} \sqrt{2} \cos(\sqrt{2}x) c_1}{3} + \frac{e^{-x}}{3} + \frac{5e^x}{6}$$

✓ Solution by Mathematica

Time used: 0.032 (sec). Leaf size: 108

```
DSolve[{y1'[x]==2*y1[x]-3*y2[x]+5*Exp[x],y2'[x]==y1[x]+4*y2[x]-2*Exp[-x]},{y1[x],y2[x]},x,In
```

$$y_1(x) \rightarrow -\frac{1}{2}e^x \left(-2c_1 e^{2x} \cos(\sqrt{2}x) + \sqrt{2}(c_1 + 3c_2)e^{2x} \sin(\sqrt{2}x) + 5 \right)$$
$$y_2(x) \rightarrow \frac{5e^x}{6} + c_2 e^{3x} \cos(\sqrt{2}x) + \frac{(c_1 + c_2)e^{3x} \sin(\sqrt{2}x)}{\sqrt{2}}$$

18.2 problem 2

Internal problem ID [12840]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 2.

ODE order: 1.

ODE degree: 1.

Solve

$$\begin{aligned}y_1'(x) &= y_2(x) - 2y_1(x) + 2 \cos(x) \sin(x) \\y_2'(x) &= -3y_1(x) + y_2(x) - 8 \cos(x)^3 + 6 \cos(x)\end{aligned}$$

✓ Solution by Maple

Time used: 1.578 (sec). Leaf size: 146

```
dsolve([diff(y__1(x),x)=y__2(x)-2*y__1(x)+sin(2*x),diff(y__2(x),x)=-3*y__1(x)+y__2(x)-2*cos(x)^3+6*cos(x))])
```

$$\begin{aligned}y_1(x) &= c_2 e^{-\frac{x}{2}} \sin\left(\frac{\sqrt{3}x}{2}\right) + e^{-\frac{x}{2}} \cos\left(\frac{\sqrt{3}x}{2}\right) c_1 \\&\quad + \frac{16 \cos(3x)}{73} - \frac{4 \cos(2x)}{13} - \frac{6 \sin(3x)}{73} + \frac{7 \sin(2x)}{13} \\y_2(x) &= \frac{3c_2 e^{-\frac{x}{2}} \sin\left(\frac{\sqrt{3}x}{2}\right)}{2} + \frac{c_2 e^{-\frac{x}{2}} \sqrt{3} \cos\left(\frac{\sqrt{3}x}{2}\right)}{2} + \frac{3 e^{-\frac{x}{2}} \cos\left(\frac{\sqrt{3}x}{2}\right) c_1}{2} \\&\quad - \frac{e^{-\frac{x}{2}} \sqrt{3} \sin\left(\frac{\sqrt{3}x}{2}\right) c_1}{2} - \frac{60 \sin(3x)}{73} + \frac{9 \sin(2x)}{13} + \frac{14 \cos(3x)}{73} + \frac{6 \cos(2x)}{13}\end{aligned}$$

✓ Solution by Mathematica

Time used: 4.455 (sec). Leaf size: 223

```
DSolve[{y1'[x]==y2[x]-2*y1[x]+Sin[2*x],y2'[x]==-3*y1[x]+y2[x]-2*Cos[3*x]},{y1[x],y2[x]},x,Integrate]
```

$$\begin{aligned}y_1(x) &\rightarrow \frac{7}{13} \sin(2x) - \frac{6}{73} \sin(3x) - \frac{4}{13} \cos(2x) + \frac{16}{73} \cos(3x) \\ &\quad + c_1 e^{-x/2} \cos\left(\frac{\sqrt{3}x}{2}\right) - \sqrt{3}c_1 e^{-x/2} \sin\left(\frac{\sqrt{3}x}{2}\right) + \frac{2c_2 e^{-x/2} \sin\left(\frac{\sqrt{3}x}{2}\right)}{\sqrt{3}} \\ y_2(x) &\rightarrow \frac{9}{13} \sin(2x) - \frac{60}{73} \sin(3x) + \frac{6}{13} \cos(2x) + \frac{14}{73} \cos(3x) \\ &\quad + c_2 e^{-x/2} \cos\left(\frac{\sqrt{3}x}{2}\right) - 2\sqrt{3}c_1 e^{-x/2} \sin\left(\frac{\sqrt{3}x}{2}\right) + \sqrt{3}c_2 e^{-x/2} \sin\left(\frac{\sqrt{3}x}{2}\right)\end{aligned}$$

18.3 problem 3

Internal problem ID [12841]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 3.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = 2y_2(x)$$

$$y_2'(x) = 3y_1(x)$$

$$y_3'(x) = 2y_3(x) - y_1(x)$$

✓ Solution by Maple

Time used: 0.062 (sec). Leaf size: 107

```
dsolve([diff(y__1(x),x)=2*y__2(x),diff(y__2(x),x)=3*y__1(x),diff(y__3(x),x)=2*y__3(x)-y__1(x)
```

$$y_1(x) = e^{\sqrt{6}x}c_2 + c_3e^{-\sqrt{6}x}$$

$$y_2(x) = \frac{\sqrt{6} \left(e^{\sqrt{6}x}c_2 - c_3e^{-\sqrt{6}x} \right)}{2}$$

$$y_3(x) = \frac{2e^{2x}c_1}{(2 + \sqrt{6})(-2 + \sqrt{6})} + \frac{e^{-\sqrt{6}x}c_3}{2 + \sqrt{6}} - \frac{e^{\sqrt{6}x}c_2}{-2 + \sqrt{6}}$$

✓ Solution by Mathematica

Time used: 0.025 (sec). Leaf size: 232

```
DSolve[{y1'[x]==2*y2[x],y2'[x]==3*y1[x],y3'[x]==2*y3[x]-y1[x]},{y1[x],y2[x],y3[x]},x,Include
```

$$y1(x) \rightarrow \frac{1}{6}e^{-\sqrt{6}x} \left(3c_1 \left(e^{2\sqrt{6}x} + 1 \right) + \sqrt{6}c_2 \left(e^{2\sqrt{6}x} - 1 \right) \right)$$

$$y2(x) \rightarrow \frac{1}{4}e^{-\sqrt{6}x} \left(\sqrt{6}c_1 \left(e^{2\sqrt{6}x} - 1 \right) + 2c_2 \left(e^{2\sqrt{6}x} + 1 \right) \right)$$

$$y3(x) \rightarrow \frac{1}{12}e^{-\sqrt{6}x} \left(2 \left(c_2 \left(- \left(3 + \sqrt{6} \right) e^{2\sqrt{6}x} + 6e^{(2+\sqrt{6})x} - 3 + \sqrt{6} \right) + 6c_3 e^{(2+\sqrt{6})x} \right) \right. \\ \left. - 3c_1 \left(\left(2 + \sqrt{6} \right) e^{2\sqrt{6}x} - 4e^{(2+\sqrt{6})x} + 2 - \sqrt{6} \right) \right)$$

18.4 problem 4

Internal problem ID [12842]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 4.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = 2y_1(x)x - x^2y_2(x) + 4x$$

$$y_2'(x) = y_1(x)e^x + 3e^{-x}y_2(x) - 4\cos(x)^3 + 3\cos(x)$$

X Solution by Maple

```
dsolve([diff(y__1(x),x)=2*x*y__1(x)-x^2*y__2(x)+4*x,diff(y__2(x),x)=exp(x)*y__1(x)+3*exp(-x)
```

No solution found

X Solution by Mathematica

Time used: 0.0 (sec). Leaf size: 0

```
DSolve[{y1'[x]==2*x*y1[x]-x^2*y2[x]+4*x,y2'[x]==Exp[x]*y1[x]+3*Exp[-x]*y2[x]-Cos[3*x]},{y1[x]
```

Not solved

18.5 problem 5 a

Internal problem ID [12843]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 5 a.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = 2y_1(x) - 3y_2(x)$$

$$y_2'(x) = y_1(x) - 2y_2(x)$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 31

```
dsolve([diff(y__1(x),x)=2*y__1(x)-3*y__2(x),diff(y__2(x),x)=y__1(x)-2*y__2(x)],singsol=all)
```

$$y_1(x) = c_1 e^x + c_2 e^{-x}$$

$$y_2(x) = \frac{c_1 e^x}{3} + c_2 e^{-x}$$

✓ Solution by Mathematica

Time used: 0.021 (sec). Leaf size: 81

```
DSolve[{y1'[x]==-2*y1[x]-3*y2[x],y2'[x]==y1[x]-2*y2[x]},{y1[x],y2[x]},x,IncludeSingularSolut
```

$$y_1(x) \rightarrow e^{-2x} \left(c_1 \cos(\sqrt{3}x) - \sqrt{3}c_2 \sin(\sqrt{3}x) \right)$$

$$y_2(x) \rightarrow \frac{1}{3} e^{-2x} \left(3c_2 \cos(\sqrt{3}x) + \sqrt{3}c_1 \sin(\sqrt{3}x) \right)$$

18.6 problem 5 c

Internal problem ID [12844]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 5 c.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = 2y_1(x) - 3y_2(x) + 4x - 2$$

$$y_2'(x) = y_1(x) - 2y_2(x) + 3x$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 36

```
dsolve([diff(y__1(x),x)=2*y__1(x)-3*y__2(x)+4*x-2,diff(y__2(x),x)=y__1(x)-2*y__2(x)+3*x],sin
```

$$y_1(x) = c_2 e^x + e^{-x} c_1 + x$$

$$y_2(x) = \frac{c_2 e^x}{3} + e^{-x} c_1 - 1 + 2x$$

✓ Solution by Mathematica

Time used: 3.724 (sec). Leaf size: 101

```
DSolve[{y1'[x]==-2*y1[x]-3*y2[x]+4*x-2,y2'[x]==y1[x]-2*y2[x]+3*x},{y1[x],y2[x]},x,IncludeSin
```

$$y_1(x) \rightarrow -\frac{x}{7} + c_1 e^{-2x} \cos(\sqrt{3}x) - \sqrt{3} c_2 e^{-2x} \sin(\sqrt{3}x) + \frac{4}{49}$$

$$y_2(x) \rightarrow \frac{10x}{7} + c_2 e^{-2x} \cos(\sqrt{3}x) + \frac{c_1 e^{-2x} \sin(\sqrt{3}x)}{\sqrt{3}} - \frac{33}{49}$$

18.7 problem 6 a

Internal problem ID [12845]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 6 a.

ODE order: 1.

ODE degree: 1.

Solve

$$\begin{aligned}y_1'(x) &= \frac{5y_1(x)}{x} + \frac{4y_2(x)}{x} \\y_2'(x) &= -\frac{6y_1(x)}{x} - \frac{5y_2(x)}{x}\end{aligned}$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 34

```
dsolve([diff(y__1(x),x)=5/x*y__1(x)+4/x*y__2(x),diff(y__2(x),x)=-6/x*y__1(x)-5/x*y__2(x)],si
```

$$\begin{aligned}y_1(x) &= \frac{c_1x^2 + c_2}{x} \\y_2(x) &= -\frac{2c_1x^2 + 3c_2}{2x}\end{aligned}$$

✓ Solution by Mathematica

Time used: 0.017 (sec). Leaf size: 34

```
DSolve[{y1'[x]==5/x*y1[x]+4/x*y2[x],y2'[x]==-6/x*y1[x]-5/x*y2[x]},{y1[x],y2[x]},x,IncludeSim
```

$$\begin{aligned}y_1(x) &\rightarrow \frac{c_1}{x} + c_2x \\y_2(x) &\rightarrow -\frac{3c_1}{2x} - c_2x\end{aligned}$$

18.8 problem 6 c

Internal problem ID [12846]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 6 c.

ODE order: 1.

ODE degree: 1.

Solve

$$\begin{aligned}y_1'(x) &= \frac{5y_1(x)}{x} + \frac{4y_2(x)}{x} - 2x \\y_2'(x) &= -\frac{6y_1(x)}{x} - \frac{5y_2(x)}{x} + 5x\end{aligned}$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 44

```
dsolve([diff(y__1(x),x)=5/x*y__1(x)+4/x*y__2(x)-2*x,diff(y__2(x),x)=-6/x*y__1(x)-5/x*y__2(x)
```

$$\begin{aligned}y_1(x) &= \frac{c_1x^2 + 2x^3 + c_2}{x} \\y_2(x) &= -\frac{2c_1x^2 + 2x^3 + 3c_2}{2x}\end{aligned}$$

✓ Solution by Mathematica

Time used: 0.013 (sec). Leaf size: 44

```
DSolve[{y1'[x]==5/x*y1[x]+4/x*y2[x]-2*x,y2'[x]==-6/x*y1[x]-5/x*y2[x]+5*x},{y1[x],y2[x]},x,In
```

$$\begin{aligned}y_1(x) &\rightarrow 2x^2 + c_2x + \frac{c_1}{x} \\y_2(x) &\rightarrow -x^2 - c_2x - \frac{3c_1}{2x}\end{aligned}$$

18.9 problem 7

Internal problem ID [12847]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 7.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = 2y_1(x) + y_2(x) - 2y_3(x)$$

$$y_2'(x) = 3y_2(x) - 2y_3(x)$$

$$y_3'(x) = 3y_1(x) + y_2(x) - 3y_3(x)$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 65

```
dsolve([diff(y__1(x),x)=2*y__1(x)+y__2(x)-2*y__3(x),diff(y__2(x),x)=3*y__2(x)-2*y__3(x),diff
```

$$y_1(x) = c_1 e^x + \frac{c_2 e^{2x}}{2} + c_3 e^{-x}$$

$$y_2(x) = c_1 e^x + c_2 e^{2x} + c_3 e^{-x}$$

$$y_3(x) = c_1 e^x + \frac{c_2 e^{2x}}{2} + 2c_3 e^{-x}$$

✓ Solution by Mathematica

Time used: 0.012 (sec). Leaf size: 159

```
DSolve[{y1'[x]==2*y1[x]+y2[x]-2*y3[x],y2'[x]==3*y2[x]-2*y3[x],y3'[x]==3*y1[x]+y2[x]-3*y3[x]}
```

$$y_1(x) \rightarrow e^{-x}((e^x - 1)(c_2 e^{2x} - c_3 e^x - c_3) - c_1(-3e^{2x} + e^{3x} + 1))$$

$$y_2(x) \rightarrow e^{-x}(-(c_1(2e^x + 1)(e^x - 1)^2) + 2c_2 e^{3x} - (c_2 + c_3)e^{2x} + c_3)$$

$$y_3(x) \rightarrow e^{-x}(-(c_1(-3e^{2x} + e^{3x} + 2)) + c_2 e^{3x} - (c_2 + c_3)e^{2x} + 2c_3)$$

18.10 problem 8

Internal problem ID [12848]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 8.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = 5y_1(x) - 5y_2(x) - 5y_3(x)$$

$$y_2'(x) = -y_1(x) + 4y_2(x) + 2y_3(x)$$

$$y_3'(x) = 3y_1(x) - 5y_2(x) - 3y_3(x)$$

✓ Solution by Maple

Time used: 0.109 (sec). Leaf size: 71

```
dsolve([diff(y__1(x),x)=5*y__1(x)-5*y__2(x)-5*y__3(x),diff(y__2(x),x)=-1*y__1(x)+4*y__2(x)+2*y__3(x),diff(y__3(x),x)=3*y__1(x)-5*y__2(x)-3*y__3(x))
```

$$y_1(x) = e^{2x}(\sin(x) c_2 + \cos(x) c_3)$$

$$y_2(x) = -\frac{(2 \sin(x) c_2 - \sin(x) c_3 + \cos(x) c_2 + 2 \cos(x) c_3 - 5c_1) e^{2x}}{5}$$

$$y_3(x) = e^{2x}(\sin(x) c_2 + \cos(x) c_3 - c_1)$$

✓ Solution by Mathematica

Time used: 0.026 (sec). Leaf size: 109

```
DSolve[{y1'[x]==5*y1[x]-5*y2[x]-5*y3[x],y2'[x]==-1*y1[x]+4*y2[x]+2*y3[x],y3'[x]==3*y1[x]-5*y2[x]-3*y3[x]}
```

$$y_1(x) \rightarrow e^{2x}(c_1 \cos(x) + (3c_1 - 5(c_2 + c_3)) \sin(x))$$

$$y_2(x) \rightarrow e^{2x}(-c_1(\sin(x) + \cos(x) - 1) + c_3(2 \sin(x) + \cos(x) - 1) + c_2(2 \sin(x) + \cos(x)))$$

$$y_3(x) \rightarrow e^{2x}(c_1 \cos(x) + (3c_1 - 5(c_2 + c_3)) \sin(x) - c_1 + c_3)$$

18.11 problem 9

Internal problem ID [12849]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 9.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = 4y_1(x) + 6y_2(x) + 6y_3(x)$$

$$y_2'(x) = y_1(x) + 3y_2(x) + 2y_3(x)$$

$$y_3'(x) = -y_1(x) - 4y_2(x) - 3y_3(x)$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 63

```
dsolve([diff(y__1(x),x)=4*y__1(x)+6*y__2(x)+6*y__3(x),diff(y__2(x),x)=1*y__1(x)+3*y__2(x)+2*y__3(x),diff(y__3(x),x)=-1*y__1(x)-4*y__2(x)-3*y__3(x)),y__1(x),y__2(x),y__3(x))
```

$$y_1(x) = c_2 e^{4x} + c_3 e^{-x}$$

$$y_2(x) = \frac{c_2 e^{4x}}{3} + \frac{c_3 e^{-x}}{3} + c_1 e^x$$

$$y_3(x) = -\frac{7c_3 e^{-x}}{6} - \frac{c_2 e^{4x}}{3} - c_1 e^x$$

✓ Solution by Mathematica

Time used: 0.017 (sec). Leaf size: 145

```
DSolve[{y1'[x]==4*y1[x]+6*y2[x]+6*y3[x],y2'[x]==1*y1[x]+3*y2[x]+2*y3[x],y3'[x]==-1*y1[x]-4*y2[x]-3*y3[x]},y1[x],y2[x],y3[x]]
```

$$y_1(x) \rightarrow \frac{1}{5} e^{-x} ((5c_1 + 6(c_2 + c_3))e^{5x} - 6(c_2 + c_3))$$

$$y_2(x) \rightarrow \frac{1}{15} e^{-x} (-5(c_1 - 3c_2)e^{2x} + (5c_1 + 6(c_2 + c_3))e^{5x} - 6(c_2 + c_3))$$

$$y_3(x) \rightarrow \frac{1}{3}(c_1 - 3c_2)e^x + \frac{7}{5}(c_2 + c_3)e^{-x} - \frac{1}{15}(5c_1 + 6(c_2 + c_3))e^{4x}$$

18.12 problem 10

Internal problem ID [12850]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 10.

ODE order: 1.

ODE degree: 1.

Solve

$$\begin{aligned}y_1'(x) &= y_1(x) + 2y_2(x) - 3y_3(x) \\y_2'(x) &= -3y_1(x) + 4y_2(x) - 2y_3(x) \\y_3'(x) &= 2y_1(x) + y_3(x)\end{aligned}$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 102

```
dsolve([diff(y__1(x),x)=1*y__1(x)+2*y__2(x)-3*y__3(x),diff(y__2(x),x)=-3*y__1(x)+4*y__2(x)-2*y__3(x),diff(y__3(x),x)=2*y__1(x)+y__3(x))
```

$$\begin{aligned}y_1(x) &= \frac{e^{2x}(3 \cos(3x) c_2 + \cos(3x) c_3 + \sin(3x) c_2 - 3 \sin(3x) c_3 + c_1)}{2} \\y_2(x) &= \frac{e^{2x}(6 \cos(3x) c_2 - 2 \cos(3x) c_3 - 2 \sin(3x) c_2 - 6 \sin(3x) c_3 + 7c_1)}{4} \\y_3(x) &= e^{2x}(c_1 + \sin(3x) c_2 + \cos(3x) c_3)\end{aligned}$$

✓ Solution by Mathematica

Time used: 0.028 (sec). Leaf size: 176

```
DSolve[{y1'[x]==1*y1[x]+2*y2[x]-3*y3[x],y2'[x]==-3*y1[x]+4*y2[x]-2*y3[x],y3'[x]==2*y1[x]+0*y2[x]+y3[x]}
```

$$\begin{aligned}y_1(x) &\rightarrow \frac{1}{9}e^{2x}((11c_1 - 2(c_2 + c_3)) \cos(3x) - 3(c_1 - 2c_2 + 3c_3) \sin(3x) + 2(-c_1 + c_2 + c_3)) \\y_2(x) &\rightarrow \frac{1}{9}e^{2x}((7c_1 + 2c_2 - 7c_3) \cos(3x) + (-9c_1 + 6c_2 - 6c_3) \sin(3x) + 7(-c_1 + c_2 + c_3)) \\y_3(x) &\rightarrow \frac{1}{9}e^{2x}((4c_1 - 4c_2 + 5c_3) \cos(3x) + (6c_1 - 3c_3) \sin(3x) + 4(-c_1 + c_2 + c_3))\end{aligned}$$

18.13 problem 11

Internal problem ID [12851]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 11.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = -2y_1(x) - y_2(x) + y_3(x)$$

$$y_2'(x) = -y_1(x) - 2y_2(x) - y_3(x)$$

$$y_3'(x) = y_1(x) - y_2(x) - 2y_3(x)$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 51

```
dsolve([diff(y__1(x),x)=-2*y__1(x)-1*y__2(x)+1*y__3(x),diff(y__2(x),x)=-1*y__1(x)-2*y__2(x)-
```

$$y_1(x) = c_2 + c_3 e^{-3x}$$

$$y_2(x) = -c_2 - c_3 e^{-3x} + c_1 e^{-3x}$$

$$y_3(x) = -2c_3 e^{-3x} + c_2 + c_1 e^{-3x}$$

✓ Solution by Mathematica

Time used: 0.015 (sec). Leaf size: 130

```
DSolve[{y1'[x]==-2*y1[x]-1*y2[x]+1*y3[x],y2'[x]==-1*y1[x]-2*y2[x]-1*y3[x],y3'[x]==1*y1[x]-1*
```

$$y_1(x) \rightarrow \frac{1}{3} e^{-3x} (c_1 (e^{3x} + 2) - (c_2 - c_3) (e^{3x} - 1))$$

$$y_2(x) \rightarrow \frac{1}{3} e^{-3x} (-(c_1 (e^{3x} - 1)) + c_2 (e^{3x} + 2) - c_3 (e^{3x} - 1))$$

$$y_3(x) \rightarrow \frac{1}{3} e^{-3x} (c_1 (e^{3x} - 1) - c_2 (e^{3x} - 1) + c_3 (e^{3x} + 2))$$

18.14 problem 12

Internal problem ID [12852]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 12.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = y_1(x) + y_2(x) + 2y_3(x)$$

$$y_2'(x) = y_1(x) + y_2(x) + 2y_3(x)$$

$$y_3'(x) = 2y_1(x) + 2y_2(x) + 4y_3(x)$$

✓ Solution by Maple

Time used: 0.032 (sec). Leaf size: 42

```
dsolve([diff(y__1(x),x)=1*y__1(x)+1*y__2(x)+2*y__3(x),diff(y__2(x),x)=1*y__1(x)+1*y__2(x)+2*
```

$$y_1(x) = c_2 + c_3 e^{6x}$$

$$y_2(x) = c_2 + c_3 e^{6x} + c_1$$

$$y_3(x) = 2c_3 e^{6x} - c_2 - \frac{c_1}{2}$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 114

```
DSolve[{y1'[x]==1*y1[x]+1*y2[x]+2*y3[x],y2'[x]==1*y1[x]+1*y2[x]+2*y3[x],y3'[x]==2*y1[x]+2*y2
```

$$y_1(x) \rightarrow \frac{1}{6}(c_1(e^{6x} + 5) + (c_2 + 2c_3)(e^{6x} - 1))$$

$$y_2(x) \rightarrow \frac{1}{6}(c_1(e^{6x} - 1) + c_2(e^{6x} + 5) + 2c_3(e^{6x} - 1))$$

$$y_3(x) \rightarrow \frac{1}{3}(c_1(e^{6x} - 1) + c_2(e^{6x} - 1) + c_3(2e^{6x} + 1))$$

18.15 problem 13

Internal problem ID [12853]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 13.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = 2y_1(x) + y_2(x)$$

$$y_2'(x) = -y_1(x) + 2y_2(x)$$

$$y_3'(x) = 3y_3(x) - 4y_4(x)$$

$$y_4'(x) = 4y_3(x) + 3y_4(x)$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 82

```
dsolve([diff(y__1(x),x)=2*y__1(x)+1*y__2(x)+0*y__3(x)+0*y__4(x),diff(y__2(x),x)=-1*y__1(x)+2*y__2(x)+0*y__3(x)+0*y__4(x),diff(y__3(x),x)=3*y__3(x)-4*y__4(x),diff(y__4(x),x)=4*y__3(x)+3*y__4(x)),y__1(0)=1,y__2(0)=0,y__3(0)=0,y__4(0)=0)
```

$$y_1(x) = e^{2x}(\sin(x) c_3 + c_4 \cos(x))$$

$$y_2(x) = -e^{2x}(\sin(x) c_4 - \cos(x) c_3)$$

$$y_3(x) = e^{3x}(\cos(4x) c_2 + \sin(4x) c_1)$$

$$y_4(x) = -e^{3x}(\cos(4x) c_1 - \sin(4x) c_2)$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 92

```
DSolve[{y1'[x]==2*y1[x]+1*y2[x]+0*y3[x]+0*y4[x],y2'[x]==-1*y1[x]+2*y2[x]+0*y3[x]+0*y4[x],y3'[x]==3*y3[x]-4*y4[x],y4'[x]==4*y3[x]+3*y4[x],y1[0]==1,y2[0]==0,y3[0]==0,y4[0]==0},y1,y2,y3,y4,x]
```

$$y1(x) \rightarrow e^{2x}(c_1 \cos(x) + c_2 \sin(x))$$

$$y2(x) \rightarrow e^{2x}(c_2 \cos(x) - c_1 \sin(x))$$

$$y3(x) \rightarrow e^{3x}(c_3 \cos(4x) - c_4 \sin(4x))$$

$$y4(x) \rightarrow e^{3x}(c_4 \cos(4x) + c_3 \sin(4x))$$

18.16 problem 14

Internal problem ID [12854]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 14.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = y_2(x)$$

$$y_2'(x) = -3y_1(x) + 2y_3(x)$$

$$y_3'(x) = y_4(x)$$

$$y_4'(x) = 2y_1(x) - 5y_3(x)$$

✓ Solution by Maple

Time used: 0.109 (sec). Leaf size: 548

`dsolve([diff(y__1(x),x)=0*y__1(x)+1*y__2(x)+0*y__3(x)+0*y__4(x),diff(y__2(x),x)=-3*y__1(x)+0`

$$\begin{aligned}
 y_1(x) &= -\frac{c_1(4+\sqrt{5})^{\frac{3}{2}}\cos(\sqrt{4+\sqrt{5}x})}{11} - \frac{c_2(4-\sqrt{5})^{\frac{3}{2}}\cos(\sqrt{4-\sqrt{5}x})}{11} \\
 &\quad - \frac{c_3(4+\sqrt{5})^{\frac{3}{2}}\sin(\sqrt{4+\sqrt{5}x})}{11} - \frac{c_4(4-\sqrt{5})^{\frac{3}{2}}\sin(\sqrt{4-\sqrt{5}x})}{11} \\
 &\quad + \frac{8c_1\sqrt{4+\sqrt{5}}\cos(\sqrt{4+\sqrt{5}x})}{11} + \frac{8c_2\sqrt{4-\sqrt{5}}\cos(\sqrt{4-\sqrt{5}x})}{11} \\
 &\quad + \frac{8c_3\sqrt{4+\sqrt{5}}\sin(\sqrt{4+\sqrt{5}x})}{11} + \frac{8c_4\sqrt{4-\sqrt{5}}\sin(\sqrt{4-\sqrt{5}x})}{11} \\
 y_2(x) &= -c_1\sin(\sqrt{4+\sqrt{5}x}) - c_2\sin(\sqrt{4-\sqrt{5}x}) \\
 &\quad + c_3\cos(\sqrt{4+\sqrt{5}x}) + c_4\cos(\sqrt{4-\sqrt{5}x}) \\
 y_3(x) &= \frac{13c_1\sqrt{4+\sqrt{5}}\cos(\sqrt{4+\sqrt{5}x})}{22} + \frac{13c_2\sqrt{4-\sqrt{5}}\cos(\sqrt{4-\sqrt{5}x})}{22} \\
 &\quad + \frac{13c_3\sqrt{4+\sqrt{5}}\sin(\sqrt{4+\sqrt{5}x})}{22} + \frac{13c_4\sqrt{4-\sqrt{5}}\sin(\sqrt{4-\sqrt{5}x})}{22} \\
 &\quad - \frac{3c_1(4+\sqrt{5})^{\frac{3}{2}}\cos(\sqrt{4+\sqrt{5}x})}{22} - \frac{3c_2(4-\sqrt{5})^{\frac{3}{2}}\cos(\sqrt{4-\sqrt{5}x})}{22} \\
 &\quad - \frac{3c_3(4+\sqrt{5})^{\frac{3}{2}}\sin(\sqrt{4+\sqrt{5}x})}{22} - \frac{3c_4(4-\sqrt{5})^{\frac{3}{2}}\sin(\sqrt{4-\sqrt{5}x})}{22} \\
 y_4(x) &= \frac{c_1\sin(\sqrt{4+\sqrt{5}x})\sqrt{5}}{2} - \frac{c_2\sin(\sqrt{4-\sqrt{5}x})\sqrt{5}}{2} \\
 &\quad - \frac{c_3\cos(\sqrt{4+\sqrt{5}x})\sqrt{5}}{2} + \frac{c_4\cos(\sqrt{4-\sqrt{5}x})\sqrt{5}}{2} + \frac{c_1\sin(\sqrt{4+\sqrt{5}x})}{2} \\
 &\quad + \frac{c_2\sin(\sqrt{4-\sqrt{5}x})}{2} - \frac{c_3\cos(\sqrt{4+\sqrt{5}x})}{2} - \frac{c_4\cos(\sqrt{4-\sqrt{5}x})}{2}
 \end{aligned}$$

✓ Solution by Mathematica

Time used: 0.099 (sec). Leaf size: 730

`DSolve[{y1'[x]==0*y1[x]+1*y2[x]+0*y3[x]+0*y4[x],y2'[x]==-3*y1[x]+0*y2[x]+2*y3[x]+0*y4[x],y3'`

$$\begin{aligned}y_1(x) &\rightarrow \frac{1}{2}c_3\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{e^{\#1x}}{\#1^2 + 4}\&\right] \\ &+ \frac{1}{4}c_1\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{\#1^2e^{\#1x} + 5e^{\#1x}}{\#1^2 + 4}\&\right] \\ &+ \frac{1}{2}c_4\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{e^{\#1x}}{\#1^3 + 4\#1}\&\right] \\ &+ \frac{1}{4}c_2\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{\#1^2e^{\#1x} + 5e^{\#1x}}{\#1^3 + 4\#1}\&\right] \\ y_2(x) &\rightarrow \frac{1}{2}c_4\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{e^{\#1x}}{\#1^2 + 4}\&\right] \\ &+ \frac{1}{2}c_3\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{\#1e^{\#1x}}{\#1^2 + 4}\&\right] \\ &+ \frac{1}{4}c_2\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{\#1^2e^{\#1x} + 5e^{\#1x}}{\#1^2 + 4}\&\right] \\ &- \frac{1}{4}c_1\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{3\#1^2e^{\#1x} + 11e^{\#1x}}{\#1^3 + 4\#1}\&\right] \\ y_3(x) &\rightarrow \frac{1}{2}c_1\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{e^{\#1x}}{\#1^2 + 4}\&\right] \\ &+ \frac{1}{4}c_3\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{\#1^2e^{\#1x} + 3e^{\#1x}}{\#1^2 + 4}\&\right] \\ &+ \frac{1}{2}c_2\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{e^{\#1x}}{\#1^3 + 4\#1}\&\right] \\ &+ \frac{1}{4}c_4\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{\#1^2e^{\#1x} + 3e^{\#1x}}{\#1^3 + 4\#1}\&\right] \\ y_4(x) &\rightarrow \frac{1}{2}c_2\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{e^{\#1x}}{\#1^2 + 4}\&\right] \\ &+ \frac{1}{2}c_1\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{\#1e^{\#1x}}{\#1^2 + 4}\&\right] \\ &+ \frac{1}{4}c_4\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{\#1^2e^{\#1x} + 3e^{\#1x}}{\#1^2 + 4}\&\right] \\ &- \frac{1}{4}c_3\text{RootSum}\left[\#1^4 + 8\#1^2 + 11\&, \frac{5\#1^2e^{\#1x} + 11e^{\#1x}}{\#1^3 + 4\#1}\&\right]\end{aligned}$$

18.17 problem 15

Internal problem ID [12855]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 15.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = 3y_1(x) + 2y_2(x)$$

$$y_2'(x) = -2y_1(x) + 3y_2(x)$$

$$y_3'(x) = y_3(x)$$

$$y_4'(x) = 2y_4(x)$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 62

```
dsolve([diff(y__1(x),x)=3*y__1(x)+2*y__2(x)+0*y__3(x)+0*y__4(x),diff(y__2(x),x)=-2*y__1(x)+3
```

$$y_1(x) = e^{3x}(\sin(2x)c_1 + \cos(2x)c_2)$$

$$y_2(x) = -e^{3x}(\sin(2x)c_2 - \cos(2x)c_1)$$

$$y_3(x) = c_4e^x$$

$$y_4(x) = c_3e^{2x}$$

✓ Solution by Mathematica

Time used: 0.067 (sec). Leaf size: 255

```
DSolve[{y1'[x]==3*y1[x]+2*y2[x]+0*y3[x]+0*y4[x],y2'[x]==-2*y1[x]+3*y2[x]+0*y3[x]+0*y4[x],y3'
```

$$y1(x) \rightarrow e^{3x}(c_1 \cos(2x) + c_2 \sin(2x))$$

$$y2(x) \rightarrow e^{3x}(c_2 \cos(2x) - c_1 \sin(2x))$$

$$y3(x) \rightarrow c_3 e^x$$

$$y4(x) \rightarrow c_4 e^{2x}$$

$$y1(x) \rightarrow e^{3x}(c_1 \cos(2x) + c_2 \sin(2x))$$

$$y2(x) \rightarrow e^{3x}(c_2 \cos(2x) - c_1 \sin(2x))$$

$$y3(x) \rightarrow c_3 e^x$$

$$y4(x) \rightarrow 0$$

$$y1(x) \rightarrow e^{3x}(c_1 \cos(2x) + c_2 \sin(2x))$$

$$y2(x) \rightarrow e^{3x}(c_2 \cos(2x) - c_1 \sin(2x))$$

$$y3(x) \rightarrow 0$$

$$y4(x) \rightarrow c_4 e^{2x}$$

$$y1(x) \rightarrow e^{3x}(c_1 \cos(2x) + c_2 \sin(2x))$$

$$y2(x) \rightarrow e^{3x}(c_2 \cos(2x) - c_1 \sin(2x))$$

$$y3(x) \rightarrow 0$$

$$y4(x) \rightarrow 0$$

18.18 problem 16

Internal problem ID [12856]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 8. Linear Systems of First-Order Differential Equations. Exercises 8.3 page 379

Problem number: 16.

ODE order: 1.

ODE degree: 1.

Solve

$$y_1'(x) = y_2(x) + y_4(x)$$

$$y_2'(x) = y_1(x) - y_3(x)$$

$$y_3'(x) = y_4(x)$$

$$y_4'(x) = y_3(x)$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 71

```
dsolve([diff(y__1(x),x)=0*y__1(x)+1*y__2(x)+0*y__3(x)+1*y__4(x),diff(y__2(x),x)=1*y__1(x)+0*y__3(x)+0*y__4(x),diff(y__3(x),x)=0*y__3(x)+1*y__4(x),diff(y__4(x),x)=1*y__3(x)+0*y__4(x)),y__1(x)=0,y__2(x)=0,y__3(x)=0,y__4(x)=0)
```

$$y_1(x) = c_1 e^x + c_2 e^{-x}$$

$$y_2(x) = c_1 e^x - c_2 e^{-x} - c_3 e^x + c_4 e^{-x}$$

$$y_3(x) = c_3 e^x + c_4 e^{-x}$$

$$y_4(x) = c_3 e^x - c_4 e^{-x}$$

✓ Solution by Mathematica

Time used: 0.017 (sec). Leaf size: 148

```
DSolve[{y1'[x]==0*y1[x]+1*y2[x]+0*y3[x]+1*y4[x],y2'[x]==1*y1[x]+0*y2[x]-1*y3[x]+0*y4[x],y3'[x]==0*y3[x]+1*y4[x],y4'[x]==1*y3[x]+0*y4[x],y1[x]==0,y2[x]==0,y3[x]==0,y4[x]==0}
```

$$y_1(x) \rightarrow \frac{1}{2} e^{-x} (c_1 (e^{2x} + 1) + (c_2 + c_4) (e^{2x} - 1))$$

$$y_2(x) \rightarrow \frac{1}{2} e^{-x} (c_1 (e^{2x} - 1) + c_2 e^{2x} - c_3 e^{2x} + c_2 + c_3)$$

$$y_3(x) \rightarrow \frac{1}{2} e^{-x} (c_3 (e^{2x} + 1) + c_4 (e^{2x} - 1))$$

$$y_4(x) \rightarrow \frac{1}{2} e^{-x} (c_3 (e^{2x} - 1) + c_4 (e^{2x} + 1))$$

19 Chapter 10. Applications of Systems of Equations. Exercises 10.2 page 432

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19.1 problem 1

Internal problem ID [12857]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 10. Applications of Systems of Equations. Exercises 10.2 page 432

Problem number: 1.

ODE order: 1.

ODE degree: 1.

Solve

$$x'(t) = -2x(t) + 3y(t)$$

$$y'(t) = -x(t) + 2y(t)$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 31

```
dsolve([diff(x(t),t)=-2*x(t)+3*y(t),diff(y(t),t)=-x(t)+2*y(t)],singsol=all)
```

$$x(t) = c_1 e^t + c_2 e^{-t}$$

$$y(t) = c_1 e^t + \frac{c_2 e^{-t}}{3}$$

✓ Solution by Mathematica

Time used: 0.01 (sec). Leaf size: 72

```
DSolve[{x'[t]==-2*x[t]+3*y[t],y'[t]==-x[t]+2*y[t]},{x[t],y[t]},t,IncludeSingularSolutions ->
```

$$x(t) \rightarrow \frac{1}{2} e^{-t} (3c_2 (e^{2t} - 1) - c_1 (e^{2t} - 3))$$

$$y(t) \rightarrow -\frac{1}{2} e^{-t} (c_1 (e^{2t} - 1) + c_2 (1 - 3e^{2t}))$$

19.2 problem 2

Internal problem ID [12858]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 10. Applications of Systems of Equations. Exercises 10.2 page 432

Problem number: 2.

ODE order: 1.

ODE degree: 1.

Solve

$$x'(t) = -x(t) + 2y(t)$$

$$y'(t) = -2x(t) + 3y(t)$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 29

```
dsolve([diff(x(t),t)=-x(t)+2*y(t),diff(y(t),t)=-2*x(t)+3*y(t)],singsol=all)
```

$$x(t) = e^t(c_2t + c_1)$$

$$y(t) = \frac{e^t(2c_2t + 2c_1 + c_2)}{2}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 42

```
DSolve[{x'[t]==-x[t]+2*y[t],y'[t]==-2*x[t]+3*y[t]},{x[t],y[t]},t,IncludeSingularSolutions ->
```

$$x(t) \rightarrow e^t(-2c_1t + 2c_2t + c_1)$$

$$y(t) \rightarrow e^t(-2c_1t + 2c_2t + c_2)$$

19.3 problem 3

Internal problem ID [12859]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 10. Applications of Systems of Equations. Exercises 10.2 page 432

Problem number: 3.

ODE order: 1.

ODE degree: 1.

Solve

$$x'(t) = -x(t) - 2y(t)$$

$$y'(t) = 2x(t) - 3y(t)$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 76

```
dsolve([diff(x(t),t)=-x(t)-2*y(t),diff(y(t),t)=2*x(t)-3*y(t)],singsol=all)
```

$$x(t) = e^{-2t} \left(\sin(\sqrt{3}t) c_1 + \cos(\sqrt{3}t) c_2 \right)$$
$$y(t) = \frac{e^{-2t} (\sqrt{3} \sin(\sqrt{3}t) c_2 - \sqrt{3} \cos(\sqrt{3}t) c_1 + \sin(\sqrt{3}t) c_1 + \cos(\sqrt{3}t) c_2)}{2}$$

✓ Solution by Mathematica

Time used: 0.028 (sec). Leaf size: 96

```
DSolve[{x'[t]==-x[t]-2*y[t],y'[t]==2*x[t]-3*y[t]},{x[t],y[t]},t,IncludeSingularSolutions ->
```

$$x(t) \rightarrow \frac{1}{3} e^{-2t} \left(3c_1 \cos(\sqrt{3}t) + \sqrt{3}(c_1 - 2c_2) \sin(\sqrt{3}t) \right)$$
$$y(t) \rightarrow \frac{1}{3} e^{-2t} \left(3c_2 \cos(\sqrt{3}t) + \sqrt{3}(2c_1 - c_2) \sin(\sqrt{3}t) \right)$$

19.4 problem 4

Internal problem ID [12860]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 10. Applications of Systems of Equations. Exercises 10.2 page 432

Problem number: 4.

ODE order: 1.

ODE degree: 1.

Solve

$$x'(t) = -x(t) - 2y(t)$$

$$y'(t) = 5x(t) + y(t)$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 50

```
dsolve([diff(x(t),t)=-x(t)-2*y(t),diff(y(t),t)=5*x(t)+1*y(t)],singsol=all)
```

$$x(t) = c_1 \sin(3t) + c_2 \cos(3t)$$

$$y(t) = -\frac{3c_1 \cos(3t)}{2} + \frac{3c_2 \sin(3t)}{2} - \frac{c_1 \sin(3t)}{2} - \frac{c_2 \cos(3t)}{2}$$

✓ Solution by Mathematica

Time used: 0.008 (sec). Leaf size: 54

```
DSolve[{x'[t]==-x[t]-2*y[t],y'[t]==5*x[t]+1*y[t]},{x[t],y[t]},t,IncludeSingularSolutions ->
```

$$x(t) \rightarrow c_1 \cos(3t) - \frac{1}{3}(c_1 + 2c_2) \sin(3t)$$

$$y(t) \rightarrow c_2 \cos(3t) + \frac{1}{3}(5c_1 + c_2) \sin(3t)$$

19.5 problem 5

Internal problem ID [12861]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 10. Applications of Systems of Equations. Exercises 10.2 page 432

Problem number: 5.

ODE order: 1.

ODE degree: 1.

Solve

$$x'(t) = -x(t) + 2y(t)$$

$$y'(t) = -2x(t) - y(t)$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 45

```
dsolve([diff(x(t),t)=-x(t)+2*y(t),diff(y(t),t)=-2*x(t)-1*y(t)],singsol=all)
```

$$x(t) = e^{-t}(c_1 \sin(2t) + c_2 \cos(2t))$$

$$y(t) = e^{-t}(c_1 \cos(2t) - c_2 \sin(2t))$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 51

```
DSolve[{x'[t]==-x[t]+2*y[t],y'[t]==-2*x[t]-1*y[t]},{x[t],y[t]},t,IncludeSingularSolutions ->
```

$$x(t) \rightarrow e^{-t}(c_1 \cos(2t) + c_2 \sin(2t))$$

$$y(t) \rightarrow e^{-t}(c_2 \cos(2t) - c_1 \sin(2t))$$

19.6 problem 6

Internal problem ID [12862]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 10. Applications of Systems of Equations. Exercises 10.2 page 432

Problem number: 6.

ODE order: 1.

ODE degree: 1.

Solve

$$x'(t) = x(t) - 2y(t)$$

$$y'(t) = 2x(t) + y(t)$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 42

```
dsolve([diff(x(t),t)=x(t)-2*y(t),diff(y(t),t)=2*x(t)+1*y(t)],singsol=all)
```

$$x(t) = e^t(c_1 \sin(2t) + c_2 \cos(2t))$$

$$y(t) = -e^t(c_1 \cos(2t) - c_2 \sin(2t))$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 47

```
DSolve[{x'[t]==x[t]-2*y[t],y'[t]==2*x[t]+1*y[t]},{x[t],y[t]},t,IncludeSingularSolutions -> T
```

$$x(t) \rightarrow e^t(c_1 \cos(2t) - c_2 \sin(2t))$$

$$y(t) \rightarrow e^t(c_2 \cos(2t) + c_1 \sin(2t))$$

19.7 problem 7

Internal problem ID [12863]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 10. Applications of Systems of Equations. Exercises 10.2 page 432

Problem number: 7.

ODE order: 1.

ODE degree: 1.

Solve

$$x'(t) = -5x(t) - y(t) + 2$$

$$y'(t) = 3x(t) - y(t) - 3$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 39

```
dsolve([diff(x(t),t)=-5*x(t)-y(t)+2,diff(y(t),t)=3*x(t)-1*y(t)-3],singsol=all)
```

$$x(t) = \frac{5}{8} - \frac{e^{-4t}c_1}{2} + c_2e^{-2t}$$

$$y(t) = \frac{e^{-4t}c_1}{2} - 3c_2e^{-2t} - \frac{9}{8}$$

✓ Solution by Mathematica

Time used: 0.037 (sec). Leaf size: 93

```
DSolve[{x'[t]==-5*x[t]-y[t]+2,y'[t]==3*x[t]-1*y[t]-3},{x[t],y[t]},t,IncludeSingularSolutions
```

$$x(t) \rightarrow \frac{1}{48}e^{-4t}(30e^{4t} - (1 + 24c_1 + 24c_2)e^{2t} + 3 + 72c_1 + 24c_2)$$

$$y(t) \rightarrow \frac{1}{16}e^{-4t}(-18e^{4t} + (1 + 24c_1 + 24c_2)e^{2t} - 1 - 24c_1 - 8c_2)$$

19.8 problem 8

Internal problem ID [12864]

Book: Ordinary Differential Equations by Charles E. Roberts, Jr. CRC Press. 2010

Section: Chapter 10. Applications of Systems of Equations. Exercises 10.2 page 432

Problem number: 8.

ODE order: 1.

ODE degree: 1.

Solve

$$x'(t) = 3x(t) - 2y(t) - 6$$

$$y'(t) = 4x(t) - y(t) + 2$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 57

```
dsolve([diff(x(t),t)=3*x(t)-2*y(t)-6,diff(y(t),t)=4*x(t)-1*y(t)+2],singsol=all)
```

$$x(t) = -2 + e^t(c_1 \cos(2t) + c_2 \sin(2t))$$

$$y(t) = -6 + e^t(c_1 \cos(2t) - c_2 \cos(2t) + c_1 \sin(2t) + c_2 \sin(2t))$$

✓ Solution by Mathematica

Time used: 0.358 (sec). Leaf size: 64

```
DSolve[{x'[t]==3*x[t]-2*y[t]-6,y'[t]==4*x[t]-1*y[t]+2},{x[t],y[t]},t,IncludeSingularSolution
```

$$x(t) \rightarrow c_1 e^t \cos(2t) + (c_1 - c_2) e^t \sin(2t) - 2$$

$$y(t) \rightarrow c_2 e^t \cos(2t) + (2c_1 - c_2) e^t \sin(2t) - 6$$